# DRAFT

# New Ground Motion Selection Procedures and Selected Motions for the PEER Transportation Research Program

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# ABSTRACT

The primary goal of this project was to develop strategies for selecting standardized sets of ground motions for use by the PEER Transportation Research Program. The broad research activities of the Transportation Research Program require ground motions for use in a variety of applications, including analysis of structural and geotechnical systems at locations throughout California (or other active areas where seismic hazard is dominated by mid- to large-magnitude crustal earthquakes at near to moderate distances). The systems of interest may be sensitive to excitation at a wide range of periods, and some sites of interest may have the potential to experience near-fault directivity pulses. A unique aspect of this project is that these are not structure-specific and site-specific goals, so many ground motion selection techniques developed in previous research efforts are not directly applicable here.

This report summarizes the approaches that were developed to meet these goals and describes the properties of the ground motion sets that were selected. To develop some of the ground motion sets, a new selection algorithm is proposed that allows the user to select a set of ground motions whose response spectra match a target mean and variance; this new algorithm is also described. The project thus provides several useful sets of standardized ground motions, as well as a new approach to select alternate sets to meet user-specific needs.

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# **1 STUDY OVERVIEW**

# **1.1 INTRODUCTION**

Efforts in recent decades to understand the properties of earthquake ground motions that affect geotechnical and structural systems have led to insights for structure-specific ground motion selection in performance-based earthquake engineering. Current practice selects ground motions whose intensity (measured by an Intensity Measure or IM) is exceeded with some specified probability at a given site, and whose other properties are also appropriate (as typically determined by probabilistic seismic hazard and deaggregation calculations). See, for example, (Krawinkler et al. 2003; Stewart et al. 2002; Mavroeidis et al. 2004; Kramer and Mitchell 2006; Kennedy et al. 1984; Bazzurro et al. 1998; Baker and Cornell 2006; Haselton et al. 2009) among many others for progress and recommendations on structure-specific ground motion selection.

Research on this topic has been focused primarily on cases where the structure and location of interest is known (so that ground motions can be selected and modified with specific structural properties and seismic hazard information in mind). The PEER Transportation Research Program (*peer.berkeley.edu/transportation/*), in contrast, is studying a wide variety of structural and geotechnical systems at a wide range of locations, and would benefit from having a standardized set of ground motions to facilitate comparative evaluations in this research. Even in situations where a specific location might be of interest, the Transportation Research Program is sometimes evaluating alternative structural systems (with differing periods of vibration) for potential use at a given location, so ground motion selection techniques that depend upon knowledge of structural periods are not applicable. Other techniques are thus needed to choose 'appropriate' ground motion sets for this Research Program. This document describes the process that was used to select three standardized ground motion sets for PEER and documents the properties of the selected ground motions. Because the ground motions are not structure-specific or site-specific, it may be useful for the user to pre-process these ground motions prior to

using them for structural analysis (e.g., by scaling the motions) or to post-process the structural analysis results (e.g., by using regression analysis to identify trends in structural response as a function of ground motion intensity parameters). The selected ground motions described in this report, and some additional descriptive data for these motions, are available electronically at *www.stanford.edu/~bakerjw/PEER\_gms.html*.

# **1.2 OBJECTIVES**

The goal of this project is to select several standardized sets of ground motions that can be used in the PEER Transportation Research Program, for use in analyzing a variety of structural and geotechnical systems that would potentially be located in active seismic regions such as California. Because of the wide variety of uses for these ground motions, it is not feasible to use the site-specific/structure-specific ground motion selection methods most frequently proposed in recent research, for reasons discussed above. Despite the generality of this objective, several decisions were made to constrain the scope of the ground motion selection:

- Although the sites of interest will vary, we are generally interested in high-seismicity sites that may experience strong ground motions from mid- to large-magnitude earthquakes at close distances.
- Some sites of interest may be located nearby active faults and have the potential to experience near-fault directivity.
- There are a variety of structures to be studied, some of which are also sensitive to excitation at a wide range of periods. This means that it is likely not useful to focus on a specific period or narrow range of periods when selecting ground motions.
- The primary period range of interest is between 0 and 3 seconds, with secondary interest in periods as long as 5 seconds.
- The users are willing and able to utilize a relatively large number of ground motions (i.e., dozens to hundreds) in order identify probability distributions and statistical trends in system responses.
- Three component ground motions are desired.

With these objectives and criteria in mind, four ground motion sets were selected and are described in Section 3 below.

Site and structure-specific ground-motion selection methods often involve selecting a set of ground motions whose response spectra match a site-specific target response spectrum. That approach will not be effective here, because no single target spectrum is available. Instead, we preferred to select ground motions with a variety of spectral shapes, in order to ensure that ground motions with a range of properties were available to analysts (and to capture ground motion aleatory variability in the case that the analyst is interested in response from the scenario earthquake); variability in ground motion durations and directivity pulse periods (when applicable) is also present in the selected ground motions. This ensures that research into the effect of spectral shape and directivity pulse properties on structural response (e.g., Baker and Cornell 2006; Rodriguez-Marek and Bray 2006) is possible using these ground motions. To achieve this goal, ground motions have been selected such that the mean and variance of their logarithmic response spectra match that predicted for a 'generic earthquake scenario' typical of high-seismicity sites in California. This type of approach requires the selection of ground motions with specified variability in their response spectra and other parameters. No algorithm was available to easily incorporate such variability, so a new algorithm was devised and is described in Section 2.

# **1.3 GROUND MOTION LIBRARY**

All ground motions and associated metadata were obtained from the PEER NGA Project ground motion library (Chiou et al. 2008). This library, available online at *http://peer.berkeley.edu/nga* contains 3551 multi-component ground motions from 173 earthquakes. The earthquakes, ranging in magnitudes from 4.3 to 7.9, are primarily from shallow crustal earthquakes observed in seismically active regions of the world. The NGA project made a significant effort to carefully process these ground motion recordings (including filtering, baseline correcting, and verification of metadata such as associated source-site-distances and near surface site conditions). For this project, the selected ground motions were rotated from their as-recorded orientations (the orientations provided by PEER) to strike-normal and strike-parallel orientations. The strike orientations used when performing this rotation come from the NGA Flatfile.

### 1.4 DOCUMENTATION OF SELECTED GROUND MOTIONS

The following sections of report summarize the procedures used to select ground motions and provide some summary data of the selected motions. The most detailed documentation of these motions, however, comes from the ground motion time histories themselves, as well as metadata such as their magnitudes, distances, and response spectra. A brief summary of the ground motion properties is provided in the appendix, which provides a few metadata fields for each selected ground motion. A more complete set of information is available from the project website (http://peer.berkeley.edu/transportation/publications data.html), including complete time histories, response spectra for all three components of each ground motion, etc. The appendix tables and project website also list an 'NGA Record Sequence Number' for each ground motion, which matches a corresponding field in the much more complete NGA Flatfile (http://peer.berkeley.edu/nga/documentation.html). Additional information not in the current NGA Flatfile, such as directivity pulse periods, scale factors (if applicable), and  $\varepsilon$  values, are included in the appendix tables or in spreadsheets posted at the project website.

# 2 A COMPUTATIONALLY EFFICIENT GROUND-MOTION SELECTION ALGORITHM FOR MATCHING A TARGET RESPONSE SPECTRUM MEAN AND VARIANCE

*Note: this section is adapted from the following publication, with slightly modified text in some sections to more directly address the specific ground motion selection results presented below.* 

Jayaram, N., Lin, T., and Baker, J. W. (2011). "A computationally efficient groundmotion selection algorithm for matching a target response spectrum mean and variance." *Earthquake Spectra*, in press.

# 2.1 Introduction

The 'broadband' ground motion sets discussed in Section 3 below were selected so that their response spectra (more precisely, their log response spectra) match a target mean and variance. When this objective was chosen, no practical algorithm was available to perform such a procedure, and so one was developed to facilitate this task. This section presents a brief description of the new ground motion selection algorithm. This new selection algorithm probabilistically generates multiple response spectra from a target distribution, and then selects recorded ground motions whose response spectra individually match the simulated response spectra. A greedy optimization technique further improves the match between the target and the sample means and variances. The proposed algorithm is used to select ground motion variance on the structural response estimates. The implications for code-based design and performance-based earthquake engineering are discussed.

The unique feature of this new approach is that it is able to produce a set of ground motions matching both a target mean and target variance of a log response spectrum, as opposed to most methods which match only a mean spectrum (e.g., Beyer and Bommer 2007; Shantz 2006; Watson-Lamprey and Abrahamson 2006). A notable exception is the algorithm of Kottke and Rathje (2008), but the technique developed here is more suitable to the current task because it works easily with the large ground motion catalog considered here, does not require ground

motion scaling, and also reproduces desired correlations among response spectral values at pairs of periods.

Selecting a set of ground motions to match only a target mean response spectrum is computationally inexpensive, since it can be done by choosing time histories whose response spectra individually deviate the least from the target response spectrum. The deviation can be measured using the sum of squared differences between the response spectrum of the record and the target response spectrum (e.g., AMEC Geomatrix Inc. 2009; Youngs et al. 2006).

When matching a target mean and a target variance, however, it does not suffice to treat ground motions individually, but rather requires comparisons of the mean and variance of *sets* of ground motions to the target values. That is, the suitability of a particular ground motion can only be determined in the context of the complete ground-motion set in which it might be included. There are generally an intractably large number of possible ground-motion sets, and so identifying the best set is a computationally-expensive combinatorial optimization problem (Naeim et al. 2004). No automated procedures are available in the literature, however, to select ground motions that match the response spectrum mean and variance. One notable work in this regard is that of Kottke and Rathje (2008), who proposed a semi-automated procedure that first selects ground motions based on matching the mean spectrum, and subsequently applies individual scale factors on the ground motions to achieve the target variance. This technique, however, does not easily scale to work with large ground-motion datasets, and also cannot be used for the selection of unscaled ground motions.

Besides the broadband selection cases discussed in Section 3, another important case where response spectrum variance may be important is, the conditional mean spectrum (CMS), which is derived by conditioning on spectral acceleration at only a single period,  $S_a(T^*)$ , so the response spectra at other periods have variance (Baker 2011). To demonstrate the generality of this new algorithm and its relevance to cases beyond the broadband selection of Section 3, this section includes example results where the proposed algorithm is used to select ground motions matching a CMS for the purpose of estimating the seismic response of sample single-degree-offreedom (SDOF) and multiple-degree-of-freedom (MDOF) structures<sup>1</sup>. The results are used to demonstrate the algorithm, and also to assess the impact of considering ground-motion variance

<sup>&</sup>lt;sup>1</sup> A description of this algorithm that selects the "Set #1A" ground motions described below as the example application is provided in Jayaram and Baker (2010).

on the structural response estimates. The implications for code-based design and performancebased earthquake engineering are discussed.

#### 2.2 Ground-motion selection algorithm

The objective of the proposed algorithm is to select a suite of ground motions whose response spectra have a specified mean and variance. This algorithm is based on the empirically verified observation that the set of logarithmic spectral accelerations  $(\ln S_a)$  at various periods is a random vector that follows a multivariate normal distribution (Jayaram and Baker 2008). The first step in this algorithm is to parameterize the multivariate normal distribution of  $\ln S_a$ 's at multiple periods. The parameters of the multivariate normal distribution are the means and the variances of the  $\ln S_a$ 's at all periods and the correlations between the  $\ln S_a$ 's at all pairs of periods. Equivalently, the distribution can be parameterized using the means of the  $\ln S_a$ 's and the covariances between the  $\ln S_a$ 's at all pairs of periods. In order to achieve the desired properties in the selected ground motions, these parameters should be set to their target values (i.e., target means and variances for the ground motions to be selected). A subsequent section illustrates this parameterization.

Once the distribution means and covariances are set equal to the desired target values, Monte Carlo simulation is used to probabilistically generate response spectra from the above mentioned multivariate normal distribution. This can be performed using a standard function in many programming languages. The number of response spectra to be simulated equals the desired number of ground motions. For each simulated response spectrum, a ground motion with a similar response spectrum is then selected. The similarity between a ground-motion response spectrum and a Monte Carlo simulated response spectrum is evaluated using the sum of squared errors (*SSE*) described below:

$$SSE = \sum_{j=1}^{P} \left( \ln S_a(T_j) - \ln S_a^{(s)}(T_j) \right)^2$$
(1)

where  $\ln S_a(T_j)$  is the logarithmic spectral acceleration of the (optionally scaled) ground motion in consideration at period  $T_j$ ,  $\ln S_a^{(s)}(T_j)$  is the target  $\ln S_a$  at period  $T_j$  from the simulated response spectrum, p is the number of periods considered and *SSE* is the sum of squared errors, which is a measure of dissimilarity. The measure of similarity defined by Equation 1 is not unique, and discussion of other measures of similarity can be found in Beyer and Bommer (2007) and Buratti et al. (2011). The selection is done by computing *SSE* for each ground motion in the database, and then choosing the ground motion having the smallest *SSE*. Other ground motion properties can be accounted for at this stage by, for example, considering only ground motions falling within a specified range of magnitudes and distances. Note that this is identical to comparison procedures in use today, except that here we are comparing to simulated spectra rather than a target mean spectrum.

The mean and the variance of the simulated response spectra will approximately match the corresponding target values because they were sampled from the desired distribution. This match will be nearly exact if a large number of spectra are simulated and will be approximate otherwise. Since the simulated response spectra have approximately the desired mean and variance, the response spectra selected using this approach will also have approximately the desired mean and variance. Additionally, this ground-motion selection approach also ensures that the selected set has the target correlation structure (i.e., correlation between  $\ln S_a$ 's at pairs of periods) specified while parameterizing the distribution of the response spectrum. This implies that, in the particular case where the logarithmic response spectrum follows a multivariate normal distribution, the proposed algorithm actually matches the entire response spectrum distribution. Another advantage of this approach is that this algorithm allows the selection of unscaled ground motions (Jayaram and Baker 2010).

As mentioned above, when ground motions are selected using the approach described above, the sample means and variances may deviate slightly from the target values, particularly when the number of ground motions selected is small. Therefore, a 'greedy' optimization technique is used to further improve the match between the sample and the target means and variances. In this approach, each ground motion selected previously is replaced one at a time with a ground motion from the database that causes the best improvement in the match between the target and the sample means and variances. If none of the potential replacements causes an improvement, the original ground motion is retained. The mismatch is estimated as the sum of squared differences between the target and the sample means and variance from the target mean and variance (denoted  $SSE_s$ ) is estimated as follows:

$$SSE_{s} = \sum_{j=1}^{p} \left[ \left( \hat{m}_{\ln S_{a}(T_{j})} - \mu_{\ln S_{a}(T_{j})}^{(t)} \right)^{2} + w \left( \hat{s}_{\ln S_{a}(T_{j})} - \sigma_{\ln S_{a}(T_{j})}^{(t)} \right)^{2} \right]$$
(2)

where  $SSE_s$  is the sum of squared errors of the set, which is the parameter to be minimized,  $\hat{m}_{\ln S_a(T_j)}$  is the set mean  $\ln S_a$  at period  $T_j$ ,  $\mu_{\ln S_a(T_j)}^{(t)}$  is the target mean  $\ln S_a$  at period  $T_j$ ,  $\hat{s}_{\ln S_a(T_j)}$  is the set standard deviation of the  $\ln S_a$  at period  $T_j$ ,  $\sigma_{\ln S_a(T_j)}^{(t)}$  is the target standard deviation of the  $\ln S_a$  at period  $T_j$ , w is a weighting factor indicating the relative importance of the errors in the standard deviation and the mean (A possible value for w is 1, but it can be chosen depending on the desired accuracy in the match between the sample and the target means and standard deviations), and p is the number of periods  $(T_j)$  at which the error is computed.

The set mean and standard deviation can be calculated as follows:

$$\hat{m}_{\ln S_a(T_j)} = \frac{1}{n} \sum_{i=1}^n \ln S_{a_i}(T_j)$$
(3)

$$\hat{S}_{\ln S_a(T_j)} = \sqrt{\frac{1}{n-1} \sum_{i=1}^n \left( \ln S_{a_i}(T_j) - \hat{m}_{\ln S_a(T_j)} \right)^2}$$
(4)

where  $\ln S_{a_i}(T_j)$  denotes the  $\ln S_a$  of the *i*<sup>th</sup> record in the set at period  $T_j$ , and *n* denotes the number of records in the set.

Note that the greedy optimization technique does not explicitly account for the correlation structure of selected sets. This correction structure is captured in the initial selection step, and is approximately retained after the greedy optimization as well.

The steps involved in the greedy optimization technique are summarized below.

- Step 1: Set j = 1.
- Step 2: Set i = 1. Denote the  $SSE_s$  of the set as  $SSE_{s,old}$
- Step 3: If the *i*th database ground motion (*G<sub>i</sub>*) is not already present in the set, replace the *j*th ground motion in the set with *G<sub>i</sub>*. Compute *SSE<sub>s,i</sub>* (i.e., the *SSE<sub>s</sub>* of the set after the replacement is carried out).
- Step 4: Reverse the replacement carried out in Step 3. Increment *i* by 1.
- Step 5: If *i* is less than or equal to the size of the ground-motion database, go to Step 3. Otherwise, identify the ground motion *i* that results in the minimum value of SSE<sub>s,i</sub>. If SSE<sub>s,i</sub> < SSE<sub>s,old</sub>, replace the *j*th ground motion in the set with the *i* th ground motion in the database.

• Step 6: Increment *j* by 1. If *j* is less than the size of the set, go to Step 2. Otherwise, terminate the algorithm.

This is called a 'greedy' optimization technique because it maximizes the improvement in match between the target and sample at each iteration, without necessarily achieving a global optimum solution. In this application, the initial simulation and selection steps result in a ground motion set that is already approximately optimal (for reasonably large sets), so it has been observed that only this greedy technique is needed to find solutions that are essentially globally optimal. Observational experience suggests that this algorithm never produces sets of ground motions with poor matches between the sample and the target means and variances (even for sets with as few as 10 ground motions, as illustrated in a subsequent section).

Appendix 'An Alternate Ground-Motion Selection Algorithm' describes an alternate selection algorithm that does not require knowledge of the response spectrum distribution or the correlation structure.

# 2.3 Illustrative ground-motion selection

This section describes the application of the proposed algorithm for selecting structure-specific ground motions that have a specified spectral acceleration at the structure's fundamental period. In this example, the target response spectrum mean and covariance matrices are obtained using the conditional mean spectrum (CMS) method (Baker 2011), which provides the mean and variance (and correlations) of the response spectrum conditioned on the specified spectral acceleration. It is to be noted that while this example uses the targets from the CMS method, the proposed algorithm can be used with any arbitrary target mean and covariance (e.g., Jayaram and Baker 2010).

#### **2.3.1** Parameterization of the target response spectrum distribution

As described in the previous section, the first step in the algorithm is to parameterize the multivariate normal distribution of the  $\ln S_a$ 's using the means and the variances of the spectral accelerations (chosen to equal the target mean and the target variance respectively) and the correlations between the spectral accelerations at two different periods. The steps involved in parameterizing the distribution using the CMS method are listed below.

• Step 1: Determine the target spectral acceleration (Sa) at a given period  $T^*$  (e.g., the fundamental period of the structure), and the associated magnitude (*M*), distance to source (*R*) and  $\varepsilon(T^*)$ , where  $\varepsilon(T^*)$  is the number of standard deviations by which a given  $\ln Sa$  differs from the mean predicted (by a ground-motion model)  $\ln Sa$  at the period of interest  $T^*$ . In general,

$$\varepsilon(T) = \frac{\ln S_a(T) - \mu_{\ln S_a(T)}}{\sigma_{\ln S_a(T)}}$$
(5)

where  $\ln S_a(T)$  is the ground motion's logarithmic spectral acceleration at period *T*, and  $\mu_{\ln S_a(T)}$  and  $\sigma_{\ln S_a(T)}$  are the predicted mean and standard deviation, respectively, of  $\ln S_a(T)$  given *M*, *R*, etc. (e.g., Campbell and Bozorgnia, 2008). The values of *M*, *R* and  $\varepsilon(T^*)$ , can be obtained from deaggregation (e.g., USGS, 2008).

- Step 2: For all T<sub>j</sub> of interest, compute the unconditional mean and the unconditional standard deviation of the response spectrum, given M and R. In other words, compute μ<sub>lnS<sub>a</sub>(T)</sub> and σ<sub>lnS<sub>a</sub>(T)</sub>.
- Step 3: Compute the mean of  $(\ln S_a(T_1), \ln S_a(T_2), ..., \ln S_a(T_n))$  conditioned on  $\varepsilon(T^*)$ . This mean matrix (denoted  $\mu$ ) is computed as follows:

$$\boldsymbol{\mu} = \begin{bmatrix} \mu_{\ln S_{a}(T_{1})} + \rho(T_{1}, T^{*}) \varepsilon(T^{*}) \sigma_{\ln S_{a}(T_{1})} \\ \mu_{\ln S_{a}(T_{2})} + \rho(T_{2}, T^{*}) \varepsilon(T^{*}) \sigma_{\ln S_{a}(T_{2})} \\ \vdots \\ \mu_{\ln S_{a}(T_{n})} + \rho(T_{n}, T^{*}) \varepsilon(T^{*}) \sigma_{\ln S_{a}(T_{n})} \end{bmatrix}$$
(6)

where  $\rho(T_j, T^*)$  is the correlation between  $\varepsilon(T_j)$  and  $\varepsilon(T^*)$  provided by, for instance, Baker and Jayaram (2008).

 Step 4: Compute the covariance of (ln S<sub>a</sub>(T<sub>1</sub>), ln S<sub>a</sub>(T<sub>2</sub>), ..., ln S<sub>a</sub>(T<sub>n</sub>)) conditioned on ε(T<sup>\*</sup>). This covariance matrix (denoted Σ) is estimated as follows: Let Σ<sub>0</sub> denote the (unconditional) covariance matrix of the vector

 $(\ln S_a(T_1), \ln S_a(T_2), ..., \ln S_a(T_n)).$ 

$$\boldsymbol{\Sigma}_{0} = \begin{bmatrix} \sigma_{\ln S_{a}(T_{1})}^{2} & \rho(T_{1}, T_{2})\sigma_{\ln S_{a}(T_{1})}\sigma_{\ln S_{a}(T_{2})} & \cdots & \rho(T_{1}, T_{n})\sigma_{\ln S_{a}(T_{1})}\sigma_{\ln S_{a}(T_{n})} \\ \rho(T_{2}, T_{1})\sigma_{\ln S_{a}(T_{2})}\sigma_{\ln S_{a}(T_{1})} & \sigma_{\ln S_{a}(T_{2})}^{2} & \cdots & \rho(T_{2}, T_{n})\sigma_{\ln S_{a}(T_{2})}\sigma_{\ln S_{a}(T_{n})} \\ \vdots & \vdots & \ddots & \ddots & \vdots \\ \rho(T_{n}, T_{1})\sigma_{\ln S_{a}(T_{n})}\sigma_{\ln S_{a}(T_{1})} & \rho(T_{n}, T_{2})\sigma_{\ln S_{a}(T_{n})}\sigma_{\ln S_{a}(T_{2})} & \cdots & \sigma_{\ln S_{a}(T_{n})}^{2} \end{bmatrix}$$
(7)

Let  $\Sigma_1$  denote the covariance between  $(\ln S_a(T_1), \ln S_a(T_2), ..., \ln S_a(T_n))$  and  $\ln S_a(T^*)$ , defined as follows:

$$\boldsymbol{\Sigma}_{1} = \begin{bmatrix} \rho(T_{1}, T^{*}) \sigma_{\ln S_{a}(T_{1})} \sigma_{\ln S_{a}(T^{*})} \\ \rho(T_{2}, T^{*}) \sigma_{\ln S_{a}(T_{2})} \sigma_{\ln S_{a}(T^{*})} \\ \vdots \\ \rho(T_{n}, T^{*}) \sigma_{\ln S_{a}(T_{n})} \sigma_{\ln S_{a}(T^{*})} \end{bmatrix}$$
(8)

The covariance matrix of  $(\ln S_a(T_1), \ln S_a(T_2), ..., \ln S_a(T_n))$  conditioned on  $\ln S_a(T^*)$  can be computed as follows (e.g., Johnson and Wichern, 2007):

$$\boldsymbol{\Sigma} = \boldsymbol{\Sigma}_{0} - \frac{1}{\sigma_{\ln S_{a}(T^{*})}^{2}} \boldsymbol{\Sigma}_{1} \boldsymbol{\Sigma}_{1}^{'}$$
(9)

where  $\Sigma'_1$  denotes the transpose of  $\Sigma_1$ . The conditional standard deviation of the  $\ln S_a$ 's is the square root of the diagonals of  $\Sigma$ , also given by Equation 10.

$$\sigma_{\ln S_a(T) \mid \ln S_a(T^*)} = \sigma_{\ln S_a(T)} \sqrt{1 - \rho (T, T^*)^2}$$
(10)

Figure 1 shows the target conditional response spectrum mean and standard deviation obtained corresponding to magnitude = 7, distance to the rupture = 10km,  $T^* = 2.63$ s and  $\varepsilon(T^*) = 2.0$ . These values have been chosen to be compatible with ground-motion studies carried out by Haselton et al. (2009). The unconditional  $\ln S_a$  means and standard deviations corresponding to this scenario,  $\mu_{\ln S_a(T_j)}$  and  $\sigma_{\ln S_a(T_j)}$ , are obtained from the Campbell and Bozorgnia (2008) ground-motion model. (Since  $\ln S_a$ 's at multiple periods follow a multivariate normal distribution, the exponential of the mean  $\ln S_a$  equals the median spectral acceleration. This is why the axis of Figure 1 is labeled as 'Median  $S_a$ '.)



Figure 1: (a) Response spectrum mean. (b) Response spectrum standard deviation.

## 2.3.2 **Response spectrum simulation**

Forty response spectra are simulated (using Monte Carlo simulation) by sampling from a multivariate normal distribution with the mean and covariance matrices defined by Equations 6 and 9 for the target scenario described above. The response spectra are simulated at 20 periods logarithmically spaced between 0.05s and 10.0s, and are shown in Figure 2a. A large period range is used to ensure a good match in the entire response spectrum that covers regions of higher modes and nonlinearity. Because individual spectra may vary while still achieving a target mean and variance of the overall set, there is often little penalty in considering a broad period range in this step.



Figure 2: (a) Simulated response spectra (b) Response spectra of ground motions selected before greedy optimization (c) Response spectra of ground motions selected after greedy optimization.

Figure 1a compares the mean of the Monte Carlo simulated response spectra to the target mean. It can be seen that the mean values agree reasonably well. Figure 1b shows a reasonable agreement between the standard deviation of the simulated  $\ln S_a$  values and the target standard deviation. The small deviation seen in these figures is because the sample mean and standard deviation for moderately small sample sizes do not necessarily match the target mean and standard deviation.

#### 2.3.3 Selection of ground motions to match simulated spectra

Forty ground motions are selected from the Next Generation Attenuation (NGA) database (Chiou et al., 2008) that individually match the forty response spectra simulated in the previous step. For

two-dimensional structural models, a single ground motion component is required as an input for every time history analysis. (For three-dimensional structural models, two ground motion components can be selected by considering their geometric mean response spectrum, as described in Jayaram and Baker 2010.) Here, each horizontal component of a recording from the same station in the NGA database is treated separately as an individual ground motion. No constraints on, for example, the magnitudes and distances of the selected recordings are used, but such constraints are easily accommodated by simply restricting the set of ground motions considered for selection. Prior to selection, each of the available 7102 ground motions in the NGA database is scaled so that its  $S_a(T^*)$  matches the target  $S_a(T^*)$  from the target mean spectrum (seen in Figure 1a) when  $T^*$  is equal to 2.63s. Figure 2b shows the response spectra of the selected ground motions. The sample and the target means and standard deviations are shown in Figure 1. The figure shows that the sample and the target response spectrum mean and variance match reasonably well. Additionally, the selected ground motion spectra also match the specified target correlation structure (specified by the non-diagonal terms of the covariance matrix in Equation 9) reasonably well, as indicated by a mean absolute error between the sample and the target correlations of 0.12.

The computational time required for selecting the set of 40 ground motions is 10 seconds using a MATLAB implementation on an 8GB RAM 2.33GHz quad core processor. This computational efficiency allows for the algorithm to be optionally applied multiple times if one wants several candidate sets to choose from. While selecting the ground motions shown in Figure 2, we applied the algorithm multiple times (twenty times, in particular) to obtain multiple candidate ground-motion sets and chose the set with the minimum value of *SSE*. This approach is also beneficial to work around situations where recorded ground motion spectra that adequately match one or more of the simulated spectra are not available.

# 2.3.4 Greedy optimization technique

The greedy optimization technique is used to modify the ground-motion suite selected in the previous step. The spectra of the selected ground motions are shown in Figure 2c. The means and the standard deviations of the set are shown in Figure 1, and have a near perfect match with the target means and standard deviations. The mean absolute error between the sample and the target correlations is 0.15.

In total, the computational time required to select the set of 40 ground motions from the 7102 available ground motions is about 180 seconds using a MATLAB implementation on an 8GB RAM 2.33GHz quad core processor. A MATLAB implementation of the proposed ground-motion selection algorithm can be downloaded from *http://www.stanford.edu/~bakerjw/gm\_selection.html*.

## 2.3.5 Selection of a smaller number of ground motions

To test the effectiveness of the algorithm in sampling smaller ground motion sets, it is repeated to select a set of 10 ground motions for the scenario described earlier (magnitude = 7, distance to rupture = 10km,  $T^* = 2.63$ s and  $\varepsilon(T^*) = 2$ ). The response spectra of the selected records are shown in Figure 3a. The set means and standard deviations are compared to the target means and standard deviations in Figure 3b-c. It can be seen that the matches are good, illustrating the effectiveness of the algorithm in selecting small sets of ground motions. The mean absolute error between the sample and the target correlations is 0.17. The computational time required to select the set of 10 ground motions is about 25 seconds using a MATLAB implementation on an 8GB RAM 2.33GHz quad core processor. The computational time required for selecting the set of 10 ground motions without using the greedy optimization technique is 4 seconds.



Figure 3: (a) Response spectra of 10 selected ground motions (b) Response spectrum mean (c) Response spectrum standard deviation.

# 2.4 Impact of matching spectrum variance on structural response

Code-based structural design and performance-based earthquake engineering applications require statistics such as the mean (e.g., American Society of Civil Engineers 2005) or the median and the dispersion (e.g., Applied Technology Council 2009a) of the structural response. It is of interest in this section to evaluate the impact of ground-motion selection considering a target response spectrum mean and variance (as compared to considering only a target mean) on these statistics.

#### 2.4.1 Ground-motion selection

The ground motions used for evaluating structural response are selected using the method described in the previous section for a target scenario with magnitude = 7, distance to rupture = 10 km,  $V_{s30} = 400 \text{m/s}$ , and a strike-slip mechanism. The Campbell and Bozorgnia (2008) ground-motion model is used to estimate the mean and variance of the response spectrum. The values of  $\varepsilon$  and period  $T^*$  are varied to obtain multiple test scenarios. Three typical  $\varepsilon$  values of 0, 1 and 2 are considered. The structures considered in this work have periods ( $T^*$ ) ranging between 0.5s and 2.63s.

In order to investigate the impact of matching response spectrum variance (Equation 9) on the structural response statistics, sets of forty ground motions are selected using two methods: 'Method 1' in which only the target mean is matched (a common approach in current practice, e.g., Baker and Cornell, 2006 and Method 300 in Haselton et al. 2009) and 'Method 2' in which both the target mean and the target variance are matched using the approach proposed here. The target response spectrum mean and covariance matrices are evaluated using Equations 6 and 9 for each combination of  $\varepsilon$  and  $T^*$ . Figure 4 shows example response spectra of ground motions selected using these two methods (for  $\varepsilon = 2$  and  $T^* = 2.63$ s).



Figure 4: Response spectra of 40 selected ground motions for  $\varepsilon = 2$  and  $T^* = 2.63$ s (a) Using Method 1: Match target response spectrum mean, and (b) Using Method 2: Match target response spectrum mean and variance.

#### 2.4.2 Structural response

This section describes the response of sample nonlinear single-degree-of-freedom (SDOF) structures and multiple-degree-of-freedom (MDOF) buildings designed according to modern building codes. In this work, we consider only maximum displacement for the SDOF structures and maximum interstory drift ratio (*MIDR*) for the MDOF structures.

## 2.4.2.1 Description of structural systems

The SDOF structures considered in this work follow a non-deteriorating, bilinear forcedisplacement relationship (Chopra 2001). They have  $T^* = 0.5$ s, 5% damping and post-yielding stiffness equal to 10% of elastic stiffness. SDOF structures with 'R factors' (the ratio of the target spectral acceleration at the period of the structure,  $S_a(T^*)$ , to the yield spectral acceleration =  $\omega^2$  \* yield displacement, where  $\omega$  is the structure's fundamental circular frequency) of 1, 4 and 8 are considered to study varying levels of non-linear behavior. The R factor is controlled by varying the yield displacements of the SDOF structures relative to the  $S_a(T^*)$  value obtained from the target spectrum. The SDOF structures are non-deteriorating systems, so structural collapse is not considered.

The MDOF structures used in this study were designed per modern building codes and modeled utilizing the Open System for Earthquake Engineering Simulation (OpenSEES) (McKenna et al. 2007) by Haselton and Deierlein (2007). The structural models consider strength and stiffness deterioration (Ibarra et al. 2005) unlike in the SDOF case. The designs for these buildings have been checked by practicing engineers as part of the Applied Technology Council Project ATC-63 (2009b). They have also been used for previous extensive ground-motion studies (Haselton et al., 2009). The two buildings used in the current study are a 4-story reinforced concrete moment frame structure with  $T^* = 0.94$ s, and a 20-story reinforced concrete moment frame structure with  $T^* = 2.63$ s. The buildings show deterioration, and collapse is said to occur if dynamic instability (large increases in the drift for small increases in the ground-motion intensity) is reached in the model (Haselton and Deierlein 2007).

## 2.4.2.2 Response of SDOF systems

Table 1 shows the mean, median and dispersion (dispersion refers to logarithmic standard deviation) of ductility ratios (spectral displacement divided by the yield displacement) of the SDOF structures under the different ground-motion scenarios described earlier. The ductility statistics are estimated using the two sets of 40 ground motions selected using Method 1 (ground motions selected by matching only the target response spectrum mean) and Method 2 (ground motions selected by matching the target response spectrum mean and variance). It can be seen from Table 1 that the median ductilities are similar across the two ground-motion selection methods, while the mean and the dispersion of the response are higher in Method 2, when the ground-motion variance is considered. The higher dispersion of the response seen while using Method 1. As expected, the increase in dispersion is particularly significant at large R values when the structure behaves in a non-linear manner. Note that there are no differences between the methods when R = 1, because the response is dependent only on  $S_a(T^*)$ , which is identical in both cases.

	R	Median Ductility		Dispersion of Ductility		Mean Ductility	
3		Method 1	Method 2	Method 1	Method 2	Method 1	Method 2
	1	1.00	1.00	0	0	1.00	1.00
0	4	3.93	3.76	0.24	0.31	4.21	4.18
	8	10.76	9.97	0.28	0.42	10.82	10.74
	1	1.00	1.00	0	0	1.00	1.00
1	4	3.55	3.35	0.22	0.33	3.79	3.93
	8	8.04	8.16	0.28	0.46	8.57	9.46
	1	1.00	1.00	0	0	1.00	1.00
2	4	3.27	3.04	0.19	0.28	3.39	3.34
	8	6.90	7.44	0.24	0.41	7.34	7.98

Table 1:Ductility ratios of example SDOF structures.

Figure 5 shows the fraction of response analyses that result in a ductility less than a specified value for the SDOF structure with R = 8 in the  $\varepsilon = 1$  scenario, estimated using Methods 1 and 2. This type of plot is referred to as an empirical cumulative distribution function, or CDF. The CDFs intersect at a value of approximately 0.5 due to the similarity in the median response in both cases. The CDF obtained using Method 2 is flatter with heavier tails as a result of the larger dispersion observed in this case. As seen from Figure 5a, the upper tails of the CDFs are heavier than the lower tails. Since the mean response is the area above the CDF (the mean of a random variable is the area under the complementary CDF, which equals 1 - CDF), it can be visually observed that the difference in the heaviness of the upper tails results in a larger mean value of the response in case of Method 2 as compared to Method 1. This is a graphical evidence of the larger mean values reported earlier in Table 1. Analytically, if the responses were to follow a lognormal distribution (a common assumption in performance-based earthquake engineering), the properties of the lognormal distribution will imply that a larger dispersion results in a larger mean for a fixed median, which also explains the larger means observed in Method 2.



Figure 5: Distribution of the structural response of the SDOF structure corresponding to R = 8 and  $\epsilon(T^*) = 1$ : (a) Linear scale (b) Logarithmic scale.

# 2.4.2.3 Response of MDOF systems

Table 2 summarizes the maximum interstory drift ratio (*MIDR*) estimates for the MDOF structures considered in this study under various ground-motion scenarios, estimated using Methods 1 and 2. The distributions of responses are summarized using the probability of collapse (i.e., counted fraction of responses indicating collapse) and the median and the dispersion of the non-collapse responses.

Duilding	З	Median MIDR		Dispersion of MIDR		Collapse Probability	
Building		Method 1	Method 2	Method 1	Method 2	Method 1	Method 2
20-story	0	0.0044	0.0043	0.18	0.32	0	0
moment	1	0.0096	0.0086	0.24	0.29	0	0
frame	2	0.0186	0.0196	0.25	0.43	0	0.05
4-story	0	0.0072	0.0072	0.09	0.09	0	0
moment	1	0.0137	0.0139	0.26	0.29	0	0
frame	2	0.0279	0.0237	0.28	0.46	0.10	0.20

Table 2:Maximum interstory drift ratio (*MIDR*) of 20-story and 4-story moment<br/>frames.

From Table 2, it can be seen that, as observed in the SDOF case, the medians are similar across Methods 1 and 2 in all the considered scenarios. The dispersions are larger, however, when the ground-motion variance is considered in Method 2. The increase in the dispersion also results in an increased probability of observing large values of structural response. This can result in an increased probability of structural collapse while using Method 2, as evidenced, for example, when  $\varepsilon = 2$  in Table 2.

Figure 6 shows the empirical CDF of the *MIDR* of the 20-story frame corresponding to the  $\varepsilon = 2$  ground-motion scenario. As seen in the SDOF case, the CDF obtained using Method 2 is flatter and has heavier tails on account of larger dispersion. The maximum plotted values of the CDFs differ from one, and the difference equals the probability of collapse.



Figure 6: Distribution of the structural response of the 20 story moment frame building corresponding to  $\varepsilon(T^*) = 2$ : (a) Linear scale (b) Logarithmic scale.

In summary, the response estimates for the SDOF and the MDOF structures across several ground-motion scenarios show that the consideration of the response spectrum variance while selecting ground motions does not significantly impact the median structural response, but tends to increase the mean response and the dispersion in the response. The increased dispersion can result in more extreme responses, which can lead to a larger probability of structural collapse.

These example analysis cases serve to illustrate the potential importance of matching response spectrum variance. More detailed investigations regarding the impact are important, and will be carried out in the future.

## 2.5 Implications

Code-based design is often concerned with the average response of the structure (e.g., ASCE, 2005). The average response is typically interpreted as the mean response, although sometimes it

is interpreted as the median. If median structural response is of interest, the consideration of the response spectrum variance while selecting ground motions does not have a significant impact in the limited investigation performed here. On the other hand, if mean structural response is of interest, the consideration of the response spectrum variance appears to increase the mean structural response and may thus impact code-based design calculations.

Performance-based earthquake engineering (PBEE), in contrast, often requires knowledge about the full distribution of structural response (ATC-58, 2009). Matching target response spectrum variance increases the dispersion of structural response, thereby affecting the distribution of structural response and consequently the damage state and loss estimation computations in PBEE. The increase in the dispersion leads to higher and lower extremes of structural response and the associated damage states and losses. The increased dispersion can also lead to a larger probability of structural collapse. PBEE calculations will thus almost certainly be affected by this issue.

In summary, the example analyses presented above and engineering intuition suggest that the target response spectrum variance used when selecting ground motions has an impact on the distribution of structural responses obtained from resulting dynamic analysis. It appears that this is true for both code-based design checks and performance-based earthquake engineering analysis. Further study is needed to quantify the magnitude of these impacts, and this new algorithm will facilitate such studies.

## 2.6 Conclusions

A computationally efficient, theoretically consistent ground-motion selection algorithm was proposed to enable selection of a suite of ground motions whose response spectra have a target mean and a target variance. The algorithm first uses Monte Carlo simulation to probabilistically generate multiple realizations of response spectra from a target distribution, and then selects recorded ground motions whose response spectra individually match the simulated response spectra. A greedy optimization technique then further improves the match between the target and the sample means and variances by replacing one previously selected ground motion at a time with a record from the ground-motion database that causes the best improvement in the match. It was shown empirically that this algorithm selects ground motions whose response spectra have the target mean and variance.

The proposed algorithm was then used to select ground motions for estimating the seismic response of sample single-degree-of-freedom (SDOF) and multiple-degree-of-freedom (MDOF) structures, in order to assess the impact of considering response spectrum variance on the structural response estimates. SDOF structures with different levels of non-linearity (as indicated by their R factors) were analyzed using the selected ground motions. It was seen that considering the response spectrum variance does not significantly affect the resulting median response, but slightly increases the mean response and considerably increases the dispersion (logarithmic standard deviation) of the response. The increase in the mean and the dispersion is larger for more non-linear SDOF structures. Two code-compliant MDOF structures with heights of 4 and 20 stories were also analyzed using the selected ground motions. As with the SDOF structures, it was seen that considering the response spectrum variance does not significantly affect the median response but increases the dispersion of the response and the probability of observing collapse. These observations have implications for applications where the dispersion of the response is an important consideration, such as in many performance-based engineering evaluations. A MATLAB implementation of the proposed ground-motion selection algorithm can be downloaded from http://www.stanford.edu/~bakerjw/gm selection.html.

# 2.7 Appendix: An alternative greedy ground-motion selection technique

The ground-motion selection algorithm described in the body of this manuscript selects an initial set of ground motions whose response spectra match a set of simulated response spectra. These simulations are obtained from a multivariate normal distribution parameterized by the target mean and covariance matrices. A greedy optimization technique then further improves the match between the target and the sample means and variances and obtains the final set of ground motions.

Sometimes, it may not be possible to completely parameterize the distribution of the response spectra using the mean and covariance information. This includes situations where ground motions are selected to match the UHS (where only the mean spectrum needs to be considered) or where the mean and the variance information, but not the correlation information, are available. There may also be situations where the response spectrum does not follow a multivariate normal distribution. For such situations, the authors propose the following technique

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for selecting the initial ground-motion set that can be subsequently improved by the greedy optimization technique. The steps involved in the technique are summarized below.

- Step 1: Initialize the algorithm with an empty ground-motion set.
- Step 2: Set i = 1.
- Step 3: If the *i*th database ground motion (G<sub>i</sub>) is not already present in the ground-motion set, include it in the set and compute SSE<sub>s,i</sub> (i.e., the SSE<sub>s</sub> of the set after G<sub>i</sub> is included, where SSE<sub>s</sub> is defined in Equation 2).
- Step 4: Delete  $G_i$  from the set, if included in Step 3. Increment *i* by 1.
- Step 5: If *i* is less than or equal to the size of the ground-motion database, go to Step 3. Otherwise, identify the ground motion *i* that results in the minimum value of SSE<sub>s,i</sub>.
   Add the *i* th ground motion in the database to the ground-motion set.
- Step 5: If the size of the set equals the desired number of ground motions, terminate the algorithm. Otherwise, go to Step 2.

This selection technique will provide a reasonable starting set of ground motions that can be subsequently improved using the greedy optimization technique described earlier in the manuscript. This selection technique does not take advantage of the knowledge of the response spectrum distribution or the correlation structure, but is therefore more general in its application. It is also empirically seen to produce sets of ground motions with response spectrum mean and variance closely matching the corresponding target values.

To test the effectiveness of the technique, it is used to select a set of 40 ground motions for the scenario described earlier (magnitude = 7, distance to rupture = 10km,  $T^* = 2.63$ s and  $\varepsilon(T^*) = 2$ ). The response spectra of the selected records are shown in Figure 7a. The groundmotion set means and standard deviations are compared to the target means and standard deviations in Figure 7b-c. It can be seen that the matches are good, illustrating the effectiveness of the technique. Incidentally, despite the fact that the technique does not use the correlation information, it is seen that the mean absolute error between the sample and the target correlations (Equation 7) is only 0.15.


Figure 7: (a) Response spectra of 40 ground motions selected using the greedy selection and optimization techniques (b) Response spectrum mean (c) Response spectrum standard deviation.

## **3 SELECTED GROUND MOTIONS**

Using the approach of Section 2, two sets of 'broad-band' ground motions were selected that have the distribution of response spectra associated with moderately large earthquakes at small distances. A third set of ground motions was selected to have strong velocity pulses that might be expected at sites experiencing near-fault directivity. A fourth set of ground motions is provided to match a Uniform Hazard Spectrum for a site in Oakland, and is comparable to ground motions that would be used to satisfy a code-type analysis. Details regarding the selection of these sets of ground motions are provided in this section.

### 3.1 SET #1A: BROAD-BAND GROUND MOTIONS (M = 7, R = 10 KM, SOIL SITE)

This ground motion set consists of 40 unscaled three-component ground motions selected so that their horizontal response spectra match the median and log standard deviations predicted for a magnitude 7 strike slip earthquake at a distance of 10 km. The site  $V_{s30}$  (average shear wave velocity in the top 30m) was assumed to be 250 m/s. The means and standard deviations of resulting response spectra were computed from Boore and Atkinson (2008), and correlations of response spectra among periods were computed from Baker and Jayaram (2008). The ground motions were selected to match this target at periods between 0 and 5 seconds, as this was identified as the period range of interest for the systems being studied in the Transportation Research Program. Figure 8 illustrates the distribution of response spectra expected for this earthquake scenario (where the median response spectrum is computed by taking the exponential of  $\overline{\ln S_a}(T_i) \pm 1.96\sigma(T_i)$ ).

When using the procedure of Section 2 to search for ground motions matching the target means and standard deviations, ground motions of with any magnitude and with distance < 50

km were considered. This decision was made with the justification that the ground motion response spectra are often more important to structural response than the ground motion magnitude and distance (Shome et al. 1998), so using a wide magnitude and distance range would increase the number of potential usable ground motions without significantly compromising the accuracy of resulting structural analysis results obtained using the ground motions. Further, having ground motions with variability in their magnitude and distance values will allow researchers to examine whether there are trends in computed structural or geotechnical response parameters that correlate with variation in the ground motion properties such as magnitude and distance. Such studies are not possible when all of the selected ground motions have a narrow range of magnitudes and distances. Comparison of the ground motion magnitudes and distance target, are provided later in Section 3.6.

Because the selected ground motions in this set are intended specifically for use at soil sites, only recorded ground motions with site  $V_{s30}$  values between 200 and 400 m/s were considered for selection.

The response spectra of the selected ground motions are shown in Figure 8, and they visually match the target means and standard deviations of the logarithmic response spectrum predicted for this scenario. This match is further illustrated in Figure 9, which compares of the means and standard deviations of  $\ln Sa$  for the recorded ground motions to the associated targets. Table 6 in the appendix provides further summary data for the selected ground motions.



Figure 8: Response spectra of the selected ground motions<sup>2</sup> for soil sites, compared to the target response spectra predicted by the ground motion model (Boore and Atkinson 2008): (a) plot with log-log of the axes, and (b) plot with linear scaling of the axes.

<sup>&</sup>lt;sup>2</sup> Throughout this chapter, plots of response spectra show the geometric mean spectra of the horizontal ground motion components after they have been rotated to their fault-normal and fault-parallel orientations. This is only one way of defining spectral acceleration for multi-component ground motions, but was deemed suitable for these graphical comparisons. The project website at *http://peer.berkeley.edu/transportation/publications\_data.html* contains the complete documentation of the ground motions and spectra, and includes tables of these geometric mean spectra as well as GMRotI50 spectra (Boore et al. 2006) (which are generally very similar to the geometric mean values), vertical response spectra and individual-component response spectra.



Figure 9: (a) Target median response spectra and the median response spectra of the selected ground motions for soil sites (medians are computed as the exponentials of mean ln*Sa* values). (b) Target standard deviations of ln*Sa*, and standard deviations of the ln*Sa* values of the selected ground motions.

### 3.2 SET #1B: BROAD-BAND GROUND MOTIONS (M = 6, R = 25 KM, SOIL SITE)

This ground motion set was selected using the same procedures as Set #1A, except the ground motions selected so that their response spectra match the median and log standard deviations predicted for a magnitude 6 strike slip earthquake at a distance of 25 km. The site  $V_{s30}$  (average shear wave velocity in the top 30m) was again assumed to be 250 m/s. The response spectra of

the selected ground motions are shown in Figure 10 with the target spectra superimposed, and Comparison of the means and standard deviations of the selected spectra are compared to their corresponding targets in Figure 11. Selected summary data for these ground motions is provided in Table 7 of the Appendix.



Figure 10: Response spectra of the selected ground motions for soil sites, compared to the target response spectra predicted by the ground motion model (Boore and Atkinson 2008): (a) plot with log-log of the axes, and (b) plot with linear scaling of the axes.



# Figure 11: (a) Target median response spectra and the median response spectra of the selected ground motions for soil sites (medians are computed as the exponentials of mean ln*Sa* values). (b) Target standard deviations of ln*Sa*, and standard deviations of the ln*Sa* values of the selected ground motions.

Figure 12 shows the response spectra from Set #1A and #1B of the ground motions superimposed in a single plot, to illustrate the broad range of spectral amplitudes represented by the union of these two sets. Another way to view this variability is as a histogram of spectral values at a single period, as shown in Figure 13 for a period of 1 second. We see from Figure 12 and Figure 13 that elastic spectral values across the union of these two sets can vary by up to two orders of magnitude, and that the sets overlap at intermediate spectral values. Recalling that these

ground motions are all unscaled, we see that the union of these sets provides a set of as-recorded ground motions that cover a broad range of intensities of interest at sites located near active crustal earthquake sources.



Figure 12: Spectra ground motions selected for Set #1A and #1B.



Figure 13: Histogram of spectral acceleration values at a period of 1s from the ground motions in Set #1A and #1B.

#### **3.3** SET #2: BROAD-BAND GROUND MOTIONS (M = 7, R = 10 KM, ROCK SITE)

This ground motion set consists of 40 unscaled three-component ground motions selected so that their response spectra match the median and log standard deviations predicted for a magnitude 7 strike slip earthquake at a distance of 10 km. The site  $V_{s30}$  was assumed to be 760 m/s; this shear wave velocity is the only value that differs from the target scenario for Set #1. The larger  $V_{s30}$ value was chosen because ground motions are intended to be representative of those observed at rock sites, or to be used as bedrock level ground motions for site response analyses. The distribution of response spectra associated with this event was computed as for Set #1A and #1B.

All ground motions in the database with  $V_{s30} > 625$  m/s were considered for inclusion in the set (this was the narrowest range for which there were sufficient ground motions to ensure a good match to the target response spectrum distribution).

The response spectra of the selected ground motions are shown in Figure 14, and as with Set #1 they visually match the target means and standard deviations of the logarithmic response spectra predicted for this scenario. This match is also illustrated in Figure 15, which compares the means and standard deviations of  $\ln Sa$  for the recorded ground motions to the associated targets. Table 8 in the appendix provides further summary data for the selected ground motions.



Figure 14: Response spectra of the selected ground motions for rock sites, compared to the target response spectra predicted by the ground motion model (Boore and Atkinson 2008): (a) plot with log-log scaling of the axes, and (b) plot with linear scaling of the axes.



Figure 15: (a) Target median response spectra and the median response spectra of the selected ground motions for rock sites (medians are computed as the exponentials of mean ln*Sa* values). (b) Target standard deviations of ln*Sa*, and standard deviations of the ln*Sa* values of the selected ground motions.

### 3.4 SET #3: PULSE-LIKE GROUND MOTIONS

This ground motion set consists of 40 unscaled three-component ground motions containing strong velocity pulses of varying periods in their strike normal components. These velocity pulses are expected to occur in some ground motions observed near fault ruptures, due to directivity effects. Example velocity time histories of these motions are shown in Figure 16.

The ground motions in this set were all selected because they have a strong velocity pulse in the strike normal direction, as determined using the method described by Baker (2007). Strong velocity pulses are also apparent in a range of other orientations in these ground motions, but the strike-normal component was the one studied carefully during the selection process. The method used here to identify velocity pulses has previously been used in the PEER Design Ground Motion Library (Youngs et al. 2006) and the ATC-63 project (Applied Technology Council 2009b). The near-fault ground motions used in the ATC-63 project are similar to those here slight differences will be discussed below. For this set, no attempt was made to match any target response spectrum, so the selection procedure of Section 2 was not used.



Figure 16: Strike normal velocity time histories of four ground motions from Set #3.



Figure 17: Histogram of pulse periods in ground motion Set #3.

These 40 ground motions were chosen to have a variety of pulse periods. This was done because the pulse period, relative to the period(s) of oscillation a structure, is known to be an important factor affecting structural response. The histogram of pulse periods present in this set is shown in Figure 17. Pulse periods range between 1.0 seconds and 12.9 seconds, with a mean of 5.5 seconds. Pulse periods are determined as part of the analysis technique used to identify the pulses (Baker 2007), and pulse periods for the selected ground motions are tabulated along with other data in Table 9 of the appendix.

Histograms of peak ground velocities of the selected ground motions are shown in Figure 18, and indicate that these ground motions are generally very intense. Strike normal peak ground velocities range from 30 to 185 cm/s, with a mean of 85 cm/s. Strike parallel peak ground velocities are generally somewhat smaller (17 to 115 cm/s, with a mean of 61 cm/s), with the exception of the Chi-Chi TCU068 motion having a strike parallel PGV of 250 cm/s. Distances from the fault rupture are shown in Figure 19. All but one ground motion was observed within 11 km of the fault rupture, and the mean distance was 5 km. The selected ground motions come from earthquakes having a variety of rupture mechanisms.



Figure 18: Histogram of strike normal peak ground velocities in ground motion Set #3.



Figure 19: Histogram of closest distances to the fault ruptures for the ground motions in Set #3.

One benefit of the technique used to identify velocity pulses is that it also extracts the pulse portion of the ground motion from the overall ground motion. Example output from this extraction analysis is shown in Figure 20. Separate sets of time histories for the original motion, the extracted pulse and the residual ground motion are provided at http://peer.berkeley.edu/transportation/publications data.html, to facilitate any studies of the effects of the pulse and non-pulse components of the motions separately.



Figure 20: Original ground motion, extracted pulse, and residual ground motion for the 1979 Imperial Valley El Centro Array #3 ground motion.

### 3.5 SET #4: SITE-SPECIFIC GROUND MOTIONS FOR OAKLAND

These site-specific ground motions were selected to be representative of the hazard at the site of the I880 viaduct in Oakland, California. The viaduct runs from near the intersection of Center and 3rd Streets to Market and 5th Streets. Those locations are noted in Figure 21 below. For the hazard analysis used here, a location of 37.803N x 122.287W was used, and this location is labeled 'Oakland site' in Figure 21.



Figure 21: Location of I880 bridge viaduct. Aerial imagery from Google Earth (*http://earth.google.com*).

### 3.5.1 Information from previous ground motion selection for this site

Ground motions were previously selected for this site as part of the 2002 PEER Testbeds effort (2002). Information from that effort was thus utilized to determine site conditions and initial selection parameters. Key information from this 2002 report is summarized here. The bridge is located on soil classified as Sc ('soft rock') by the Uniform Building Code. Ground motions were selected under the assumption that the NEHRP side class is C or D. The 2002 report hazard analysis calculations showed that spectral accelerations at 1 second were caused primarily by earthquakes with magnitudes of 6.6 to 7, on the nearby Hayward fault (these observations are confirmed in the new hazard analysis below). The ground motions selected in 2002 were chosen to have distances of less than 10 km, and magnitudes from 5.5 to 6.2 (for the '50% in 50 years'

case) and magnitudes greater than 6.6 (for the '10% in 50 years' and '2% in 50 years' cases). The ground motions were taken exclusively from strike slip earthquake recordings. It is stated that "Some of the selected recordings contain strong forward rupture directivity pulses, but others do not." All ground motions were rotated to the strike-normal and strike-parallel orientations. Ten ground motions were provided at each hazard level.

The report states that "The ground motion time histories have not been scaled, because a unique period for use in scaling has not been identified. Once a period has been identified, a scaling factor should be found for the strike normal component using the strike normal response spectral value." Uniform hazard spectra were provided for each of the three exceedance probabilities of interest, and these would be used as the targets for ground motion scaling.

### 3.5.2 Hazard analysis

To characterize seismic hazard at the site (37.803N, 122.287W), the 2008 USGS hazard maps and interactive deaggregations tools were used (Petersen et al. 2008; USGS 2008). The assumed site conditions were  $V_{s30} = 360$  m/s (i.e., the NEHRP site class C/D boundary). Uniform hazard spectra were obtained, along with the mean magnitude/ distance/ $\varepsilon$  values associated with occurrence of each spectral value. This information is summarized in Table 3 through Table 5 for probabilities of exceedance of 2%, 10% and 50% in 50 years. These uniform hazard spectra are plotted in Figure 22.

Table 3:	Uniform hazard spectrum and mean deaggregation values of distance,
	magnitude and $\varepsilon$ for the Oakland site, with a 2% probability of exceedance in
	50 years.

Period (s)	Sa (g)	<i>R</i> (km)	М	З
0.0	0.94	8.8	6.78	1.70
0.1	1.78	8.4	6.73	1.76
0.2	2.20	8.4	6.77	1.74
0.3	2.13	8.5	6.81	1.73
1.0	1.14	9.9	7.00	1.74
2.0	0.60	13.4	7.20	1.74
5.0	0.22	16.0	7.43	1.64

Table 4:Uniform hazard spectrum and mean deaggregation values of distance,<br/>magnitude and ε for the Oakland site, with a 10% probability of exceedance in<br/>50 years.

Period (s)	Sa (g)	<i>R</i> (km)	М	З
0.0	0.60	10.1	6.80	1.05
0.1	1.11	10.0	6.75	1.10
0.2	1.38	10.0	6.78	1.10
0.3	1.32	10.2	6.82	1.09
1.0	0.67	11.8	7.00	1.09
2.0	0.34	15.6	7.15	1.09
5.0	0.12	16.9	7.31	1.01

Table 5:Uniform hazard spectrum and mean deaggregation values of distance,<br/>magnitude and  $\varepsilon$  for the Oakland site, with a 50% probability of exceedance in<br/>50 years.

Period (s)	Sa (g)	<i>R</i> (km)	M	3
0.0	0.27	15.1	6.79	0.00
0.1	0.48	15.0	6.73	0.10
0.2	0.60	15.7	6.76	0.11
0.3	0.56	16.2	6.80	0.10
1.0	0.26	19.3	6.96	0.04
2.0	0.12	24.2	7.06	0.02
5.0	0.04	24.2	7.13	-0.02



Figure 22: Uniform hazard spectra for the Oakland site.

The mean deaggregation values in Table 3 through Table 5 provide some idea as to the causal earthquakes causing occurrence of these spectral values. More complete information is only available, however, by looking at a complete deaggregation plot for a given period and spectral amplitude. Figure 23 and Figure 24 show the deaggregation plots for *Sa* values exceeded with 2% probability in 50 years at periods of 0.1 and 1 seconds, respectively. We see that at 0.1s, almost all occurrences of Sa(0.1s) = 1.78g are caused by earthquakes on the Hayward fault at 7km, having magnitudes of approximately 7. For reference, a map of the Oakland site is shown in Figure 26, noting the Hayward fault approximately 7 km away. Looking back to Table 3, the mean magnitude of 6.73 corresponds to these large Hayward fault events, and the mean distance of 8.4 km corresponds to the Hayward fault distance (it is larger than 7 km because some ground motions are caused on portions of the Hayward fault not occurring on this closest segment, and also because this is the mean distance of all events, and includes some events on the more distant San Andreas fault). At a period of 1 second, shown in Figure 24, we see that the contribution from the San Andreas Fault has gotten larger. That contribution continues to grow as the period gets larger (as seen in the increasing mean magnitude values with increasing period in Table 3).



Figure 23: Deaggregation plot for Sa(0.1s) exceeded with 2% probability in 50 years The largest contribution is from the Hayward fault at 7 km, with a small contribution from M>7 earthquakes on the San Andreas fault (figure from USGS 2008).



GMT 20 10 JJ 8 22:34:12 Distance (R), magnitude (M), epsilon (E0,E) deaggregation for a site on soil with a warage vsz 360. mistop 30 m. USGS CGHT PSHA2008 UPDATE Bins with H0.05% contrib. on the

## Figure 24: Deaggregation plot for Sa(1s) exceeded with 2% probability in 50 years. The largest contribution is from the Hayward fault at 7 km, with some contribution from M>7 earthquakes on the San Andreas fault (figure from USGS 2008).

Looking at the other hazard levels, we see that the mean distances increase and mean magnitudes and  $\varepsilon$ 's decrease as the probability of exceedance increases from 2% to 10% and 50% in 50 years. This is expected, as at these lower ground motion intensity levels one does not need such an extreme event (i.e., close distance, large magnitude, and large  $\varepsilon$ ) to achieve the given Sa level. At the 50% in 50 year level especially, larger-distance events contribute significantly to the hazard.

This variation in causal sources with period is one reason why the uniform hazard spectrum cannot be interpreted as the response spectrum associated with any single ground motion (Reiter 1990; Beyer and Bommer 2007). Also, note that the mean  $\varepsilon$  values in Table 3 are typically about 1.7, indicating that these spectral values are associated with ground motions having spectra 1.7 standard deviations larger than the mean predicted (logarithmic) spectra associated with the causal earthquake. Any single ground motion is unlikely to be this much larger than mean at all periods, providing a second reason why these uniform hazard spectra should not be interpreted as the spectra of individual ground motions that might be seen at this Oakland site (Baker and Cornell 2006). To help illustrate this, the uniform hazard spectra are replotted in Figure 22, along with median predicted spectrum (i.e., the exponential of the mean

predicted logarithmic spectrum) for a magnitude 7 earthquake at a distance of 10 km. This is the dominant causal earthquake for occurrence of Sa(1s)= 1.14g, the 2% in 50 year hazard value from Table 3, but the amplitude of this spectrum is dramatically lower than the 2% in 50 year spectrum. In fact, it is only slightly larger than the 50% in 50 years spectrum.



## Figure 25: Uniform hazard spectra for the Oakland site, compared to the median predicted spectrum for an M = 7, R= 10 km event (as predicted by Campbell and Bozorgnia 2008).

Despite the limitations of uniform hazard spectra discussed above, ground motions selected and scaled to approximately match these uniform hazard spectra have the advantage that their amplitude at any given period has approximately the same probability of exceedance; this is a useful property when one desires to use a single set of ground motions to analyze structures sensitive to excitation at differing periods, and one wants the ground motions to be comparably 'intense' in their excitation of each building. These uniform hazard spectra will thus be used as target spectra for the selection of site-specific ground motions.



Figure 26: Oakland site. The pushpin marks the site location and the Hayward fault is shown in the upper right portion of the map, approximately 7 km from the site.

### 3.5.3 Ground motion selection

With the above hazard and site information, ground motions were selected to represent the hazard at the site. The following criteria and procedures were used for selection:

- Forty three-component ground motions were selected at each hazard level.
- The selected ground motions were rotated from their as-recorded orientations to strikenormal and strike-parallel orientations.
- Ground motions were selected based on their close match to the target spectrum over a range of periods between 0 and 5 seconds.
- The ground motions have been amplitude scaled to match their target spectrum as closely as possible. (In the selection and scaling operation, mismatch is computed as the sum of squared differences between the logarithm of the scaled ground motion's geometric mean spectrum and the logarithm of the target spectrum.) All three components of the ground motion were scaled by the same factor. No ground motions were scaled by more than a

factor of 8. The mean scale factors of the selected ground motions were 3.8, 2.5 and 1.5 at the 2%, 10% and 50% in 50 years hazard levels, respectively.

- Ground motions were selected to have magnitudes between 5.9 and 7.3, to approximately match the magnitudes of causal earthquakes identified in the hazard calculations above.
- Ground motions were selected to have closest distances to the fault rupture of between 0 and 20 km for the 2% and 10% in 50 years hazard levels. At the 50% in 50 years hazard level, ground motions were selected to have closest distances to the fault rupture of between 0 and 30 km. These limits were chosen to be approximately consistent with the hazard deaggregation results above.
- Ground motions were selected to have  $V_{s30}$  values less than 550 m/s, to approximately represent the site conditions at the location of interest.
- No ground motions were selected from dam abutments, or from instruments located above the first floor of a structure.
- No restriction was put on the mechanism of the earthquake associated with the ground motion.
- No restriction was put on the number of ground motions selected from a single earthquake, although some ground motions were omitted manually if the initial selection identified two ground motions in close proximity to each other.
- The site of interest is close enough to the Hayward fault to potentially experience directivity effects, so some selected ground motions have velocity pulses in the fault-normal component of the recording. The selected sets for the 2%, 10% and 50% in 50 years hazard levels have 19, 16 and 7 pulses, respectively. The pulses were identified using the procedure of Baker (2007), and have a variety of pulse periods between 1 and 7 seconds. The fraction of pulse-like motions is approximately consistent with what might be expected at a site of this type (Shahi and Baker 2011), but an exact comparison is not possible because hazard analysis used here does not explicitly account for directivity effects, and even if it did the fraction of pulses expected would vary with the period of interest. This characterization nonetheless provides an approximate representation of potential directivity effects at the site.

The above criteria are a compromise between the desire to have ground motions whose properties closely matched the target properties identified above, and the limitations of the finite

number of recorded strong ground motions available for use. The restrictions above result in 172 ground motions being available at the 2% and 10% in 50 years hazard levels, out of 3551 total ground motions in the NGA library. At the 50% in 50 years hazard level, there are 303 available ground motions because of the increased range of acceptable distances used in that case.

Response spectra of the selected ground motions are shown Figure 27, Figure 28 and Figure 29. The selected motions in general have a close match to the target, but there is variability around the target spectra due to the inherent 'bumpiness' of real ground motions. The geometric means of the selected spectra generally match closely to the target spectra. An exception is at periods greater than 2.5 seconds for the 2% in 50 years hazard level, where the selected motions are slightly lower on average than the target spectrum; this is in part because those spectral values are partially driven by different events than the spectral values at shorter periods, as discussed above, so recorded ground motions tend not to have the shape of this enveloped uniform hazard spectrum. The discrepancy in this case is unavoidable given the currently available ground motion library, unless one is willing to relax the selection criteria listed above.

Additional summary data, as well as the time histories of the ground motions, are provided online at *http://peer.berkeley.edu/transportation/gm peer transportation.html*.



Figure 27: Target uniform hazard spectrum at the 2% in 50 years hazard level, and the response spectra of the selected ground motions.



Figure 28: Target uniform hazard spectrum at the 10% in 50 years hazard level, and the response spectra of the selected ground motions.



Figure 29: Target uniform hazard spectrum at the 50% in 50 years hazard level, and the response spectra of the selected ground motions.



Figure 30: Target uniform hazard spectrum at all three hazard levels, and the response spectra of the selected ground motions. (a) Log scale plot. (b) Linear scale plot.

## 3.6 ADDITIONAL COMPARISONS BETWEEN SELECTED GROUND MOTION SETS

Sets #1 and #2 were termed 'broadband' sets as they aimed to capture a specified variability in response spectra and also have a range of associated magnitude and distance values. In contrast, the ground motions in Set #4 aimed to match a specific response spectrum and specific magnitude and distance value. Here we make a few comparisons between these sets to illustrate the differences in resulting selected ground motions. Figure 31 shows the spectra from Set #1A (top row) and Set #4 at the 50%/50 years level (bottom row) in both log scale (left column) and linear scale (right column) to aid comparison of similar plots that were shown above. Clearly Set #1A has more variability in its response spectra than Set #4. Looking at the example individual spectra shown in these subfigures in blue, we also see that individual spectra tend to be 'bumpier' in Set #1A than Set #4. The bumpy Set #1 spectra are more representative of spectra from typical ground motions, as they have been selected to match the variability and period-toperiod correlations in response spectra from real ground motions, while the Set #4 spectra tend to be smoother than typical spectra, as they were preferentially selected due to their match to a smooth target spectrum. The Set #1B and #2 spectra are comparable to the Set #1A spectra plotted here, and the Set #4 spectra at the other two amplitudes are similar to the #4 spectra shown here.



Figure 31: (a) Set #1A (broadband soil) ground motions, plotted in log scale. (b) Set #1A (broadband soil) ground motions, plotted in linear scale. (c) Set #4 (site specific) ground motions for the 50% in 50 years hazard level, plotted in log scale. (d) Set #4 (site specific) ground motions for the 50% in 50 years hazard level, plotted in linear scale.

Figure 32 shows the magnitudes and distances of the selected ground motions for two sets of ground motions, to illustrate some differences between the broadband sets and the sitespecific sets. Some important characteristics of the broadband set are that they have wider variability in the magnitude and distance values of the selected ground motions, the ground motions are not scaled, and there was no attempt made to include or exclude velocity pulses from the set. Some important properties of the site-specific set are that they come from a relatively narrower range of magnitude and distance values (as only ground motions from that narrower range were considered for selection), the ground motions were amplitude scaled to match their associated target spectrum, and velocity pulses were included in the sets, to represent the expected fraction of ground motions at that site and hazard level that are expected to contain a velocity pulse.

The other broadband sets are qualitatively similar to Figure 32a, in that they have a broader range of magnitude and distance values, and the site-specific sets at the other two hazard levels are similar to Figure 32b in that they have a narrow range of magnitudes and distances.



Figure 32: Magnitude and distance of target ground motion scenario, and magnitudes and distances of selected ground motions. (a) Set #1A (broadband soil) ground motions, plotted in log scale. (b) Set #4 (site specific) ground motions for the 50% in 50 years hazard level.

Finally, it may be worth emphasizing again two other differences between the broadband and site-specific sets. The broadband sets have not been scaled, and there was no attempt to include or exclude velocity pulses from the selected motions. The site-specific sets, on the other hand, consist of ground motions that have been scaled so their spectra closely match the target, and velocity pulses have been included in proportion to the expected likelihood of seeing velocity pulses for that particular site and ground motion intensity level (so the number of velocity pulses in each set increases as the target spectrum increases). With these differences in mind, it will hopefully be apparent which set is most appropriate for a given analysis situation.

### 4 COMPARISON TO OTHER GROUND MOTION SETS

Several other efforts have provided standardized sets of ground motions for purposes similar to the goals here. A brief description of three similar popular sets is provided here for the purpose of comparison with the ground motions selected above, and to aid readers in choosing which set of motions might be most appropriate for their particular application.

### 4.1 SAC GROUND MOTIONS

Somerville et al. (1997) (*nisee.berkeley.edu/data/strong\_motion/sacsteel/ground\_motions.html*) selected sets of ten two-component ground motions selected to match NEHRP design response spectra for firm soil sites in Los Angeles, Seattle and Boston at multiple hazard levels (2% and 10% probabilities of exceedance in 50 years for all three sites, plus 50% probability of exceedance in 50 years at Los Angeles). Some of these ground motions were then used as inputs to site response analysis using SHAKE91 (Idriss and Sun 1992), to generate ground motions to be used for soft soil sites in each of the three cities of interest.

The recorded ground motions were selected to have magnitudes and distances that matched the approximate deaggregation results for hazard calculations at the specific sites considered. Recorded ground motions were supplemented by simulations when sufficient appropriate recordings were not available. Processing of the recorded ground motions (filtering and baseline correcting) was performed by the authors. The ground motions were scaled to best match their corresponding target design spectra. These objectives are very similar to those used to select Set #4 above, and some the Set #4 selection criteria were patterned directly after the criteria used here.

In addition to the above site-specific ground motions, a set of twenty three-component ground motions were selected to represent near-fault sites (ten recorded motions and ten simulated motions). These ground motions were selected because they were observed near earthquakes of relatively large magnitude. As with Set #3 above, which has similar goals, no target spectrum was considered when selecting these motions and no scaling of these motions was performed.

Some differences between the SAC motions and the above ground motions are:

- The SAC ground motions were selected in 1997, when available databases of recorded ground motions were much more limited compared to 2010. The recorded ground motions used in the SAC set thus necessarily come from a much more limited set of earthquakes than the sets provided in this report.
- A greater number of motions are provided in the sets provided in this report, reflecting the greater availability of recorded ground motions and greater willingness of analysts to perform more dynamic analyses.
- The SAC ground motions were developed for specific locations, allowing seismic hazard information for those locations to be considered when selecting ground motions. Sets #1-3 above have no specific associated site and thus could not utilize seismic hazard information. Set #4 above was selected under objectives similar to those of the SAC ground motion selection effort, although only a single site was considered for Set #4 while three sites were considered by Somerville et al.
- The SAC ground motions have been pre-scaled. Sets #1-3 above (the 'broadband' sets) are not pre-scaled, while the site-specific Set #4 has been pre-scaled.
- The SAC ground motions were selected to satisfy NEHRP building code requirements, specifically with respect to design response spectra. The above ground motions are intended for more general use, and thus do not use the NEHRP design spectra as a target spectrum (recognizing that this type of spectrum is often not appropriate for performance-based assessments).
- While the SAC near-fault ground motions were selected with similar objectives to the above Set #3, the SAC authors did not ensure that all ground motions in the set contained velocity pulses, and did not report any properties of velocity pulses that are present in the selected ground motions. Research progress since 1997 has enabled the Set #3 above to include such additional information.

### 4.2 LMSR GROUND MOTIONS

Krawinkler et al. (Krawinkler et al. 2003; Medina and Krawinkler 2003) selected four sets of ground motions, of which the Large-Magnitude Small-Distance (LMSR) set in particular has been widely used. This set consists of 20 two-component ground motions with magnitudes between 6.5 and 7, and distances between 13 and 30 km. No further effort was made to select the ground motions based on their response spectra. Three other sets provided by these authors had smaller magnitudes and/or larger distances, and were deemed less useful due to their lower ground motion intensity (although, after being scaled up to comparable response spectral values, these other sets were observed to produce similar structural responses to the LMSR set). These ground motions are similar in nature to Set #1 and Set #2 above, with the following minor differences:

- A greater number of motions are provided in the above sets, reflecting the greater availability of recorded ground motions and greater willingness of analysts to perform more dynamic analyses.
- The above sets provide two sets of motions, representing rock and soil site conditions.
- The above sets pay explicit attention to the response spectra of the selected motions. The LMSR set has similar variability in response spectra to the above broadband sets—this was achieved implicitly by limiting the magnitude and distance values of the selected ground motions to be comparable to a single event within the limitations of the finite ground motion library.
- The LMSR set has a much narrower range of magnitudes and distances than the above broadband sets.

### 4.3 FEMA P695 GROUND MOTIONS

Kircher et al. (Applied Technology Council 2009b, Appendix A) selected two ground motion sets for the FEMA P695 project that are intended to be structure independent and site independent, as is the objective of Sets #1 and #2 in this project. They provided a 'Far Field' set of 22 ground motions recorded at distances greater than 10 km, and a 'Near Field' set of 28 ground motions recorded at distances less than 10 km. One half of the ground motions in the Near Field set contained velocity pulses; these pulses were identified using the same wavelet-

based technique used in the current project (Baker 2007). Two component ground motions were provided. Only those ground motions with peak ground acceleration greater than 0.2g and peak ground velocity greater than 15 cm/sec were selected, and the sets were then 'normalized' (pre-scaled) to manipulate the variability in ground motion intensities seen in the scaled ground motions. After normalization, the authors note that the Far Field set of ground motions has a median spectrum comparable to that of a magnitude 7 earthquake at a distance of 15 km. The median spectrum of the Near-Field set was said to be comparable to a magnitude 7 earthquake at a distance of 5 km. The ground motions were selected specifically for assessing the collapse capacity of buildings using the FEMA P695 assessment procedure, and so the suggested normalization and scaling procedure provided by the authors may or may not be appropriate for other types of analysis objectives.

Some differences between the FEMA P695 motions and the above ground motions are:

- A greater number of motions are provided in the above sets.
- The FEMA P695 ground motions have been pre-scaled, while the above Sets #1-3 are provided unscaled. The above Set #4 has been pre-scaled, but does not retain the spectral variability of the FEMA P695 set.
- While both the P695 sets and the above sets of ground motions can be further scaled or modified by users, the FEMA P695 guidelines provide a specific set of recommended scaling instructions tailored for the purposes of assessing median collapse capacity of a structure.
- The 14 pulse-like ground motions in the FEMA P695 set (some of which match the ground motions provided in Set #3 here) are mixed with non-pulse-like ground motions, while here they are provided in an explicitly separate set.

### 5 CONCLUSIONS

This report summarizes an effort to select several sets of standardized ground motions for use by the PEER Transportation Research Program. The motions utilized the existing high quality NGA Database of recorded ground motions, and selectively searched that database for motions deemed appropriate for use in a variety of instances. Recent ground motion selection research at PEER has focused primarily on situations where the structure and location of interest are known, so that ground motions can be selected and modified with specific structural properties and seismic hazard information in mind. This project, in contrast, needed to consider a wide variety of structural and geotechnical systems at a wide range of locations, requiring standardized sets of ground motions to facilitate comparative evaluations in this research. Even in situations where a specific location is of interest, the Transportation Research Program is sometimes evaluating alternative structural systems (with differing periods of vibration) for potential use at a given location, so ground motion selection techniques that depend upon knowledge of structural periods are not applicable. Other techniques were thus needed to choose appropriate ground motion sets for this Research Program.

The selected sets included three 'broadband' sets (Sets #1A, 1B and 2) which capture spectral variability associated with a scenario earthquake magnitude and distance; sets were selected for two earthquake scenarios on both rock and soil site conditions. Ground motion Set #3 was selected to consist entirely of ground motions with strong velocity pulses, for analysts interested in the effect of such pulses on their structural or geotechnical system. Finally, 'site-specific' sets of ground motions were selected (Set #4), so that their response spectra closely matched a target Uniform Hazard Spectrum for a site in Oakland, California, at 2%, 10% and 50% probabilities of exceedance in 50 years. The assumed range of periods of interest was 0 to 5 seconds for all ground motion sets. These sets of ground motions vary in the procedures used to select them, the degree of heterogeneity of the ground motions within the set, and the analysis

objectives that they might be suited for. For that reason, comparisons of the properties of the various sets were provided, as well as comparisons to other popular ground motion sets in use today.

This report includes selected summary data for the ground motion sets, but the most detailed information is available in the form of the ground motion time histories themselves, and their metadata such as associated magnitudes, distances, and response spectra. A brief summary of the ground motion properties is provided in the Appendix, which provides a few metadata fields for each selected ground motion. A much more complete set of information is available from the project website (*http://peer.berkeley.edu/transportation/publications\_data.html*), including complete time histories and response spectra for all three components of each ground motion. The Appendix tables and project website spreadsheets all include the NGA Number for each ground motion, which matches the corresponding field in the NGA Flatfile (*http://peer.berkeley.edu/nga/documentation.html*). Some data not in the current NGA Flatfile, such as directivity pulse periods, scale factors (when applicable), and  $\varepsilon$  values, are included in the Appendix tables or in spreadsheets posted at the project website.

In addition to the practically useful ground motion sets, the key intellectual contribution of this project was a new algorithm for selecting ground motions whose response spectra have a specified mean and variance. The proposed algorithm is described in Section 2; it generates multiple response spectra from the target distribution using Monte Carlo Simulation, and then selects recorded ground motions whose response spectra individually match the simulated spectra. A greedy optimization technique further improves the match between the target and the sample means and variances, but at a fraction of the cost of a full optimization search. Prior to development of this proposed technique, selection of motions matching a target spectrum mean and variance was computationally prohibitive for the objective of this work. This is because matching a target spectrum variation requires comparisons of the median and variance of sets of ground motions to the target values. That is, the suitability of any particular ground motion can only be determined by computing the response spectrum variance of the complete ground-motion set in which it might be included, and that ground motion could be used in conjunction with a large number of possible sets. There are approximately 10<sup>93</sup> unique sets of 40 ground motions that can be chosen from the NGA library of 3500 ground motions, so searching over all of these combinations is not possible. As seen above, the proposed algorithm successfully identified sets of ground motions that matched the target spectrum means and variances, while requiring only a
few seconds of computation on a desktop computer. The new algorithm was utilized to select the specific ground motion sets described in Section 3, and the algorithm's source code has been made publicly available so that it can be used for other ground motion selection efforts by any users interested in this approach.

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## APPENDIX A: TABLES OF SELECTED GROUND MOTIONS

The following tables provide basic summary data for the selected ground motions. A significant amount of additional summary data, including response spectra and time history files for these ground motions, are available on the accompanying project website (*http://peer.berkeley.edu/transportation/publications\_data.html*).

Record number	NGA Record Sequence Number	Earthquake Name	Year	Station	Magnitude	Closest Distance	Preferred Vs30 (m/s)
1	231	Mammoth Lakes-01	1980	Long Valley Dam (Upr L Abut)	6.1	15.5	345
2	1203	Chi-Chi, Taiwan	1999	СНY036	7.6	16.1	233
3	829	Cape Mendocino	1992	Rio Dell Overpass – FF	7.0	14.3	312
4	169	Imperial Valley-06	1979	Delta	6.5	22.0	275
5	1176	Kocaeli, Turkey	1999	Yarimca	7.5	4.8	297
6	163	Imperial Valley-06	1979	Calipatria Fire Station	6.5	24.6	206
7	1201	Chi-Chi, Taiwan	1999	CHY034	7.6	14.8	379
8	1402	Chi-Chi, Taiwan	1999	NST	7.6	38.4	375
9	1158	Kocaeli, Turkey	1999	Duzce	7.5	15.4	276
10	281	Trinidad	1980	Rio Dell Overpass, E Ground	7.2	-	312
11	730	Spitak, Armenia	1988	Gukasian	6.8	-	275
12	768	Loma Prieta	1989	Gilroy Array #4	6.9	14.3	222
13	1499	Chi-Chi, Taiwan	1999	TCU060	7.6	8.5	273
14	266	Victoria, Mexico	1980	Chihuahua	6.3	19.0	275
15	761	Loma Prieta	1989	Fremont - Emerson Court	6.9	39.9	285
16	558	Chalfant Valley-02	1986	Zack Brothers Ranch	6.2	7.6	271
17	1543	Chi-Chi, Taiwan	1999	TCU118	7.6	26.8	215
18	2114	Denali, Alaska	2002	TAPS Pump Station #10	7.9	2.7	329
19	179	Imperial Valley-06	1979	El Centro Array #4	6.5	7.1	209
20	931	Big Bear-01	1992	San Bernardino - E & Hospitality	6.5	-	271
21	900	Landers	1992	Yermo Fire Station	7.3	23.6	354
22	1084	Northridge-01	1994	Sylmar - Converter Sta	6.7	5.4	251
23	68	San Fernando	1971	LA - Hollywood Stor FF	6.6	22.8	317
24	527	N. Palm Springs	1986	Morongo Valley	6.1	12.1	345
25	776	Loma Prieta	1989	Hollister - South & Pine	6.9	27.9	371
26	1495	Chi-Chi, Taiwan	1999	TCU055	7.6	6.4	273
27	1194	Chi-Chi, Taiwan	1999	CHY025	7.6	19.1	278
28	161	Imperial Valley-06	1979	Brawley Airport	6.5	10.4	209
29	1236	Chi-Chi, Taiwan	1999	CHY088	7.6	37.5	273
30	1605	Duzce, Turkey	1999	Duzce	7.1	6.6	276
31	1500	Chi-Chi, Taiwan	1999	TCU061	7.6	17.2	273
32	802	Loma Prieta	1989	Saratoga - Aloha Ave	6.9	8.5	371
33	6	Imperial Valley-02	1940	El Centro Array #9	7.0	6.1	213
34	2656	Chi-Chi, Taiwan-03	1999	TCU123	6.2	31.8	273
35	982	Northridge-01	1994	Jensen Filter Plant	6.7	5.4	373
36	2509	Chi-Chi, Taiwan-03	1999	CHY104	6.2	35.1	223
37	800	Loma Prieta	1989	Salinas - John & Work	6.9	32.8	271
38	754	Loma Prieta	1989	Coyote Lake Dam (Downst)	6.9	20.8	295
39	1183	Chi-Chi, Taiwan	1999	CHY008	7.6	40.4	211
40	3512	Chi-Chi, Taiwan-06	1999	TCU141	6.3	45.7	215

Table 6:Set #1A ground motions: Broad-band ground motions (M = 7, R = 10 km, soil site).

Record number	NGA Record Sequence Number	Earthquake Name	Year	Station	Magnitude	Closest Distance	Preferred Vs30 (m/s)
1	915	'Big Bear-01'	1992	'Lake Cachulla'	6.5	-	345
2	935	'Big Bear-01'	1992	'Snow Creek'	6.5	-	345
3	761	'Loma Prieta'	1989	'Fremont - Emerson Court'	6.9	39.9	285
4	190	'Imperial Valley-06'	1979	'Superstition Mtn Camera'	6.5	24.6	362
5	2008	'CA/Baja Border Area'	2002	'El Centro Array #7'	5.3	-	211
6	552	'Chalfant Valley-02'	1986	'Lake Crowley - Shehorn Res.'	6.2	24.5	339
7	971	'Northridge-01'	1994	'Elizabeth Lake'	6.7	36.6	235
8	1750	'Northwest China-02'	1997	'Jiashi'	5.9	-	275
9	268	'Victoria, Mexico'	1980	'SAHOP Casa Flores'	6.3	39.3	339
10	2003	'CA/Baja Border Area'	2002	'Calexico Fire Station'	5.3	-	231
11	668	'Whittier Narrows-01'	1987	'Norwalk - Imp Hwy, S Grnd'	6.0	20.4	270
12	88	'San Fernando'	1971	'Santa Felita Dam (Outlet)'	6.6	24.9	376
13	357	'Coalinga-01'	1983	'Parkfield - Stone Corral 3E'	6.4	34.0	376
14	188	'Imperial Valley-06'	1979	'Plaster City'	6.5	30.3	345
15	22	'El Alamo'	1956	'El Centro Array #9'	6.8	-	213
16	762	'Loma Prieta'	1989	'Fremont - Mission San Jose'	6.9	39.5	368
17	535	'N. Palm Springs'	1986	'San Jacinto - Valley Cemetary'	6.1	31.0	339
18	951	'Northridge-01'	1994	'Bell Gardens - Jaboneria'	6.7	44.1	309
19	2465	'Chi-Chi, Taiwan-03'	1999	'CHY034'	6.2	37.0	379
20	456	'Morgan Hill'	1984	'Gilroy Array #2'	6.2	13.7	271
21	2009	'CA/Baja Border Area'	2002	'Holtville Post Office'	5.3	0.0	203
22	470	'Morgan Hill'	1984	'San Juan Bautista, 24 Polk St'	6.2	27.2	371
23	216	'Livermore-01'	1980	'Tracy - Sewage Treatm Plant'	5.8	-	271
24	2664	'Chi-Chi, Taiwan-03'	1999	'TCU145'	6.2	48.5	215
25	522	'N. Palm Springs'	1986	'Indio'	6.1	35.6	207
26	131	'Friuli, Italy-02'	1976	'Codroipo'	5.9	41.4	275
27	964	'Northridge-01'	1994	'Compton - Castlegate St'	6.7	47.0	309
28	460	'Morgan Hill'	1984	'Gilroy Array #7'	6.2	12.1	334
29	920	'Big Bear-01'	1992	'North Shore - Salton Sea Pk HQ'	6.5	-	265
30	933	'Big Bear-01'	1992	'Seal Beach - Office Bldg'	6.5	-	371
31	214	'Livermore-01'	1980	'San Ramon - Eastman Kodak'	5.8	-	271
32	328	'Coalinga-01'	1983	'Parkfield - Cholame 3W'	6.4	45.7	339
33	122	'Friuli, Italy-01'	1976	'Codroipo'	6.5	33.4	275
34	2473	'Chi-Chi, Taiwan-03'	1999	'CHY047'	6.2	46.2	273
35	757	'Loma Prieta'	1989	'Dumbarton Bridge West End FF'	6.9	35.5	275
36	705	'Whittier Narrows-01'	1987	'West Covina - S Orange Ave'	6.0	16.3	309
37	247	'Mammoth Lakes-06'	1980	'Bishop - Paradise Lodge'	5.9	-	345
38	340	'Coalinga-01'	1983	'Parkfield - Fault Zone 16'	6.4	27.7	339
39	3275	'Chi-Chi, Taiwan-06'	1999	'CHY036'	6.3	46.2	233
40	604	'Whittier Narrows-01'	1987	'Canoga Park - Topanga Can'	6.0	49.0	267

Table 7:Set #1B ground motions: Broad-band ground motions (M = 6, R = 25 km, soil site).

Record number	NGA Record Sequence Number	Earthquake Name	Year	Station	Magnitude	Closest Distance	Preferred Vs30 (m/s)
1	72	San Fernando	1971	Lake Hughes #4	6.6	25.1	822
2	769	Loma Prieta	1989	Gilroy Array #6	6.9	18.3	663
3	1165	Kocaeli, Turkey	1999	Izmit	7.5	7.2	811
4	1011	Northridge-01	1994	LA - Wonderland Ave	6.7	20.3	1223
5	164	Imperial Valley-06	1979	Cerro Prieto	6.5	15.2	660
6	1787	Hector Mine	1999	Hector	7.1	11.7	685
7	80	San Fernando	1971	Pasadena - Old Seismo Lab	6.6	21.5	969
8	1618	Duzce, Turkey	1999	Lamont 531	7.1	8.0	660
9	1786	Hector Mine	1999	Heart Bar State Park	7.1	61.2	685
10	1551	Chi-Chi, Taiwan	1999	TCU138	7.6	9.8	653
11	3507	Chi-Chi, Taiwan-06	1999	TCU129	6.3	24.8	664
12	150	Coyote Lake	1979	Gilroy Array #6	5.7	3.1	663
13	572	Taiwan SMART1(45)	1986	SMART1 E02	7.3	-	660
14	285	Irpinia, Italy-01	1980	Bagnoli Irpinio	6.9	8.2	1000
15	801	Loma Prieta	1989	San Jose - Santa Teresa Hills	6.9	14.7	672
16	286	Irpinia, Italy-01	1980	Bisaccia	6.9	21.3	1000
17	1485	Chi-Chi, Taiwan	1999	TCU045	7.6	26.0	705
18	1161	Kocaeli, Turkey	1999	Gebze	7.5	10.9	792
19	1050	Northridge-01	1994	Pacoima Dam (downstr)	6.7	7.0	2016
20	2107	Denali, Alaska	2002	Carlo (temp)	7.9	50.9	964
21	1	Helena, Montana-01	1935	Carroll College	6.0	-	660
22	1091	Northridge-01	1994	Vasquez Rocks Park	6.7	23.6	996
23	1596	Chi-Chi, Taiwan	1999	WNT	7.6	1.8	664
24	771	Loma Prieta	1989	Golden Gate Bridge	6.9	79.8	642
25	809	Loma Prieta	1989	UCSC	6.9	18.5	714
26	265	Victoria, Mexico	1980	Cerro Prieto	6.3	14.4	660
27	1078	Northridge-01	1994	Santa Susana Ground	6.7	16.7	715
28	763	Loma Prieta	1989	Gilroy - Gavilan Coll.	6.9	10.0	730
29	1619	Duzce, Turkey	1999	Mudurnu	7.1	34.3	660
30	957	Northridge-01	1994	Burbank - Howard Rd.	6.7	16.9	822
31	2661	Chi-Chi, Taiwan-03	1999	TCU138	6.2	22.2	653
32	3509	Chi-Chi, Taiwan-06	1999	TCU138	6.3	33.6	653
33	810	Loma Prieta	1989	UCSC Lick Observatory	6.9	18.4	714
34	765	Loma Prieta	1989	Gilroy Array #1	6.9	9.6	1428
35	1013	Northridge-01	1994	LA Dam	6.7	5.9	629
36	1012	Northridge-01	1994	LA 00	6.7	19.1	706
37	1626	Sitka, Alaska	1972	Sitka Observatory	7.7	34.6	660
38	989	Northridge-01	1994	LA - Chalon Rd	6.7	20.5	740
39	748	Loma Prieta	1989	Belmont – Envirotech	6.9	44.1	628
40	1549	Chi-Chi, Taiwan	1999	TCU129	7.6	1.8	664

Table 8:Set #2 ground motions: Broad-band ground motions (M = 7, R = 10 km, rock site).

Record number	NGA Record Sequence Number	Earthquake Name	Year	Station Name	Magnitude	Closest Distance (km)	Pulse Period (s)	Preferred Vs30 (m/s)
1	170	Imperial Valley-06	1979	EC County Center FF	6.5	7.3	4.5	192
2	171	Imperial Valley-06	1979	EC Meloland Overpass FF	6.5	0.1	3.3	186
3	179	Imperial Valley-06	1979	El Centro Array #4	6.5	7.1	4.6	209
4	180	Imperial Valley-06	1979	El Centro Array #5	6.5	4.0	4.0	206
5	181	Imperial Valley-06	1979	El Centro Array #6	6.5	1.4	3.8	203
6	182	Imperial Valley-06	1979	El Centro Array #7	6.5	0.6	4.2	211
7	183	Imperial Valley-06	1979	El Centro Array #8	6.5	3.9	5.4	206
8	184	Imperial Valley-06	1979	El Centro Differential Array	6.5	5.1	5.9	202
9	451	Morgan Hill	1984	Coyote Lake Dam (SW Abut)	6.2	0.5	1.0	597
10	763	Loma Prieta	1989	Gilroy - Gavilan Coll.	6.9	10.0	1.8	730
11	779	Loma Prieta	1989	LGPC	6.9	3.9	4.4	478
12	879	Landers	1992	Lucerne	7.3	2.2	5.1	685
13	900	Landers	1992	Yermo Fire Station	7.3	23.6	7.5	354
14	982	Northridge-01	1994	Jensen Filter Plant	6.7	5.4	3.5	373
15	983	Northridge-01	1994	Jensen Filter Plant Generator	6.7	5.4	3.5	526
16	1044	Northridge-01	1994	Newhall - Fire Sta	6.7	5.9	1.0	269
17	1045	Northridge-01	1994	Newhall - W Pico Canyon Rd.	6.7	5.5	2.4	286
18	1063	Northridge-01	1994	Rinaldi Receiving Sta	6.7	6.5	1.2	282
19	1084	Northridge-01	1994	Sylmar - Converter Sta	6.7	5.4	3.5	251
20	1085	Northridge-01	1994	Sylmar - Converter Sta East	6.7	5.2	3.5	371
21	1086	Northridge-01	1994	Sylmar - Olive View Med FF	6.7	5.3	3.1	441
22	1106	Kobe, Japan	1995	КЈМА	6.9	1.0	1.0	312
23	1119	Kobe, Japan	1995	Takarazuka	6.9	0.3	1.4	312
24	1161	Kocaeli, Turkey	1999	Gebze	7.5	10.9	5.8	792
25	1197	Chi-Chi, Taiwan	1999	CHY028	7.6	3.1	2.2	543
26	1244	Chi-Chi, Taiwan	1999	CHY101	7.6	10.0	4.6	259
27	1489	Chi-Chi, Taiwan	1999	TCU049	7.6	3.8	11.7	487
28	1492	Chi-Chi, Taiwan	1999	TCU052	7.6	0.7	8.4	579
29	1493	Chi-Chi, Taiwan	1999	TCU053	7.6	6.0	12.8	455
30	1494	Chi-Chi, Taiwan	1999	TCU054	7.6	5.3	10.5	461
31	1505	Chi-Chi, Taiwan	1999	TCU068	7.6	0.3	12.2	487
32	1510	Chi-Chi, Taiwan	1999	TCU075	7.6	0.9	5.2	573
33	1511	Chi-Chi, Taiwan	1999	TCU076	7.6	2.8	4.0	615
34	1515	Chi-Chi, Taiwan	1999	TCU082	7.6	5.2	9.0	473
35	1519	Chi-Chi, Taiwan	1999	TCU087	7.6	7.0	9.4	474
36	1528	Chi-Chi, Taiwan	1999	TCU101	7.6	2.1	10.0	273
37	1529	Chi-Chi, Taiwan	1999	TCU102	7.6	1.5	9.7	714
38	1530	Chi-Chi, Taiwan	1999	TCU103	7.6	6.1	8.2	494
39	1546	Chi-Chi, Taiwan	1999	TCU122	7.6	9.4	10.9	475
40	1595	Chi-Chi, Taiwan	1999	WGK	7.6	10.0	4.4	259

 Table 9:
 Set #3 ground motions: Pulse-like ground motions.

Record number	NGA Record Sequence Number	Earthquake Name	Year	Station	Magnitude	Hypocentral Distance (km)	Closest Distance (km)	Preferred Vs30 (m/s)	FN Pulse	Pulse Period (s)
1	6	Imperial Valley-02	1940	El Centro Array #9	7.0	13.0	6.1	213	0	
2	159	Imperial Valley-06	1979	Agrarias	6.5	2.6	0.7	275	1	2.30
3	161	Imperial Valley-06	1979	Brawley Airport	6.5	43.2	10.4	209	1	4.03
4	165	Imperial Valley-06	1979	Chihuahua	6.5	18.9	7.3	275	0	
5	171	Imperial Valley-06	1979	EC Meloland Overpass FF	6.5	19.4	0.1	186	1	3.35
6	173	Imperial Valley-06	1979	El Centro Array #10	6.5	26.3	6.2	203	1	4.49
7	174	Imperial Valley-06	1979	El Centro Array #11	6.5	29.4	12.5	196	1	7.36
8	175	Imperial Valley-06	1979	El Centro Array #12	6.5	32.0	17.9	197	0	
9	178	Imperial Valley-06	1979	El Centro Array #3	6.5	28.7	12.9	163	1	5.24
10	179	Imperial Valley-06	1979	El Centro Array #4	6.5	27.1	7.1	209	1	4.61
11	180	Imperial Valley-06	1979	El Centro Array #5	6.5	27.8	4.0	206	1	4.05
12	181	Imperial Valley-06	1979	El Centro Array #6	6.5	27.5	1.4	203	1	3.84
13	183	Imperial Valley-06	1979	El Centro Array #8	6.5	28.1	3.9	206	1	5.39
14	184	Imperial Valley-06	1979	El Centro Differential Array	6.5	27.2	5.1	202	1	5.86
15	185	Imperial Valley-06	1979	Holtville Post Office	6.5	19.8	7.7	203	1	4.80
16	187	Imperial Valley-06	1979	Parachute Test Site	6.5	48.6	12.7	349	0	
17	266	Victoria, Mexico	1980	Chihuahua	6.3	36.7	19.0	275	0	
18	316	Westmorland	1981	Parachute Test Site	5.9	20.5	16.7	349	1	3.58
19	549	Chalfant Valley-02	1986	Bishop - LADWP South St	6.2	20.3	17.2	271	0	
20	718	Superstition Hills-01	1987	Wildlife Liquef. Array	6.2	24.8	17.6	207	0	
21	721	Superstition Hills-02	1987	El Centro Imp. Co. Cent	6.5	35.8	18.2	192	0	
22	728	Superstition Hills-02	1987	Westmorland Fire Sta	6.5	19.5	13.0	194	0	
23	768	Loma Prieta	1989	Gilroy Array #4	6.9	32.4	14.3	222	0	
24	802	Loma Prieta	1989	Saratoga - Aloha Ave	6.9	27.2	8.5	371	1	4.47
25	821	Erzican, Turkey	1992	Erzincan	6.7	9.0	4.4	275	1	2.65
26	949	Northridge-01	1994	Arleta - Nordhoff Fire Sta	6.7	11.1	8.7	298	0	
27	959	Northridge-01	1994	Canoga Park - Topanga Can	6.7	4.9	14.7	267	0	
28	982	Northridge-01	1994	Jensen Filter Plant	6.7	13.0	5.4	373	1	3.53
29	1042	Northridge-01	1994	N Hollywood - Coldwater Can	6.7	13.1	12.5	446	0	
30	1044	Northridge-01	1994	Newhall - Fire Sta	6.7	20.3	5.9	269	0	
31	1052	Northridge-01	1994	Pacoima Kagel Canyon	6.7	19.3	7.3	508	0	
32	1063	Northridge-01	1994	Rinaldi Receiving Sta	6.7	10.9	6.5	282	1	1.23
33	1082	Northridge-01	1994	Sun Valley - Roscoe Blvd	6.7	12.4	10.1	309	0	
34	1085	Northridge-01	1994	Sylmar - Converter Sta East	6.7	13.6	5.2	371	1	3.49
35	1116	Kobe, Japan	1995	Shin-Osaka	6.9	46.0	19.2	256	0	
36	1602	Duzce, Turkey	1999	Bolu	7.1	41.3	12.0	326	0	
37	1605	Duzce, Turkey	1999	Duzce	7.1	1.6	6.6	276	0	
38	2457	Chi-Chi, Taiwan-03	1999	CHY024	6.2	25.5	19.7	428	1	3.19
39	2734	Chi-Chi, Taiwan-04	1999	CHY074	6.2	10.1	6.2	553	0	
40	2739	Chi-Chi, Taiwan-04	1999	CHY080	6.2	14.5	12.5	553	0	

 Table 10:
 Set #4 ground motions selected for the 2% in 50 years hazard level.

d number	Record Ence Ber	quake		c	itude	central nce (km)	st nce (km)	rred Vs30	lse	Period (s)
Recor	NGA F Seque	Eartho	'ear	statio	Magn	<sup>1</sup> ypod Distar	Closes Distar	refei m/s)	nd N:	Julse
1	6	Imperial Valley-02	1940	El Centro Array #9	7.0	13.0	6.1	213	0	
2	159	Imperial Valley-06	1979	Agrarias	6.5	2.6	0.7	275	1	2.30
3	161	Imperial Valley-06	1979	Brawley Airport	6.5	43.2	10.4	209	1	4.03
4	165	Imperial Valley-06	1979	Chihuahua	6.5	18.9	7.3	275	0	
5	173	Imperial Valley-06	1979	El Centro Array #10	6.5	26.3	6.2	203	1	4.49
6	174	Imperial Valley-06	1979	El Centro Array #11	6.5	29.4	12.5	196	1	7.36
7	175	Imperial Valley-06	1979	El Centro Array #12	6.5	32.0	17.9	197	0	
8	178	Imperial Valley-06	1979	El Centro Array #3	6.5	28.7	12.9	163	1	5.24
9	179	Imperial Valley-06	1979	El Centro Array #4	6.5	27.1	7.1	209	1	4.61
10	180	Imperial Valley-06	1979	El Centro Array #5	6.5	27.8	4.0	206	1	4.05
11	181	Imperial Valley-06	1979	El Centro Array #6	6.5	27.5	1.4	203	1	3.84
12	183	Imperial Valley-06	1979	El Centro Array #8	6.5	28.1	3.9	206	1	5.39
13	184	Imperial Valley-06	1979	El Centro Differential Array	6.5	27.2	5.1	202	1	5.86
14	185	Imperial Valley-06	1979	Holtville Post Office	6.5	19.8	7.7	203	1	4.80
15	187	Imperial Valley-06	1979	Parachute Test Site	6.5	48.6	12.7	349	0	
16	192	Imperial Valley-06	1979	Westmorland Fire Sta	6.5	52.8	15.3	194	0	
17	266	Victoria, Mexico	1980	Chihuahua	6.3	36.7	19.0	275	0	
18	316	Westmorland	1981	Parachute Test Site	5.9	20.5	16.7	349	1	3.58
19	549	Chalfant Valley-02	1986	Bishop - LADWP South St	6.2	20.3	17.2	271	0	
20	718	Superstition Hills-01	1987	Wildlife Liquef. Array	6.2	24.8	17.6	207	0	
21	721	Superstition Hills-02	1987	El Centro Imp. Co. Cent	6.5	35.8	18.2	192	0	
22	728	Superstition Hills-02	1987	Westmorland Fire Sta	6.5	19.5	13.0	194	0	
23	767	Loma Prieta	1989	Gilroy Array #3	6.9	31.4	12.8	350	0	
24	768	Loma Prieta	1989	Gilroy Array #4	6.9	32.4	14.3	222	0	
25	802	Loma Prieta	1989	Saratoga - Aloha Ave	6.9	27.2	8.5	371	1	4.47
26	949	Northridge-01	1994	Arleta - Nordhoff Fire Sta	6.7	11.1	8.7	298	0	
27	959	Northridge-01	1994	Canoga Park - Topanga Can	6.7	4.9	14.7	267	0	
28	982	Northridge-01	1994	Jensen Filter Plant	6.7	13.0	5.4	373	1	3.53
29	1004	Northridge-01	1994	LA - Sepulveda VA Hospital	6.7	8.5	8.4	380	0	
30	1042	Northridge-01	1994	N Hollywood - Coldwater Can	6.7	13.1	12.5	446	0	
31	1044	Northridge-01	1994	Newhall - Fire Sta	6.7	20.3	5.9	269	0	
32	1063	Northridge-01	1994	Rinaldi Receiving Sta	6.7	10.9	6.5	282	1	1.23
33	1082	Northridge-01	1994	Sun Valley - Roscoe Blvd	6.7	12.4	10.1	309	0	
34	1085	Northridge-01	1994	Sylmar - Converter Sta East	6.7	13.6	5.2	371	1	3.49
35	1602	Duzce, Turkey	1999	Bolu	7.1	41.3	12.0	326	0	
36	1605	Duzce, Turkey	1999	Duzce	7.1	1.6	6.6	276	0	
37	1611	Duzce, Turkey	1999	Lamont 1058	7.1	13.4	0.2	425	0	
38	2699	Chi-Chi, Taiwan-04	1999	CHY024	6.2	27.9	19.7	428	0	
39	2734	Chi-Chi, Taiwan-04	1999	CHY074	6.2	10.1	6.2	553	0	
40	2739	Chi-Chi, Taiwan-04	1999	CHY080	6.2	14.5	12.5	553	0	

 Table 11:
 Set #4 ground motions selected for the 10% in 50 years hazard level.

number	ecord Ice r	Jake			ude	entral e (km)	ie (km)	ed Vs30	ē	eriod (s)
Record	NGA Ré Sequen Numbe	Earthqu Name	Year	Station	Magnit	Hypoce Distanc	Closest Distanc	Preferr (m/s)	FN Puls	Pulse P
1	6	Imperial Valley-02	1940	El Centro Array #9	7.0	13.0	6.1	213	0	
2	68	San Fernando	1971	LA - Hollywood Stor FF	6.6	39.5	22.8	316	0	
3	79	San Fernando	1971	Pasadena - CIT Athenaeum	6.6	42.8	25.5	415	0	
4	161	Imperial Valley-06	1979	Brawley Airport	6.5	43.2	10.4	209	1	4.03
5	162	Imperial Valley-06	1979	Calexico Fire Station	6.5	17.7	10.5	231	0	
6	163	Imperial Valley-06	1979	Calipatria Fire Station	6.5	57.1	24.6	206	0	
7	169	Imperial Valley-06	1979	Delta	6.5	33.7	22.0	275	0	
8	174	Imperial Valley-06	1979	El Centro Array #11	6.5	29.4	12.5	196	1	7.36
9	175	Imperial Valley-06	1979	El Centro Array #12	6.5	32.0	17.9	197	0	
10	179	Imperial Valley-06	1979	El Centro Array #4	6.5	27.1	7.1	209	1	4.61
11	183	Imperial Valley-06	1979	El Centro Array #8	6.5	28.1	3.9	206	1	5.39
12	184	Imperial Valley-06	1979	El Centro Differential Array	6.5	27.2	5.1	202	1	5.86
13	187	Imperial Valley-06	1979	Parachute Test Site	6.5	48.6	12.7	349	0	
14	302	Irpinia, Italy-02	1980	Rionero In Vulture	6.2	29.8	22.7	530	0	
15	549	Chalfant Valley-02	1986	Bishop - LADWP South St	6.2	20.3	17.2	271	0	
16	553	Chalfant Valley-02	1986	Long Valley Dam (Downst)	6.2	23.8	21.1	345	0	
17	718	Superstition Hills-01	1987	Wildlife Liquef. Array	6.2	24.8	17.6	207	0	
18	721	Superstition Hills-02	1987	El Centro Imp. Co. Cent	6.5	35.8	18.2	192	0	
19	728	Superstition Hills-02	1987	Westmorland Fire Sta	6.5	19.5	13.0	194	0	
20	754	Loma Prieta	1989	Coyote Lake Dam (Downst)	6.9	30.9	20.8	295	0	
21	767	Loma Prieta	1989	Gilroy Array #3	6.9	31.4	12.8	350	0	
22	768	Loma Prieta	1989	Gilroy Array #4	6.9	32.4	14.3	222	0	
23	802	Loma Prieta	1989	Saratoga - Aloha Ave	6.9	27.2	8.5	371	1	4.47
24	880	Landers	1992	Mission Creek Fault	7.3	32.9	27.0	345	0	
25	882	Landers	1992	North Palm Springs	7.3	32.3	26.8	345	0	
26	982	Northridge-01	1994	Jensen Filter Plant	6.7	13.0	5.4	373	1	3.53
27	985	Northridge-01	1994	LA - Baldwin Hills	6.7	28.2	29.9	297	0	
28	987	Northridge-01	1994	LA - Centinela St	6.7	25.4	28.3	235	0	
29	1004	Northridge-01	1994	LA - Sepulveda VA Hospital	6.7	8.5	8.4	380	0	
30	1008	Northridge-01	1994	LA - W 15th St	6.7	29.6	29.7	405	0	
31	1010	Northridge-01	1994	LA- Wadsworth VA Hospital S	6.7	19.6	23.6	414	0	
32	1042	Northridge-01	1994	N Hollywood - Coldwater Can	6.7	13.1	12.5	446	0	
33	1077	Northridge-01	1994	Santa Monica City Hall	6.7	22.5	26.5	336	0	
34	1082	Northridge-01	1994	Sun Valley - Roscoe Blvd	6.7	12.4	10.1	309	0	
35	1602	Duzce, Turkey	1999	Bolu	7.1	41.3	12.0	326	0	
36	2624	Chi-Chi, Taiwan-03	1999	TCU073	6.2	24.8	20.9	273	0	
37	2655	Chi-Chi, Taiwan-03	1999	TCU122	6.2	24.5	19.3	475	0	
38	2739	Chi-Chi, Taiwan-04	1999	CHY080	6.2	14.5	12.5	553	0	
39	2752	Chi-Chi, Taiwan-04	1999	CHY101	6.2	28.0	21.7	259	0	
40	2893	Chi-Chi, Taiwan-04	1999	TCU122	6.2	31.9	23.2	475	0	

 Table 12:
 Set #4 ground motions selected for the 50% in 50 years hazard level.