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Verification and Validation of Earthquake Ground Motion Simulation in the San Francisco Bay Area with SW4

Arthur Rodgers Lawrence Livermore National Laboratory

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LLNL-PRES-823639

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Thanks to many coworkers over the years



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- Bjorn Sjogreen (LLNL, CASC)
- Arben Pitarka (LLNL, AEED)
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- Rob Graves, Brad Aagaard (USGS)
- Computing Facilities
 - Livermore Computing (LLNL)
 - OLCF (Oak Ridge Lab)
 - NERSC (LBNL)



3D Seismic wave propagation simulations are complex, require verification and validation

- Ground motions depend on several factors simulations must all of these get correct
- V&V are crucial to demonstrating accuracy and confidence Key to acceptance of simulated ground motions
- Numerical method must be accurate
- **Verification** Computer code must solve the algorithm correctly

Related topic: Performance benchmarking

- Validation Inputs must be accurate and physically meaningful
 - Source, earthquake rupture
 - Earth model must represent true 3D structure
 - Path propagation effects: crustal, basin, topographic structure
 - Site effects: minimum shear wavespeed, linear and non-linear response

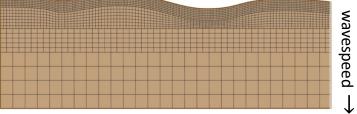


SW4: seismic wave propagation code based on the summation-by-parts FD method

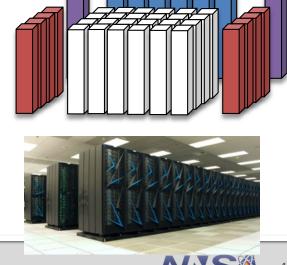
- Summation-by-parts FDTD
 - Node-centered, displacement formulation
 - Not velocity-stress staggered grid!
 - Accurate, provably stable & energy conserving
 - Super-grid boundary conditions
- SW4 is 4th order accurate (time & space)
 - Fully 3D material models (iso- and anisotropic)
 - Topography (curvilinear mesh)
 - Mesh refinement in Curv. & Cart. meshes
 - Accurate at boundaries & interfaces, w/ hanging nodes
- Optimized for the hardware
 - Many core CPU's (e.g. NERSC's Cori-II)
 - Hybrid MPI/OpenMP communications
 - GPU's (e.g. Sierra & Summit)
 - RAJA directs work on GPU's

github.com/geodynamics/sw4

Curvilinear mesh with refinements

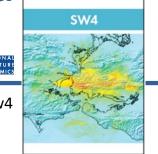


Cartesian mesh with refinements









Our demonstration problem: Hayward Fault M_w 7.0 scenario earthquake EXASCALE COMPUTING PROJEC

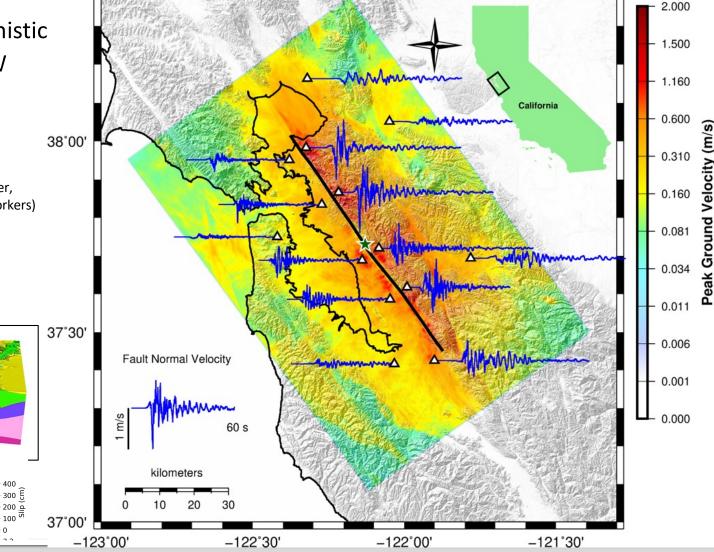
Regional-scale

SW4

- Broadband, fully deterministic
 - f_{max} = 10 Hz @ 8 PPW
 - h_{min} = 6.25, 3.125 m
 - $\lambda_{min} = 50, 25 \text{ m}$
 - v_{Smin} = 500, 250 m/s
- 3D USGS model (Jachens, Brocher, Aagaard & coworkers)
 - Surface topography

≥USGS

- Anelasticity, Q
- Graves & Pitarka ruptures



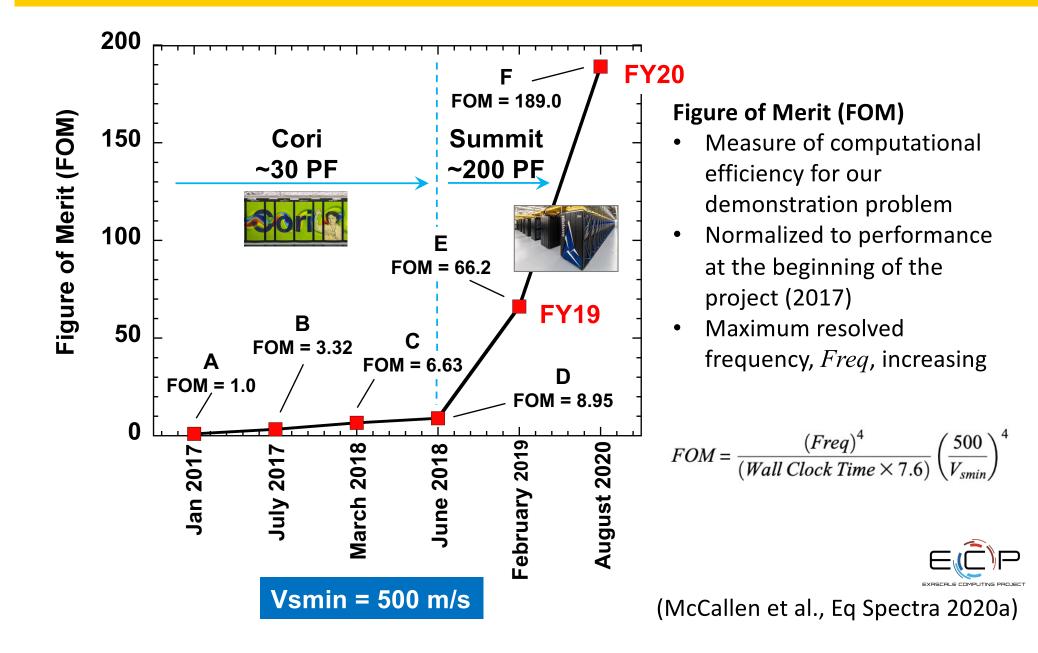
North



m7.0-77.0x13.0.s020.hypoL.v5.1.srl

100

FY20 EQSIM performance evaluation for a M7 Hayward fault SFBA simulation



Verification: the accuracy of mathematics and computation of numerical simulations

- Comparison of computed solutions (time-series) against analytic solutions or other computed solutions
- Goal: to obtain accurate and reliable simulations of seismic response and build confidence in solutions
- Criteria for comparing waveforms
 - Pointwise differences with analytic or 1D semi-analytic solution (e.g. reflectivity)
 - Anderson (2004) Goodness-of-fit score of waveform measurements
 - Kristekova et al. (2006) time-frequency phase and envelope misfit
 - wavelet-based decomposition
- A few notable examples:
 - S. M. Day, J. Bielak, D. Dreger, S. Larsen, R. Graves, A. Pitarka, and K. B. Olsen (2003).
 Test of 3D elastodynamic codes: Lifelines program task 1A02. Technical report, PEER & SCEC.
 - Moczo et al. (2006). Comparison of Numerical Methods for Seismic Wave Propagation and Source Dynamics - the SPICE Code Validation, ESG2006, Grenoble, France
 - Bielak et al. (GJI, 2010) Compares 3 SCEC ShakeOut simulations
 - Chaljub et al. (GJI, 2015) Mygdonian Basin, Greece: stringent methods



SW4 uses the method of manufactured solutions for accuracy & convergence: "twilight mode"

Elastodynamic equations of motion in 3D $\rho \mathbf{u}_{tt} = \nabla \cdot \mathcal{T} + \mathbf{F}(\mathbf{x}, t), \quad \mathbf{x} \text{ in } \Omega, \ 0 \le t \le T,$ $\mathbf{u}(\mathbf{x}, 0) = 0, \quad \mathbf{u}_t(\mathbf{x}, 0) = 0, \quad \mathbf{x} \text{ in } \Omega.$

A.1 Method of manufactured solutions

The method of manufactured solutions provides a general way of testing the accuracy of numerical solutions of partial differential equations, including effects of heterogeneous material properties and various boundary conditions on complex geometries. The test scripts can be found in the directory

.../sw4/examples/twilight

In these tests, we take the material properties to be

$$\rho(x, y, z) = A_{\rho} \left(2 + \sin(\omega_m x + \theta_m) \cos(\omega_m y + \theta_m) \sin(\omega_m z + \theta_m)\right),$$

$$\mu(x, y, z) = A_{\mu} \left(3 + \cos(\omega_m x + \theta_m) \sin(\omega_m y + \theta_m) \sin(\omega_m z + \theta_m)\right),$$

$$\lambda(x, y, z) = A_{\lambda} \left(2 + \sin(\omega_m x + \theta_m) \sin(\omega_m y + \theta_m) \cos(\omega_m z + \theta_m)\right).$$
But the probability of the second secon

The internal forcing, boundary forcing and initial conditions are chosen such that the exact (manufactured) solution becomes 1 Chosen response

$$u_e(x, y, z, t) = \sin(\omega(x - c_e t)) \sin(\omega y + \theta) \sin(\omega z + \theta),$$

 $v_e(x, y, z, t) = \sin(\omega x + \theta) \sin(\omega(y - c_e t)) \sin(\omega z + \theta),$
 $w_e(x, y, z, t) = \sin(\omega x + \theta) \sin(\omega y + \theta) \sin(\omega(z - c_e t)).$

The values of the material parameters $(\omega_m, \theta_m, A_\rho, A_\lambda, A_\mu)$ and the solution parameters (ω, θ, c_e) , can be modified in the input script. Since the exact solution is know, it is possible to evaluate the error in the numerical solution. By repeating the same test on several grid sizes, it is possible to establish the convergence rate of the numerical method.

- Compare computed and analytic solutions
- Compute norm for different grid spacing
- Measure convergence

From SW4 User Guide, Petersson & Sjogreen, 2021





Recent porting of SW4 to GPU/CPU platforms requires verification of code: 0-5 Hz HF M7

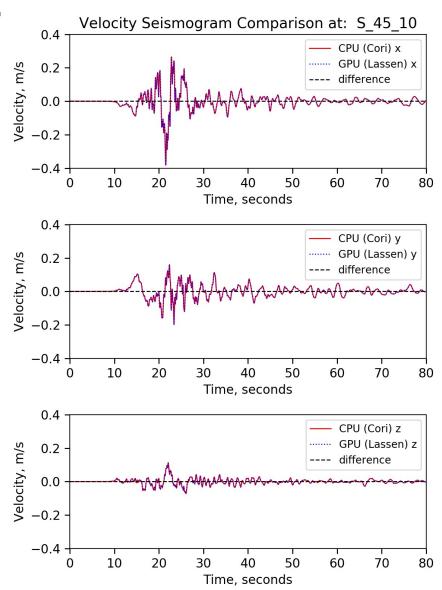
SW4 uses RAJA C++ package to manage work on GPU

SW4-RAJA uses the same source code as SW4 and a machine-specific profile to know how to offload compute intensive loops to GPU

Hayward Fault, M_W 7.0, resolved 0-5 Hz

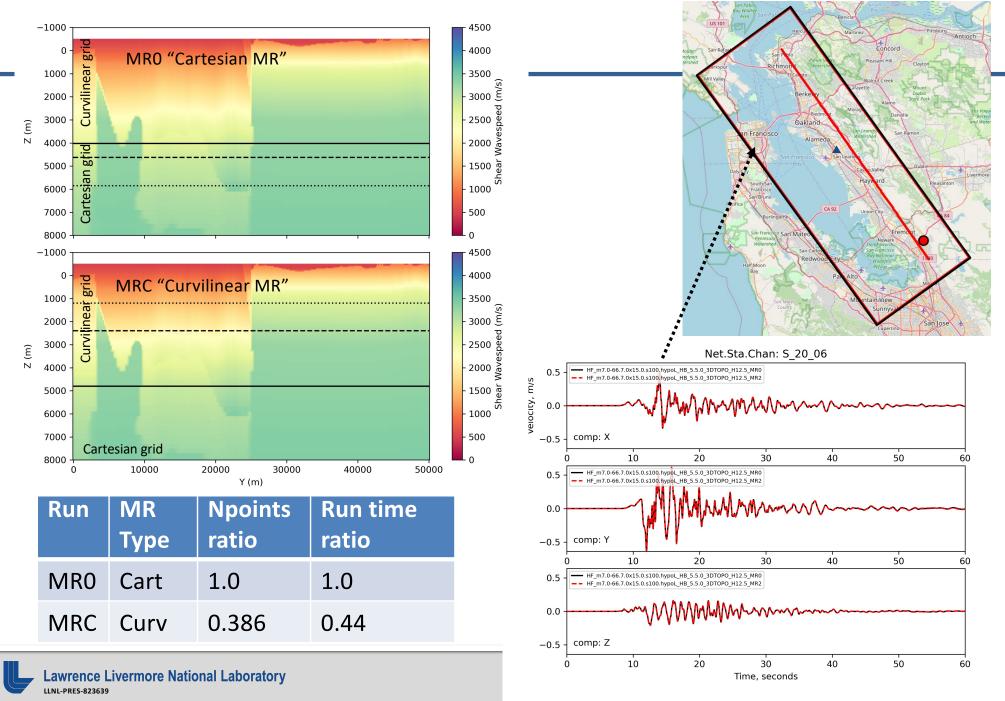
Use point-wise differences

- We get excellent agreement
- Waveforms agree to 10⁻⁷
- 3-component waveforms at 2301 sites





Verfication of mesh refinement cases



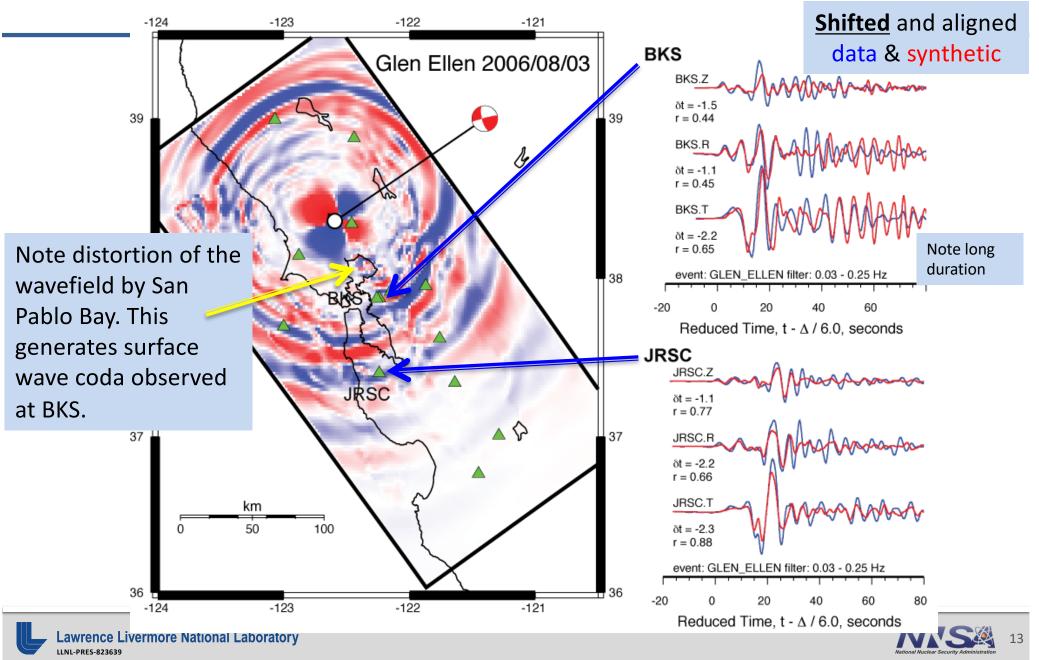
Validation: the evaluation of the physical accuracy of numerical simulation

- Comparison of computed solutions against empirical data
 Tests inputs: source and Earth model with a verified code
- Goal: to ensure that simulation predictions are realistic and consistent with empirical observations, to build confidence
- Moderate (M_W 3-5) earthquakes provide data sets for testing 3D Earth models in California
 - A few examples:
 - Rodgers et al., (BSSA, 2008) SFBA moderate events, waveforms
 - Kim et al. (BSSA, 2021) SFBA moderate events, intensities
 - Olsen & Mayhew (SRL, 2010) 2008 Chino Hills GOF
 - Taborda & Bielak (BSSA, 2013) 2008 Chino Hills
 - Hirakawa and Aagaard (SSA, 2021) update(s) of USGS SFBA model
- Large scenario events without empirical data
 - Compare with ground motion models (GMM's, GMPE's) or data from similar events

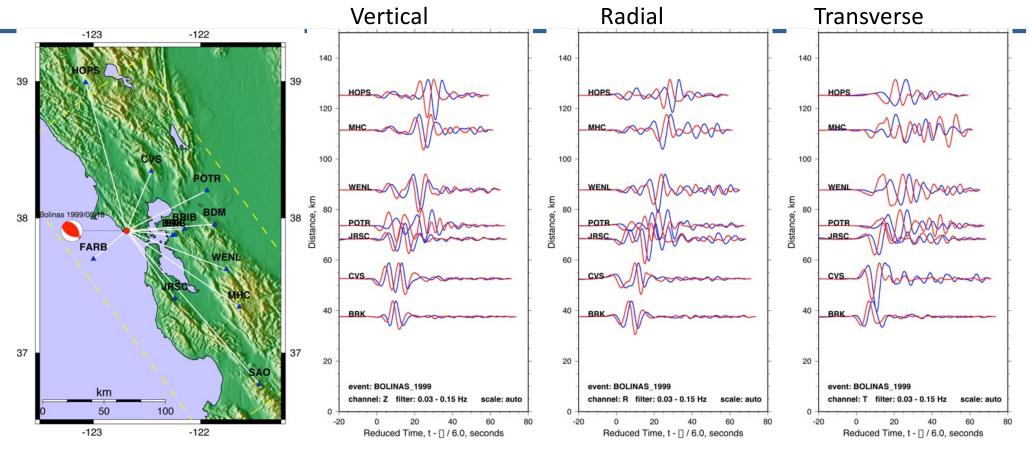


Earlier evaluation of the USGS 3D model using moderate events & long-periods (33-4 sec.) -121 -120Events, BB (BK) Stations Gevsers 2004/02/18 & Paths 39 39 Moderate (M_W 4-5) ountville 2000/09/03 Glen Ellen 200 12 events (circles) Bolinas 1999/08/18 38 38 Dublin 2003/02/0 15 stations (triangles) Coverage uneven, many Gilroy 2002/05/ 37 37 paths along Hayward Fault San Juan Bautista 1998 Rodgers et al. (BSSA, 2008) km 36 36 75 150 -124 -123-122 -121 -120

Long-period waveform comparisons for August 3 2006, Glen Ellen Earthquake



Long-period waveform comparisons for Aug. 18 1999, Bolinas Earthquake



Frequencies = 0.03-0.15 Hz Periods = 7-33 seconds

Delays increase with distance, suggests systematic bias
Note amplitudes are well matched
see Kim, Dreger & Larsen, BSSA (2010)

Data such these are useful for waveform tomography



More recent effort looking at shorter 39° periods: 1-32 sec.

8 events M_w 4.4-5.5 1998-present

With strong-motion sites

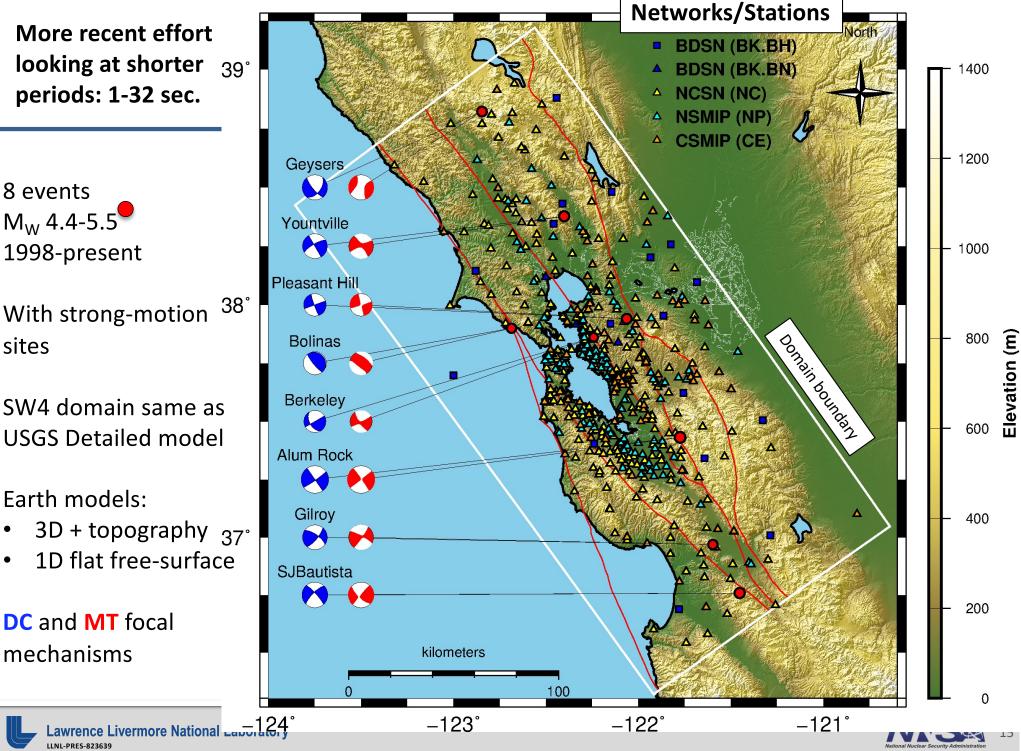
SW4 domain same as **USGS** Detailed model

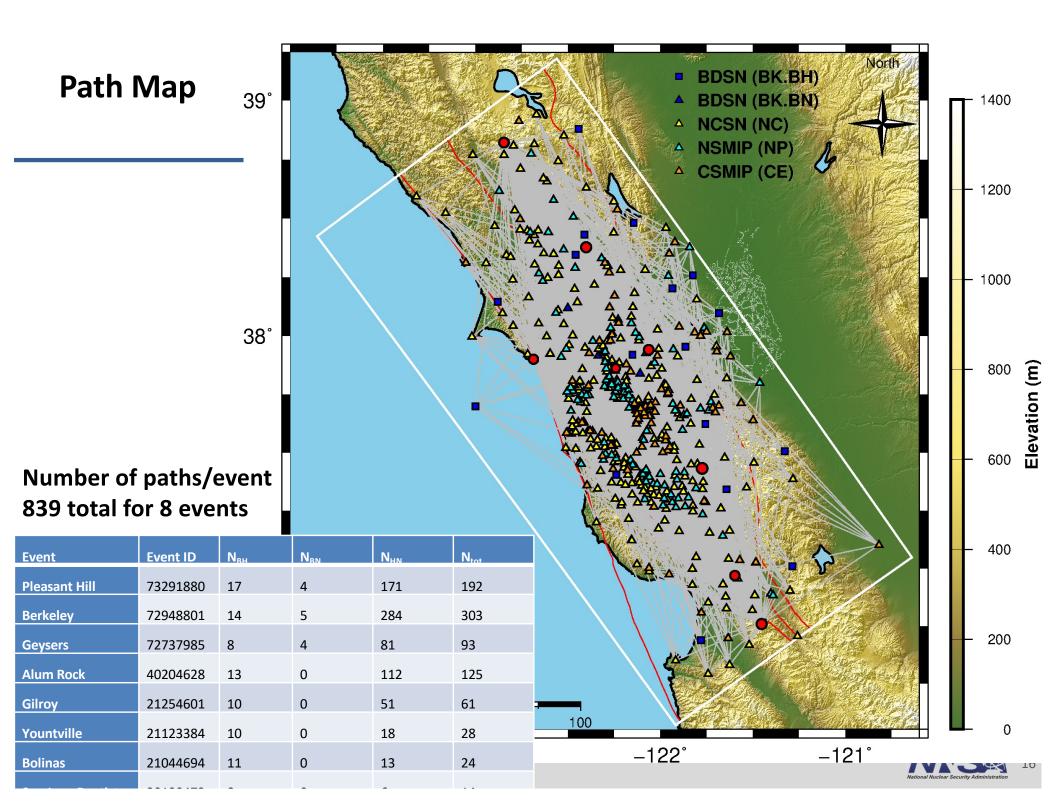
Earth models:

mechanisms

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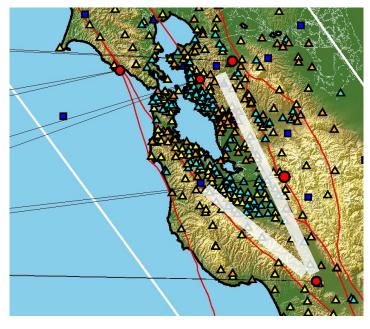
- $3D + topography _{37^{\circ}}$
- 1D flat free-surface



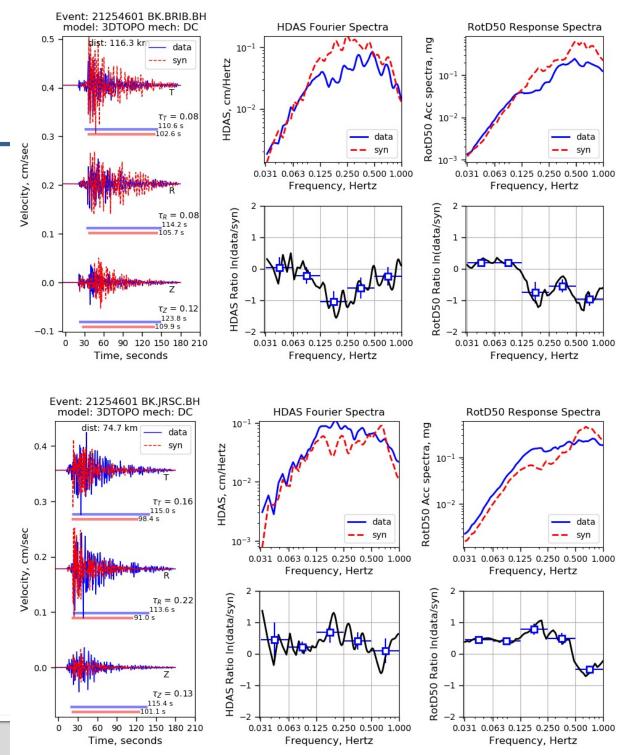


Gilroy 2002-05-14 Mw 4.9 to BDSN broadband stations

Path through East Bay Hills: USGS 3D model produces higher amplitudes than observed

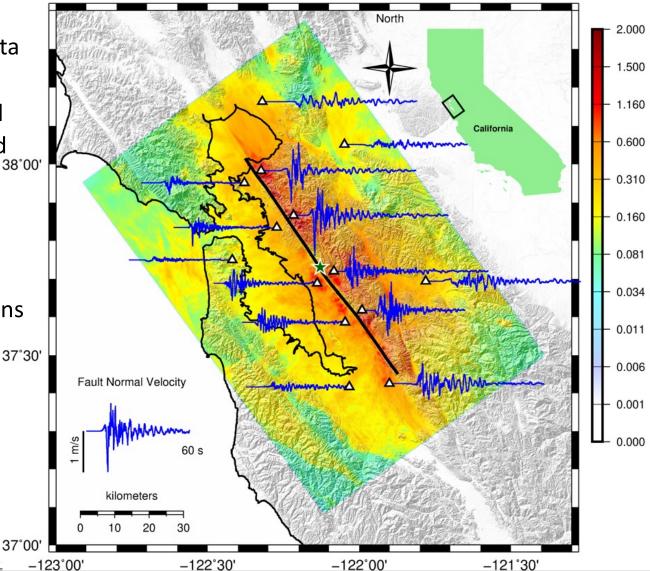


Path through Santa Cruz Mtns: USGS 3D model produces relatively unbiased amplitudes



Our demonstration problem: Hayward Fault M_w 7.0 scenario earthquake

- In the absence of empirical data for scenario earthquakes,
- we compare simulated ground motion intensities with ground ^{38'00'} motion models
- Recall that we are pushing the limits of fully deterministic scenario earthquake simulations to f_{max} = 10 Hz
- This potentially exposes shortcomings of our:
 - source model
 - v_{Smin} = 500 m/s
 - linear wave propagation 37°00







Peak Ground

Several recent papers focus on simulations of **M7 Hayward Fault scenario earthquakes**

omputing Science Rengineering

Toward Exascale Earthquake Ground Motion Simulations for Near-Fault Engineering Analysis IEEE

Hans Johansen I Lawrence Berkelev National Laboratory Arthur Rodgers and N. Anders Petersson I Lawrence Livermore National Laboratory David McCallen I Lawrence Berkeley National Laboratory Biorn Siggreen | Lawrence Livermore National Laboratory Mamun Miah I Lawrence Berkelev National Laboratory

Application modernization for massively parallel time-domain simulations of earthquake ground motion in 3D models is increasing application resolution and providing ground motion estimates for critical infrastructure risk evaluations. Improvements to the geophysics application code SW4 algorithms, developed while porting the code to systems at Lawrence Berkeley National Laboratory, revealed that reorganizing operation order can improve performance for massive problems



Broadband (0–5 Hz) Fully Deterministic 3D Ground-Motion Simulations of a Magnitude 7.0 Hayward Fault Earthquake: Comparison with Empirical Ground-Motion Models and 3D Path and Site Effects from Source Normalized Intensities

by Arthur J. Rodgers, N. Anders Petersson, Arben Pitarka, David B. McCallen, Bjorn Sjogreen, and Norman Abrahamson

ABSTRACT

We report on high-performance computing (HPC) fully deterministic simulation of ground motions for a momenter magnitude (M₂ - 7) as summarised sequence of the Harward fault o from a model of the U.S. Geological Survey (USGS). The realing ground-motion internitios cover a broader frequency range than typically considered in regional-scale simulations, including higher frequencies relevant for engineering analysis of structures. Median intensities for sites across the domain are within the reportence barvener-newn tuccrimities (r) of ground-motion models (GMMs) across spectral periods 0.2–10 s. (frequencies 0.1–5 Hz). The within-the expected deviation ϕ of ground-motion intensity measurement residuals range Ø of ground-motion intensity measurement residuals range 02–05, natural log units with values consistently larger for the 3D model. Source-normalized ratios of intensities (3D/ 1D) reveal patterns of path and site effects that are correlated with known goologic structure. These results demonstrate that earthquake simulations with fully deterministic wave propaga-tion in 3D Earth models on HPC platforms produce broad-tion in 3D Earth models on HPC platforms produce broad-tions. band ground motions with median and within-event aleatory variability consistent with empirical models. Systematic inten-sity variations for the 3D model caused by path and site effects suggest that these epistemic effects can be estimated and removed to reduce variation in site-specific hazard estimates.

This study motivates future work to evaluate the validity of the USGS 3D model and investigate the development of path and site corrections by running more scenarios.

Supplemental Content: Animation of ground motions from the 3D subsurface model with topography.

INTRODUCTION

The Hayward fault (HF) dominates seismic hazard in the e The Hypward failt (HP) dominates some haust in the casers San Francisco Bay and S(FAA), also offend to a she "Ear Bay" Currently, the HF and its northern extension, the Rodgers Corch failt, represent the none Table frait has the SFBA to represe with a moment magnitude (M_{10}) 67 or genere in the next 30 yrs according to the Uniform California Endphasic Represe Forecase, Version 3 (Field and 2014 Working Group on California Endpathe Probabilities, 2015), Egne 1 shows the area of interest for this study. The HF is capible of entrphaskes more M. 72 and enterns aimformed meand acroin haven the up to M_w 7.0 and presents significant ground-motion hazard to the heavily populated East Bay cities, including Oakland, Berkeley, Hayward, and Fremont. The last major HF rupture occurred on 21 October 1868 with an Mw 6.8-7.0 event (Toppozada et al. 1981, 2002; Bakun, 1999). Instrumental observations of this earthquake are not available; however, historical triangulation data inform the moment magnitude and fault length (7.0 and 52 km, respectively; Yu and Seagall, 1996). Reported intensities were used to create a ShakeMap for the 1868 event (Be and Bundock 2008) Modified Mercalli intensities of VII-IX

1268 Seismological Research Letters Volume 90, Number 3 May/June 2019

doi: 10.1785/022018026

@AGU PUBLICATIONS

Geophysical Research Letters

Correspondence C J Rodgers,

RESEARCH LETTER Broadband (0-4 Hz) Ground Motions for a Magnitude 7.0 Hayward Fault Earthquake With Three-Dimensional Structure and Topography

Arthur J. Rodgers^{1,2,3} , Arben Pitarka¹, N. Anders Petersson⁴ , Björn Sjögreen⁴ and David B. McCallen^{2,5}

¹Atmospheric, Earth and Energy Division and Geophysical Monitoring Program, Lawrence Livermore National Laborato Livermore, AC, USA, ¹Energy Geociences Division, Lawrence Benkeley National Laboratori, Benkeley, AC, USA, ¹Benkeley Stermological Laboratory, University of California, Benkeley, AC, USA, ¹Centrol ef Applied Sternife Computing Laboratori Livermore National Laboratory, Livermore, CA USA, ¹Office of the President, University of California, Oakland, CA USA

Abstract We performed fully deterministic broadband (0-4 Hz) high-performance computing group is of a magnitude 7.0 scenario earthquake on the Hay ward Fault (HF) in the Sa motion simulations of a mapphade 72 a scenario cartinguine on the toyourd Fault 0PI in the sin Francison Birk Jaok 2PI and Section Conduct arrange of chemiscian (11) and internet measures (CMMM) for the 3D model Elipsky dramat, difference across the HT data to policy internet measures (CMMM) for the 3D model Elipsky dramat, difference across the HT data to policy difference acrossing the section of the Granut Modern Teedotton Equations (GMTE); however, the 3D model generates measures that the section of conditions the data to Equations (GMTE); however, the 3D model generates measures that the section of conditions the data to the section of the section of the GMTE productions using entition the section of the section of the GMTE productions are on average consistent with empiral data.

empirationa. Plain Languege Summary With the use of powerful supercomputers and an efficient numer method, modeling of ground shaking for a magnitude 70 cartinguake on the Hoyward Fault results in more relation motions than prevolvay.exteed. The model inclusion for uncertainty and the superscenario Earth gleology and surface toppography to compute seismic wave ground shaking throughout the neglity Saking intensity shows differences across the Hayward Fall that that for how of of different geology. ation of the origin. On average, results are consistent with models based on actual recorded earthquake r round the world. This study shows that powerful supercomputing can be used to calculate earthquake shaking with more realism than previously obtained.



Regional-Scale 3D Ground-Motion Simulations of $M_{\rm w}$ 7 Earthquakes on the Hayward Fault, Northern California Resolving Frequencies 0-10 Hz and Including Site-Response Corrections

Arthur J. Rodgers^{*1,2}, Arben Pitarka¹, Ramesh Pankaiakshan³, Biorn Sibgreen⁴, and N. Ander

ARSTRACT ABSTRACT Deep earthquake ground-motion simulations in 10 Earth models provide constraints of provide de regionarie motion simulations in 10 Earth models provide constraints of provide de regionarie in soft table. We report new regional scale 3D simulations for moment magnitude 7D sensino samphages on the Hayward Price, motion 2D simulations with 3VM simulations resolved significantly breader land frequencies D-10 Hg the pre-sensition of the simulation of the simulation of the simulation of the distance of the simulation of the simulation of the simulation of the distance of the simulation of the simulation of the simulation of the distance of the simulation of the simulation of the simulation of the distance of the simulation of the simulation of the simulation of the distance of the simulation of the simulation of the simulation of the distance of the simulation of the simulation of the simulation of the distance of the simulation of the simulation of the simulation of the distance of the simulation of the simulation of the simulation of the distance of the simulation of the simulation of the simulation of the distance of the simulation of the simulation of the simulation of the distance of the simulation of the simulation of the simulation of the distance of the simulation of the simulation of the simulation of the distance of the simulation of the simulation of the simulation of the distance of the simulation of the simulation of the simulation of the simulation of the distance of the simulation of the simulation of the simulation of the simulation of the distance of the simulation of the distance of the simulation of the simulatio U.S. Geological survey (USSG) surveying a minimum there are varveyspeed, $V_{\rm inc.,0} \ll 500$ m/s. We correct motions for finanz and one-finanz inter-messions for the surveyspeed V. Y. See the surveyspeed V. See the sur

KEY POINTS

Advanced methods and computing enable high resolution regional-scale 3D earthquake ground motion simulations Average sch-corrected intensities for M₂, 7 Hayward fault ruptures are in agreement with ergodic models.
 Site-specific intensities reveal variations related to wave propagation in the 3D Earth (path and site effects).

nic hazard analyses typically rely on ground-motion mod-

lytical seismological and geotechnical (site-response) models. Volume XX Number XX - 2020 www.bssaonline.on

For example, GMMs from the Pacific Earthquake Engineering Research Center Next Generation Attenuation-West2 (NGA-West2) Project (Abrahamson *et al.*, 2014; Boore *et al.*, 2014;

Bulletin of the Seismological Society of America • 1

EOSIM—A multidisciplinary framework for fault-tostructure earthquake simulations on exascale computers part I: **Computational models and** workflow

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D D EARTHQUAKE

RU SPECTRA

(\$)SAGE

David McCallen, M. EERI^{1,2}, Anders Petersson³, Arthur Rodgers³, Arben Pitarka³, Mamun Miah², Floriana Petrone, M. EERI^{1,2}, Bjorn Sjogreen³, Norman Abrahamson⁴, and Houjun Tang²

Research Paper

Research Paper

EOSIM—A multidisciplinary framework for fault-tostructure earthquake simulations on exascale computers, part II: Regional simulations of building response

DD EARTHQUAKE **RI SPECTRA** Earthquake Spectra

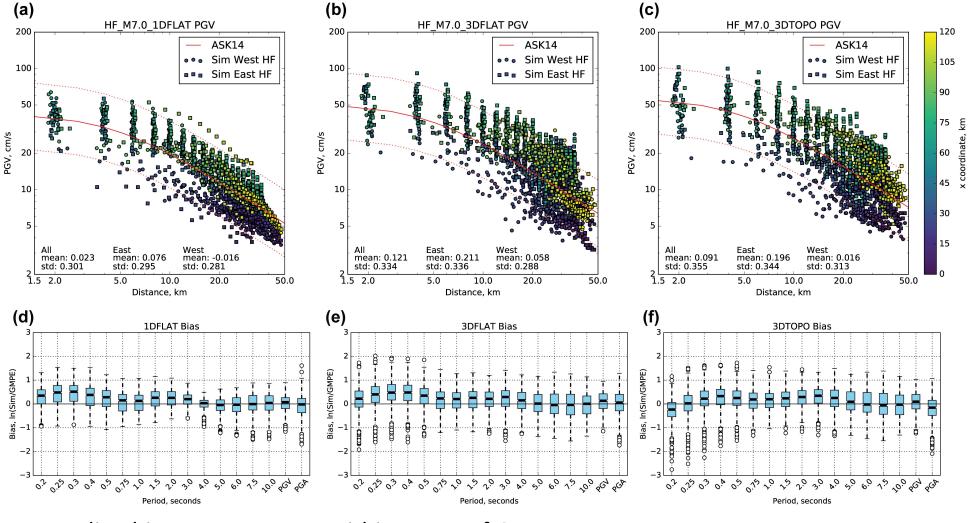
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David McCallen, M.EERI^{1,2}, Floriana Petrone, M.EERI^{1,2}, Mamun Miah², Arben Pitarka³, Arthur Rodgers³, and Norman Abrahamson⁴



Lawrence Livermore National Laboratory LLNL-PRES-823639

HF M7 0-4 Hz compared to ASK (2014) GMM



Median bias are near zero, within one σ of GMM

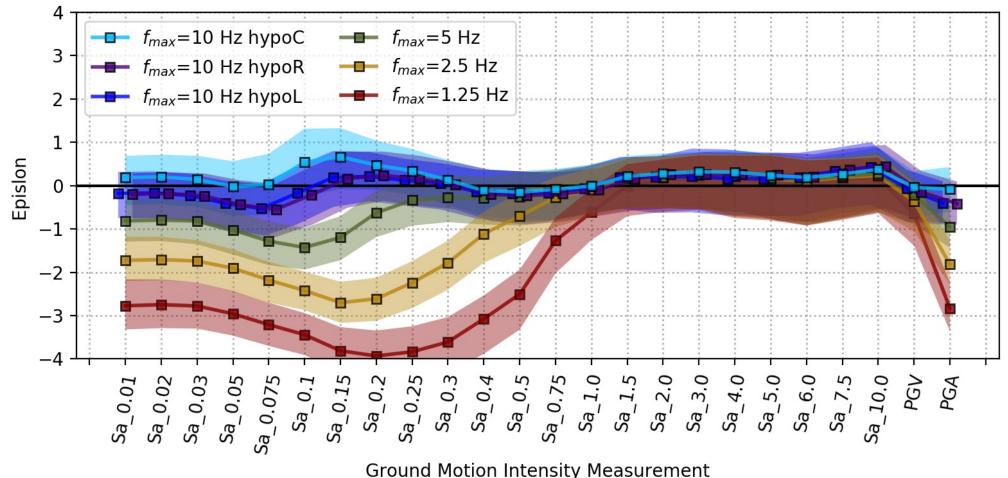
Variations $\sigma_{1D} < \sigma_{3DFLAT} < \sigma_{3DTOPO} < \sigma_{GMM}$

Rodgers et al. (GRL, 2018)



Epsilon for all sites, 3D model, f_{max} = 1.25 - 10 Hz

Colored bands show 50% of data, interquartile range

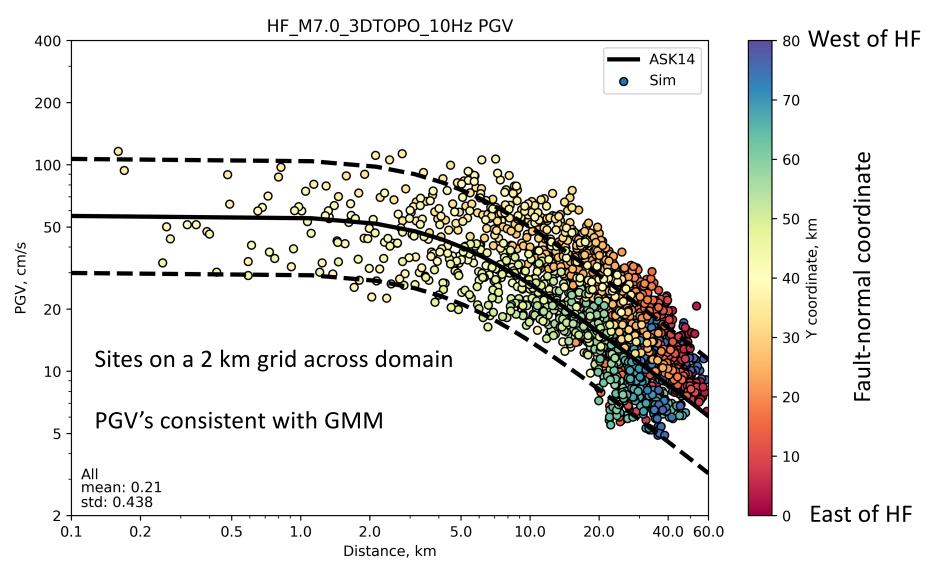






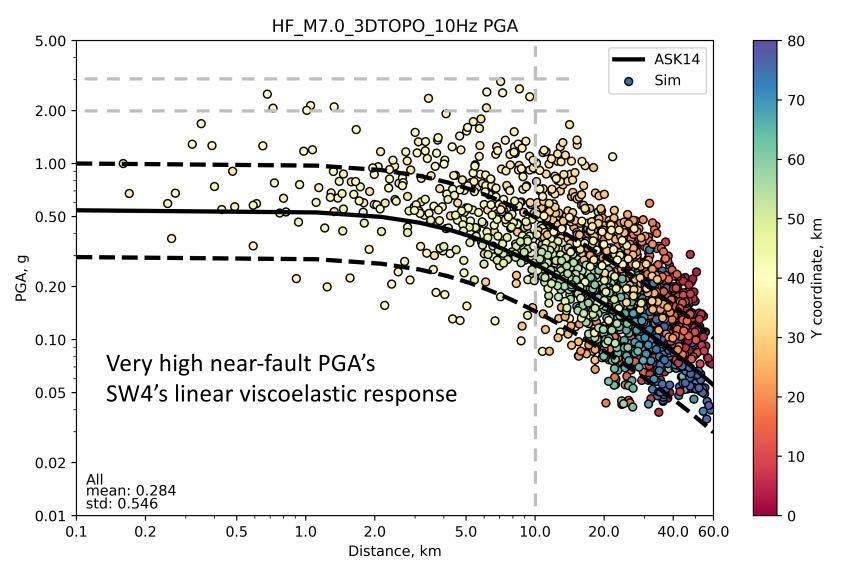
SW4 (viscoelastic) PGV versus distance compared with ASK (2014) GMM

 $HF M_w 7.0 10.0 Hz - PGV$



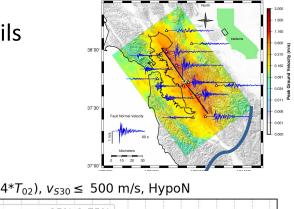
SW4 (viscoelastic) PGA versus distance compared with ASK (2014) GMM

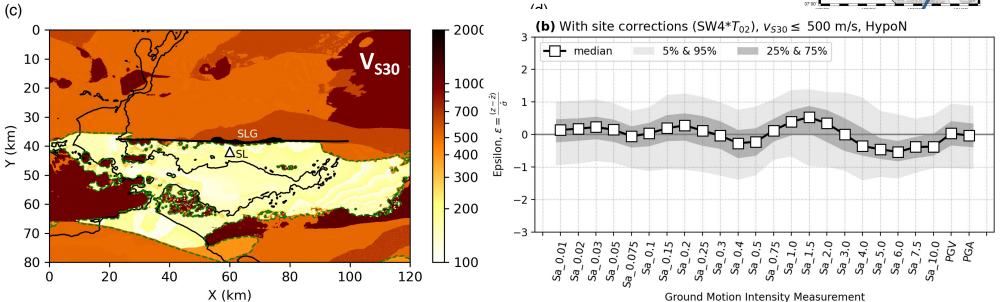
HF M_w 7.0 10.0 Hz - PGA



High PGA values indicate shortcomings in our simulations: linear viscoelasticity & assumed v_{Smin}

- Assumed v_{Smin} = 500 m/s does not honor weak near-surface soils
- These can respond with competing effects:
 - Amplify long-period weak motion
 - Dampen short-period strong motion



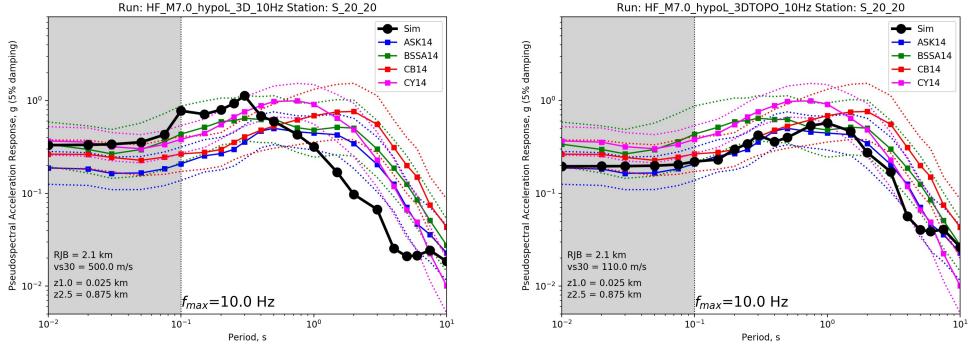


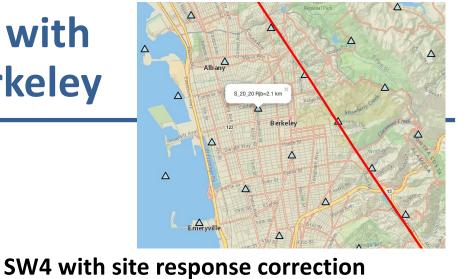
Site correction method reduces bias At low V_{S30} sites Rodgers et al. (BSSA 2020)



Ground motions without and with site response corrections: Berkeley

SW4 output, linear $v_{Smin} = 500 \text{ m/s}$ $v_{S30} = 500 \text{ m/s}$





v_{s30} = 110 m/s



Conclusions

- Verification must be an essential and ongoing task for seismic simulation codes undergoing continuous development
- Validation is needed for both source and 3D Earth structure models
- Validation of path propagation in 3D Earth models with moderate events is important
 - We must learn as much as possible from smaller events
 - Basin effects, crustal structure, waveform tomography
 - We are awaiting update of the SFBA model from USGS (Hirakawa, Aagaard)
- Validation of large event ruptures is more complex due to:
 - Lack available empirical data
 - Dependence of intensities on source, path and site effects
 - Simulated data may be consistent with GMM's, but is the Earth model correct?
 - Additional criteria must be considered such as
 - Median epsilon
 - Within-event and between-event variability
 - Spectra correlation
 - Duration
 - Building response, engineering demand



Recommendations for community-based V&V

- Encourage FAIR (Findable, Accessible, Interoperable & Reusable) best-practices
 - Version control on data sets, synthetics and 3D models
- Standardization of waveform and event parameter data used in simulations for validation
 - Assembly with Python, ObsPy, Jupyter notebooks
 - Storage as ASDF (single HDF5 file per event)
- Standardization of simulated event data and metadata
 - Simulation metadata, e.g. input file(s) so others can reproduce
 - Storage as ASDF (single file per event)
 - Source and site parameters used in GMM's
- Standardize metrics for comparison
 - Waveform and intensity measurements

https://seismic-data.org/







iupvte

pyasdf

