

# Surrogate Models of Highway Bridges for Regional-Scale Simulations of Transportation Networks

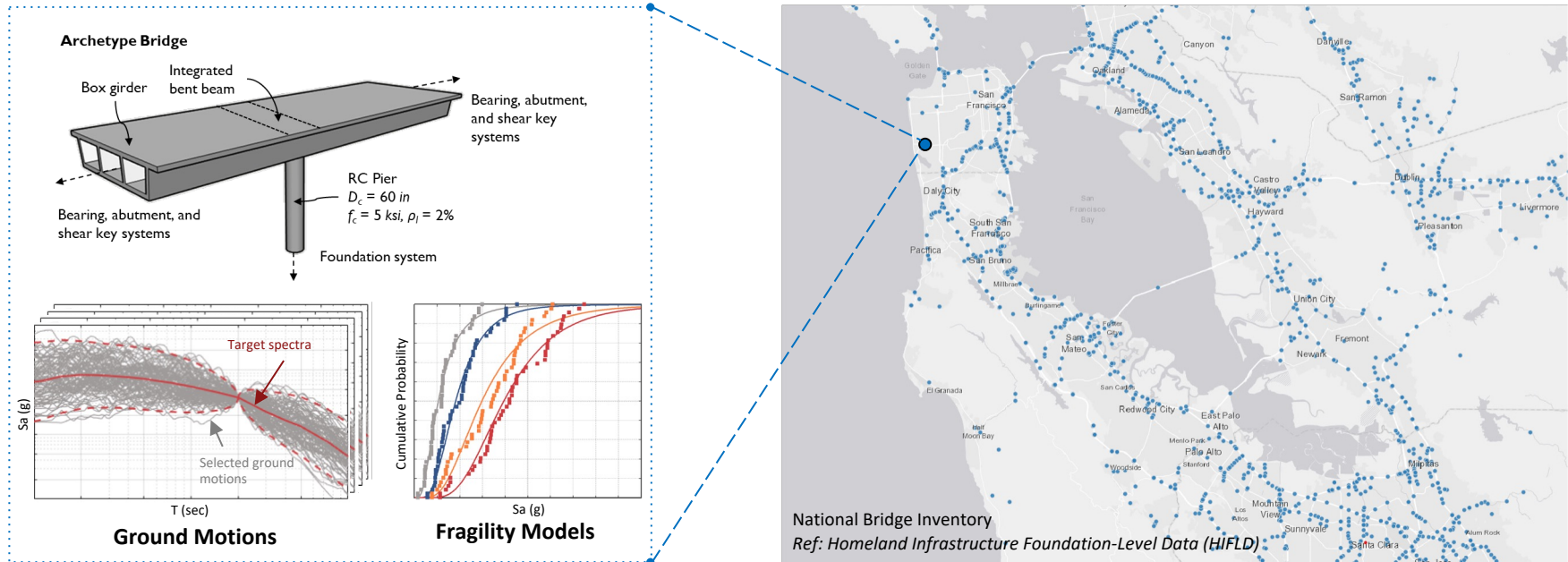
Greg Deierlein, Mia Lochhead, and Peter Lee  
*Stanford University*

Kuanshi Zhong  
*University of Cincinnati*

PEER 2023 Annual Meeting

# Seismic risk analysis of regional distributed transportation infrastructure to support planning for design, retrofit, and post-earthquake recovery

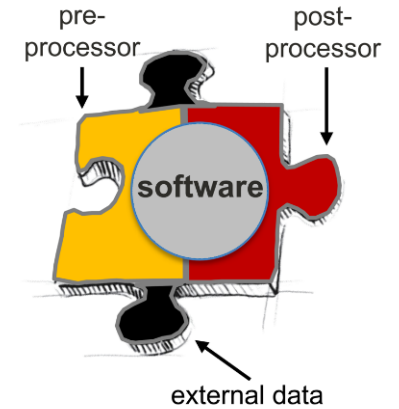
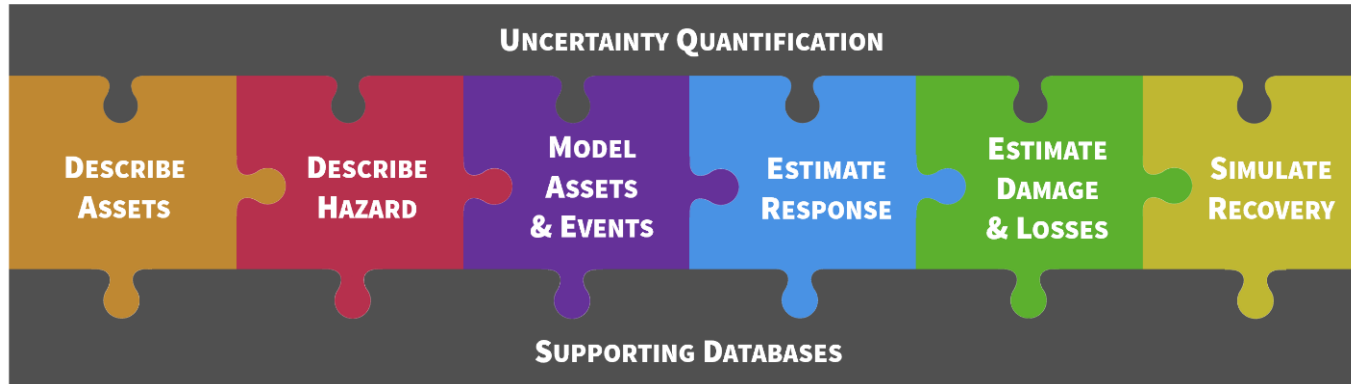
- Bridge design/modeling parameters and inventory data
- Regional earthquake ground motion hazard data
- Bridge response and damage assessment



# Outline for Today

- **Overview of supporting SimCenter tools**
  - quoFEM, EE-UQ, R2D
- **Surrogate modeling of bridge performance (quoFEM, EE-UQ)**
  - Surrogate modelling methods: SAF-IDA, Gaussian Process, PLoM
  - Scope of design studies - archetype bridge models
  - Training and assessment of surrogate models
- **Regional simulation of bridges in highway network (R2D)**
  - Characterization of ground motion hazard
  - OpenSees vs Surrogate
- **Next Steps**

# SimCenter Computational Framework



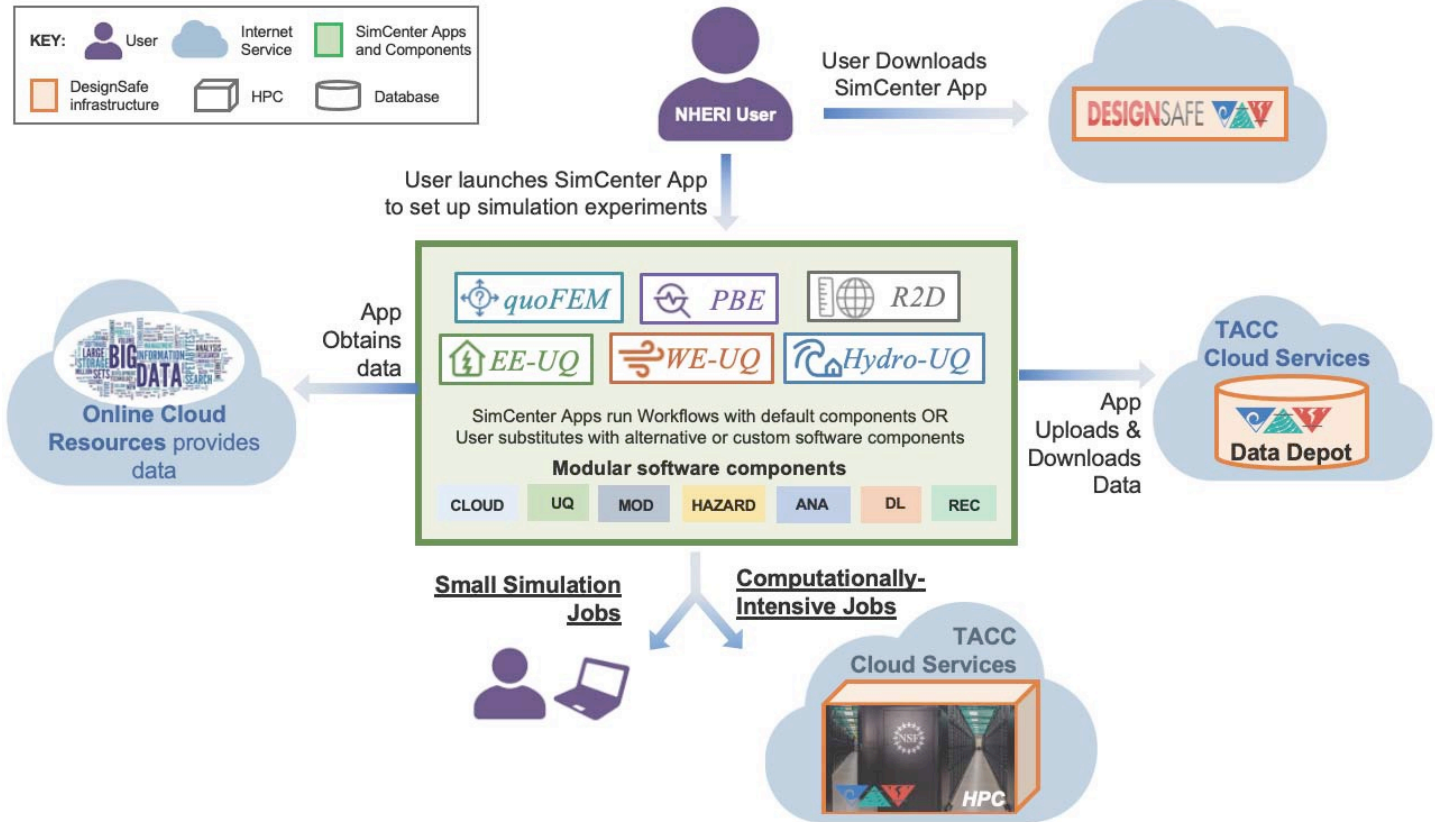
$$v(DV) = \iiint G\langle DV | DM \rangle | dG\langle DM | EDP \rangle | dG\langle EDP | IM \rangle | d\lambda(IM)$$

Impact

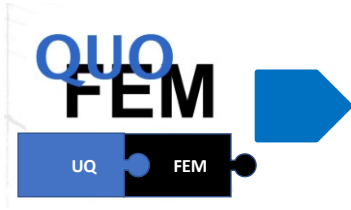
Performance (Loss) Models and Simulation

Hazard

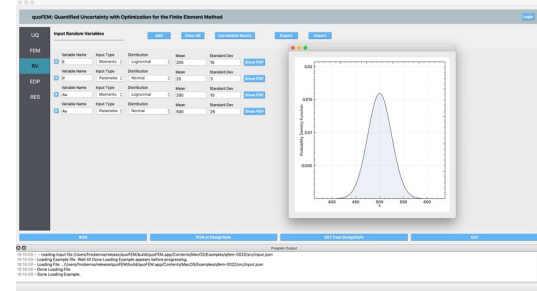
# Computational Eco-system



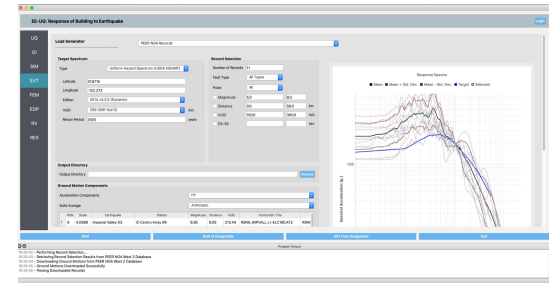
# Integration in SimCenter Software



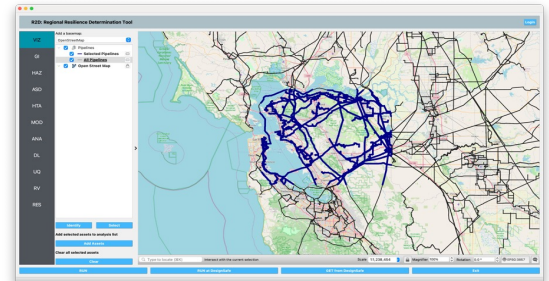
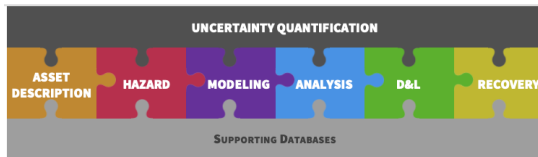
Coupling: Quantification of Uncertainties & Optimization with FEM, including capabilities for surrogate modeling (GP, PLoM)



Response of structures to ground shaking with SAF-IDA, GP, PLoM features to develop surrogate models



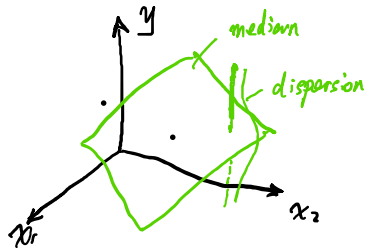
Regional assessment of facilities and systems to natural hazards



# Outline for Today

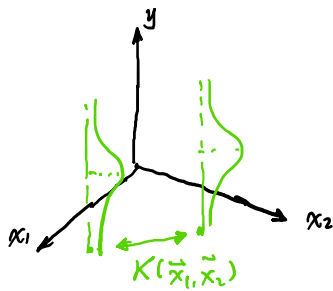
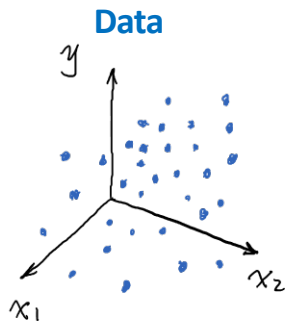
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# Surrogate Model Alternatives



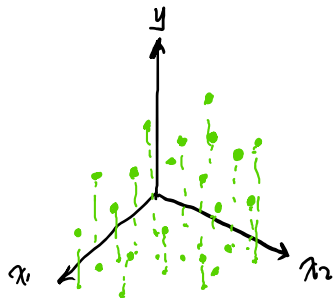
## Site-specific Adjustment Framework for IDA (SAF-IDA)

- Log Linear (parametric) and local linear regression (piecewise parametric)
- Training coefficients/weights ( $w$ )
- Predict median/dispersion of independent performance metrics
- Models are expensive (and loose accuracy) for high-dimension datasets



## Gaussian Process Regression (GP)

- Non-parametric
- Selecting the covariance function ( $K$ ) and training its hyper-parameters
- Predict median/dispersion
- Expensive for high-dimension/large-size datasets (sparse GP can improve)



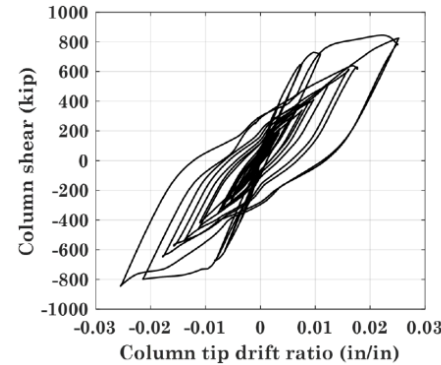
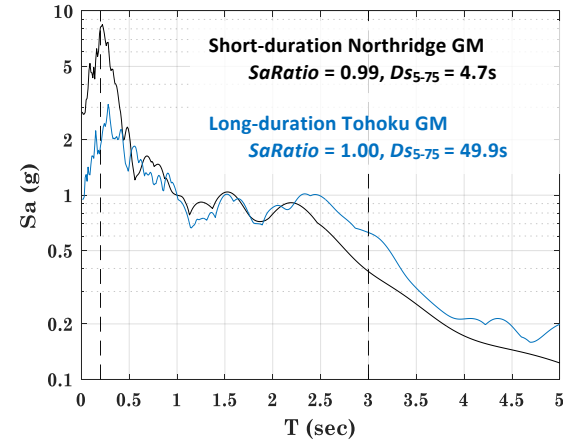
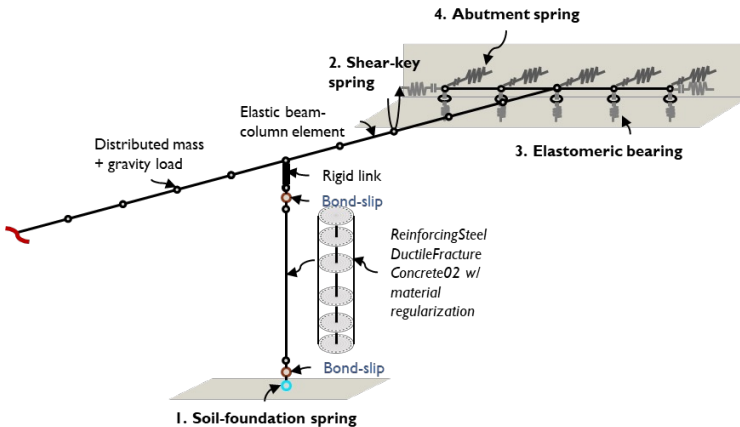
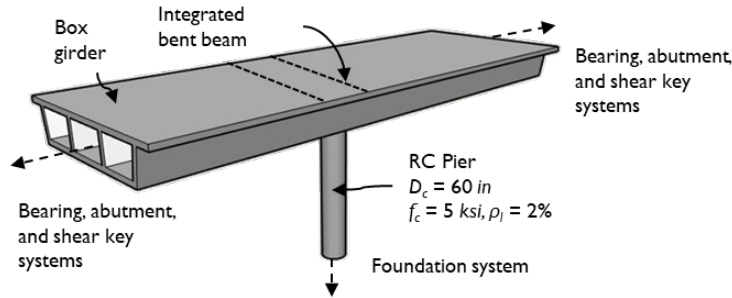
## Probabilistic Learning on Manifolds (PLoM)

- Non-parametric
- Training its diffusion-map hyper-parameters ( $\beta, \epsilon$ )
- Predict correlated samples directly
- Efficient for high-dimension correlated datasets

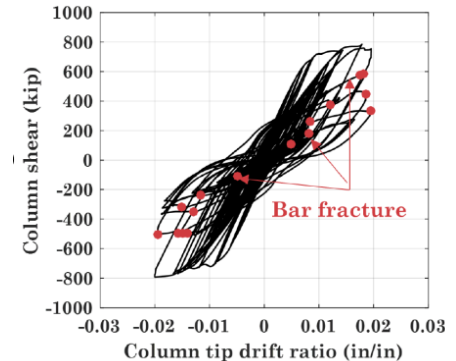


# Simulation of RC Bridge Pier: EQ Duration Effects

Archetype Bridge

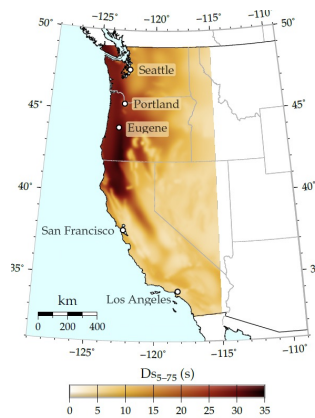


Short Duration

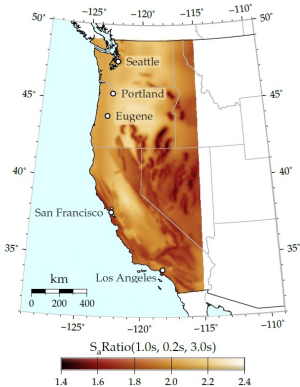


Long Duration

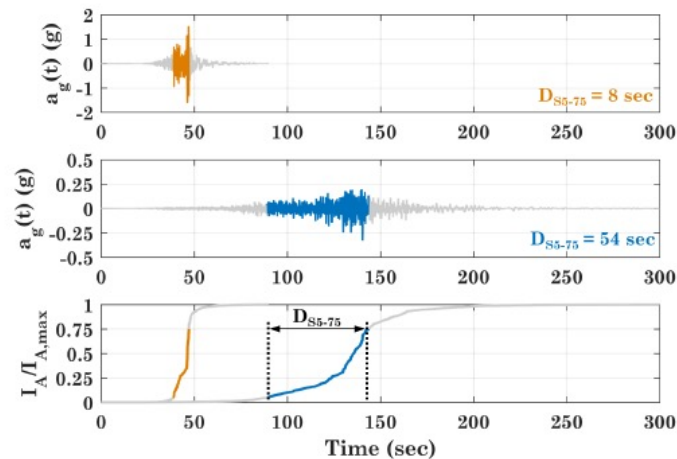
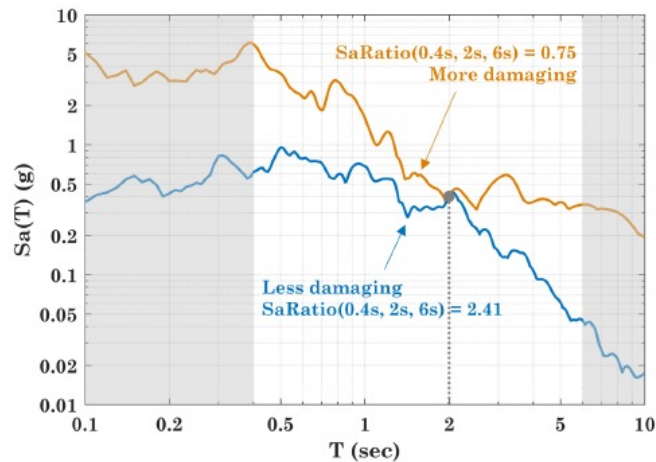
# Site-specific Adjustment Framework for IDA



Significant Duration



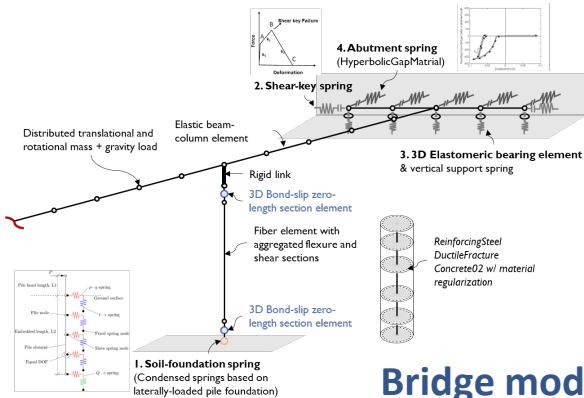
Spectral Shape



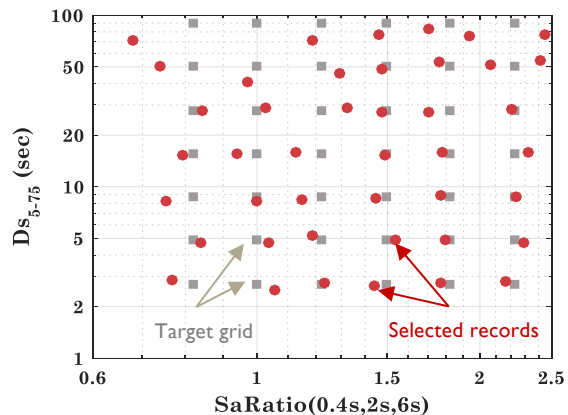
Adjust structural response from IDA to account for:

- Spectral Intensity,  $Sa(T_1)$
- Spectral Shape,  $SaRatio(T_S, T_1, T_L)$
- Significant Duration,  $D_{S5-75}$

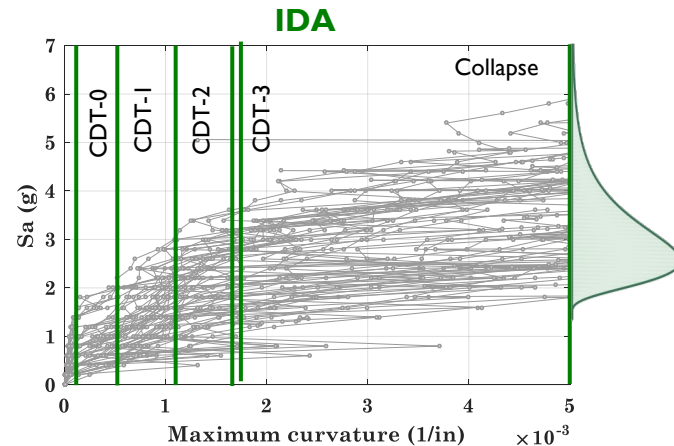
# SAF-IDA: Ground Motions and Model Training Data



Bridge model



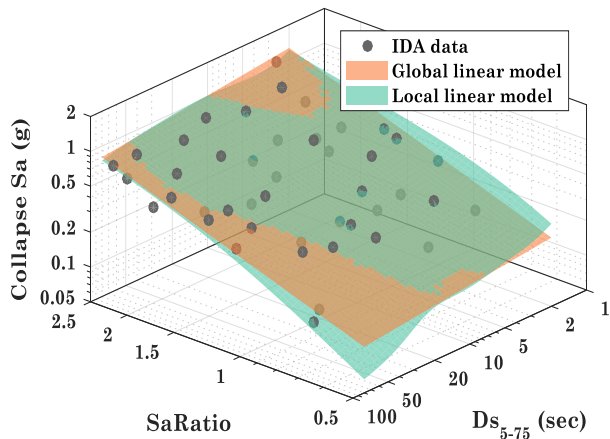
Grid (7x7) ground motion set



Using the statistics to develop limit-state fragility functions:

- CDT: curvature-based component damage thresholds (*Mangalathu, 2017*)
- First bar fracture
- 50% bars fracture
- **Collapse**

# SAF-IDA: Collapse Capacity

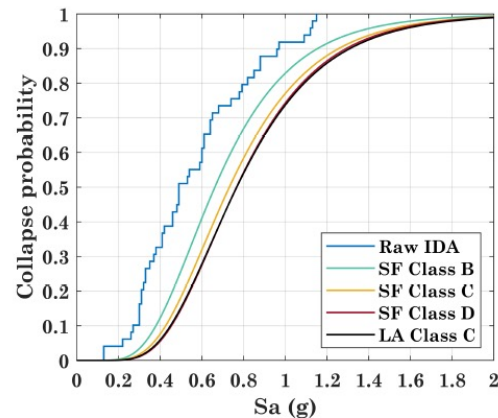


$$\ln(Sa_{collapse}) = 1.00 + 0.4 \ln(SaRatio) - 0.13 \ln(Ds_{5-75}) + \varepsilon$$

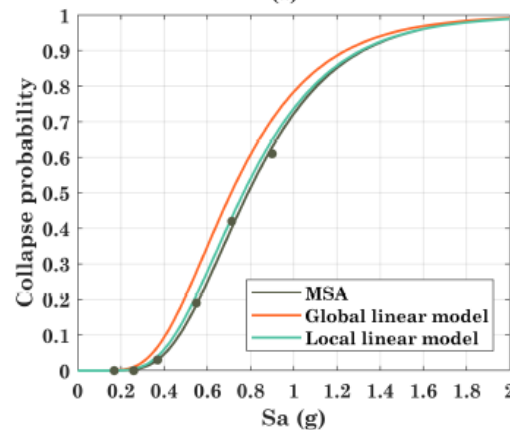
Median collapse capacity

GM parameters

**Response Surface (log-linear)**



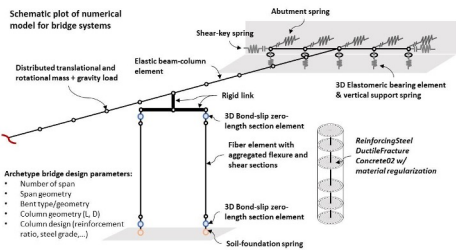
**Raw & Adjusted Collapse**



**Validation w/Multi-Stripe Analysis (MSA)**

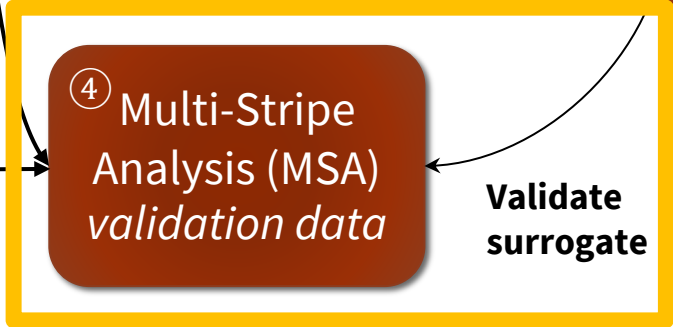
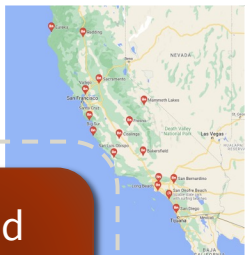
# Bridge Surrogate Models - PLoM

① Concrete bridge models



② Site deaggregation

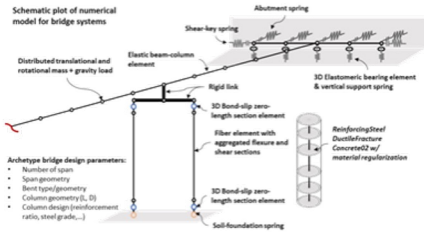
Ground motion selection



⑤ Regional Analyses

# PLoM: IDA Training Parameters and Data

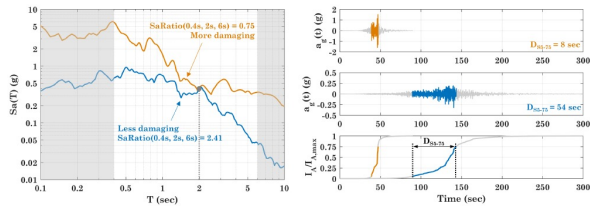
## Structural Design & Modeling Parameters ( $X_S$ )



### Model Parameters:

- Pier Slenderness ( $L/D$ )
- Axial Load Ratio ( $P/P_o$ )
- Reinf. Ratio ( $A_s/A_g$ )
- Steel  $F_y$

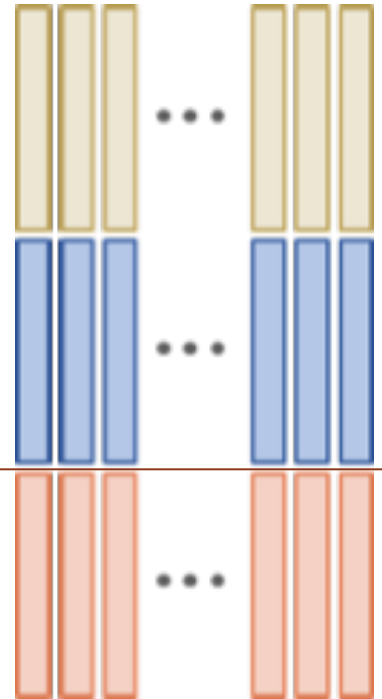
## Site Specific Ground Motion Characteristics ( $X_{GM}$ )



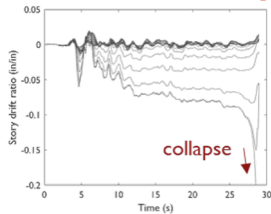
### GM Parameters:

- $S_a(T_1)$
- SaRatio
- Duration,  $D_{5-75}$

# of IDA Simulations  
(600 x ~20 = ~12,000)



## Structural Response & Damage Quantities ( $X_R$ )

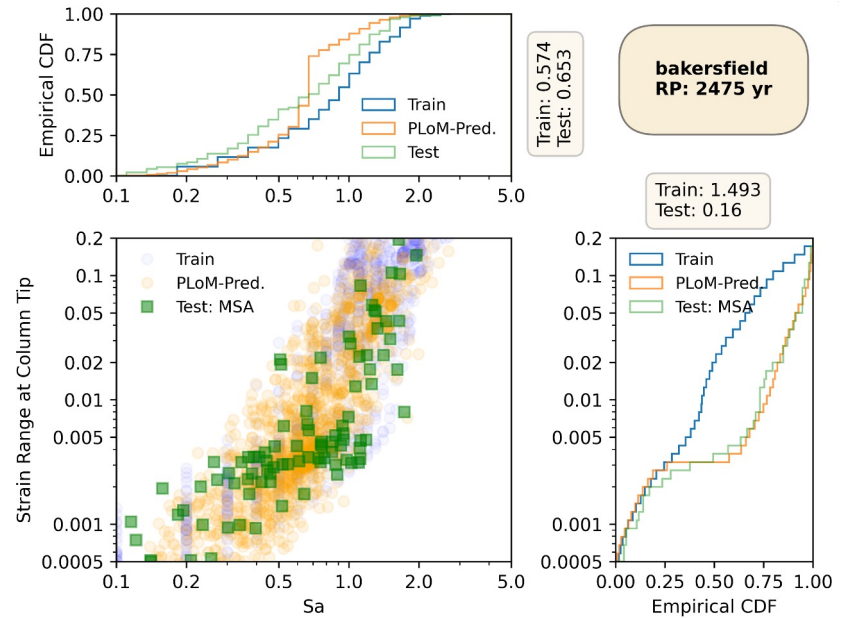
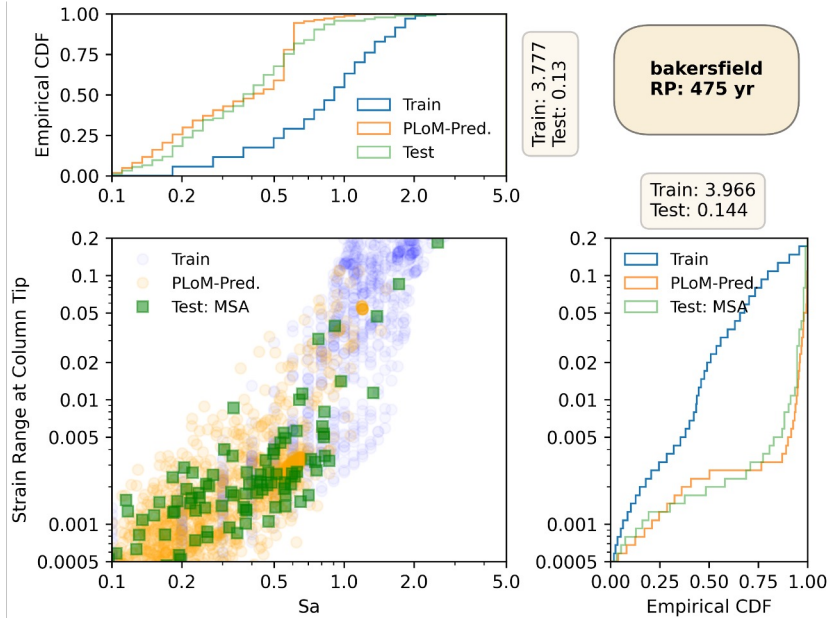


### Response Quantities:

- Curvature (top/bot)
- Strain Range (top/bot)
- Fracture Index (top/bot)
- Collapse

$X_R$

# Bridge Surrogate (PLoM) – Illustrative Results



## Strain range at column tip vs. Sa

*Calculated at Bakersfield SITE for TWO return periods (Sa, SaRatio, and Duration)*

# PLoM - Training/Calibration and Prediction


## Train Data

1. Identify Input and Response Parameters ( $13 = 4X_S + 3X_{GM} + 6X_R$ )
2. Grid Ground Motions (7x7)
3. Perform IDA (600 IDA realizations,  $n \sim 12,000$  analyses)

## PLoM Response Predictions

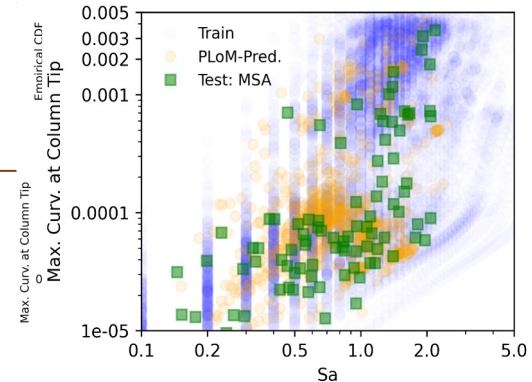
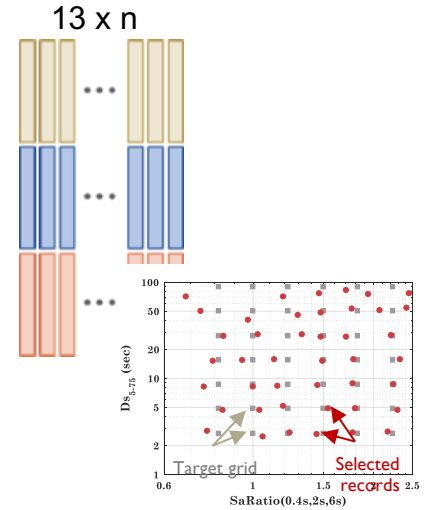
1. Constrain input variables (mean, sigma;  $6 = 4X_S + 3X_{GM}$ )
2. Run PLoM (**hyperparameters**, control parameters)

## Calibrate PLoM Hyperparameters ( $\beta$ , $\epsilon$ )

1. Assemble test data (selected set of MSA data)
2. Assume **hyperparameters**
3. Run PLoM and compare to test 

## Validation

1. Assemble validation data (comprehensive set of MSA data)
2. Run PLoM with calibrated hyperparameters
3. Compare to validation data

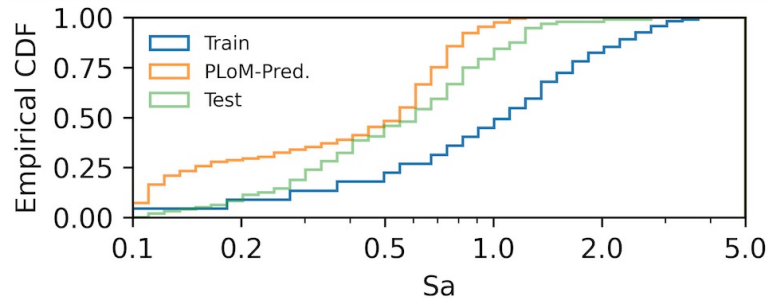




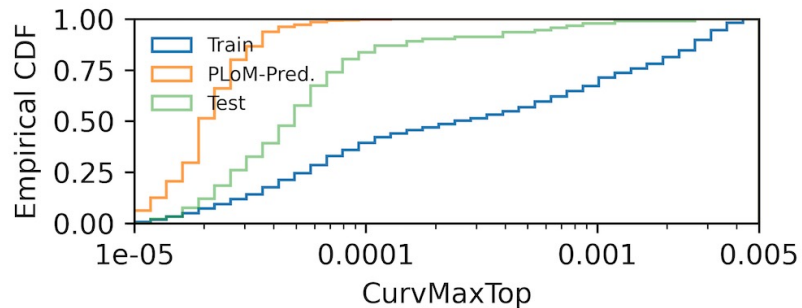
# Importance of Hyperparameters

## Poorly Fit Hyperparameters

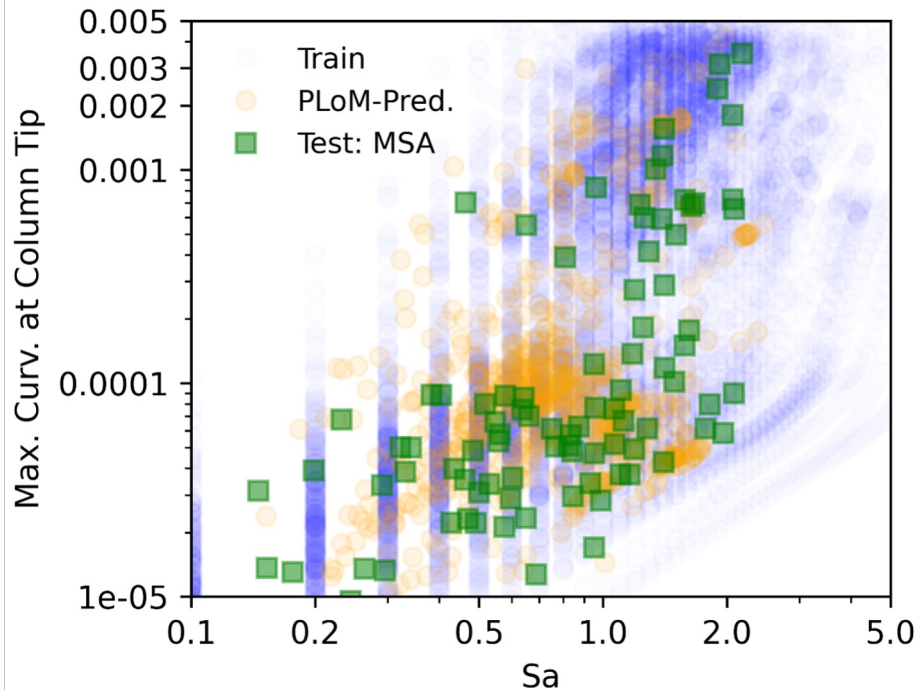
When hyperparameters are not tuned well, the input distributions do not match (example Sa):



When input distributions do not match well, the response distributions do not match well (example CurvMaxTop):



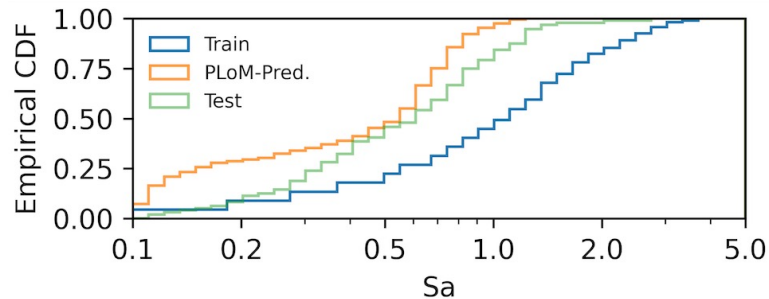
## Optimized Hyperparameters



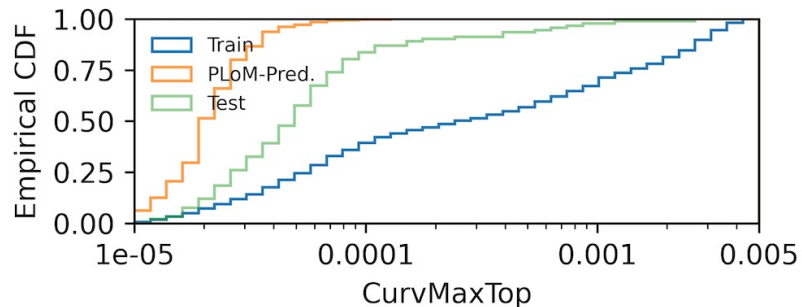
# Importance of Hyperparameters

## Poorly Fit Hyperparameters

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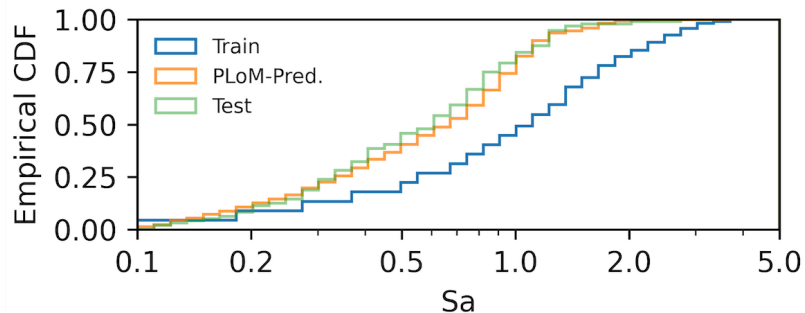


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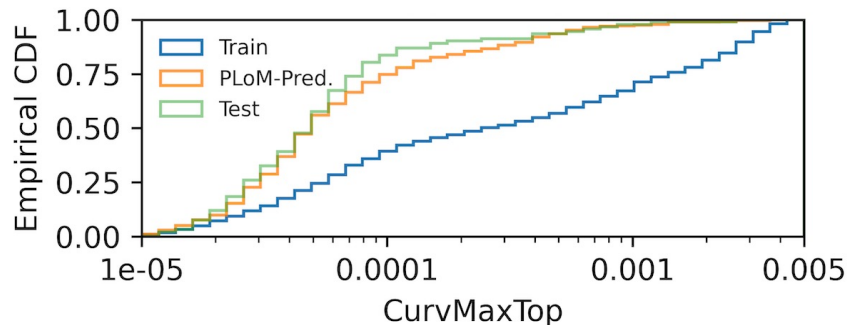


## Optimized Hyperparameters

When hyperparameters are tuned well, the input distributions match (example Sa):



When input distributions match well, the response distributions match much better (example CurvMaxTop):



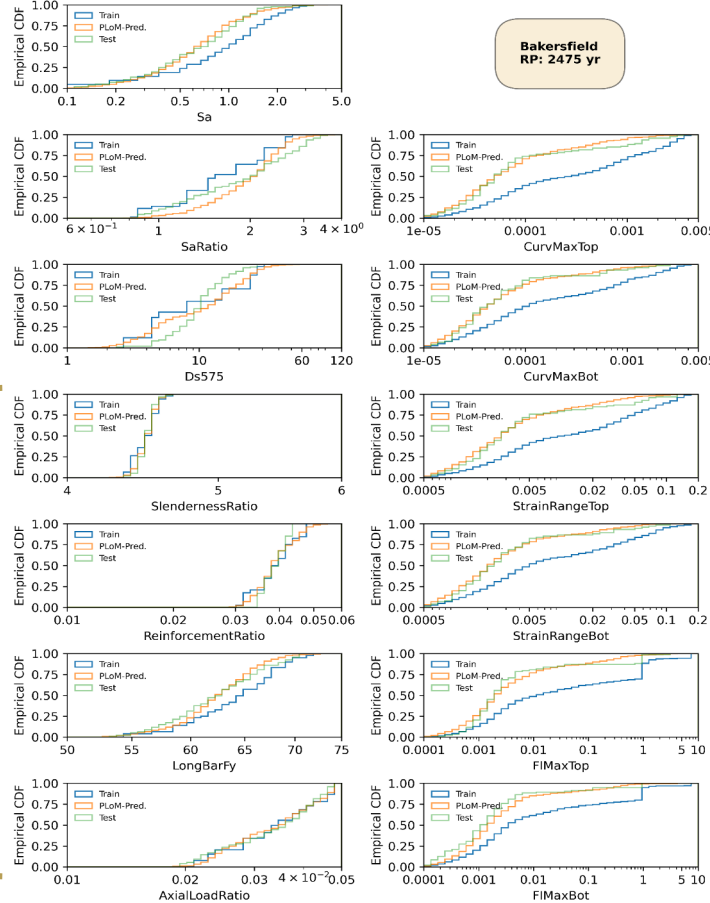
# Validation Studies – Site & Bridge Specific Simulations

## GM Parameters ( $X_{GM}$ ):

- Sa(T1)
- SaRatio
- Duration,  $Ds_{5-75}$

## Model Parameters ( $X_S$ ):

- Pier Slenderness (L/D)
- Axial Load Ratio (P/Po)
- Reinf. Ratio ( $A_s/A_g$ )
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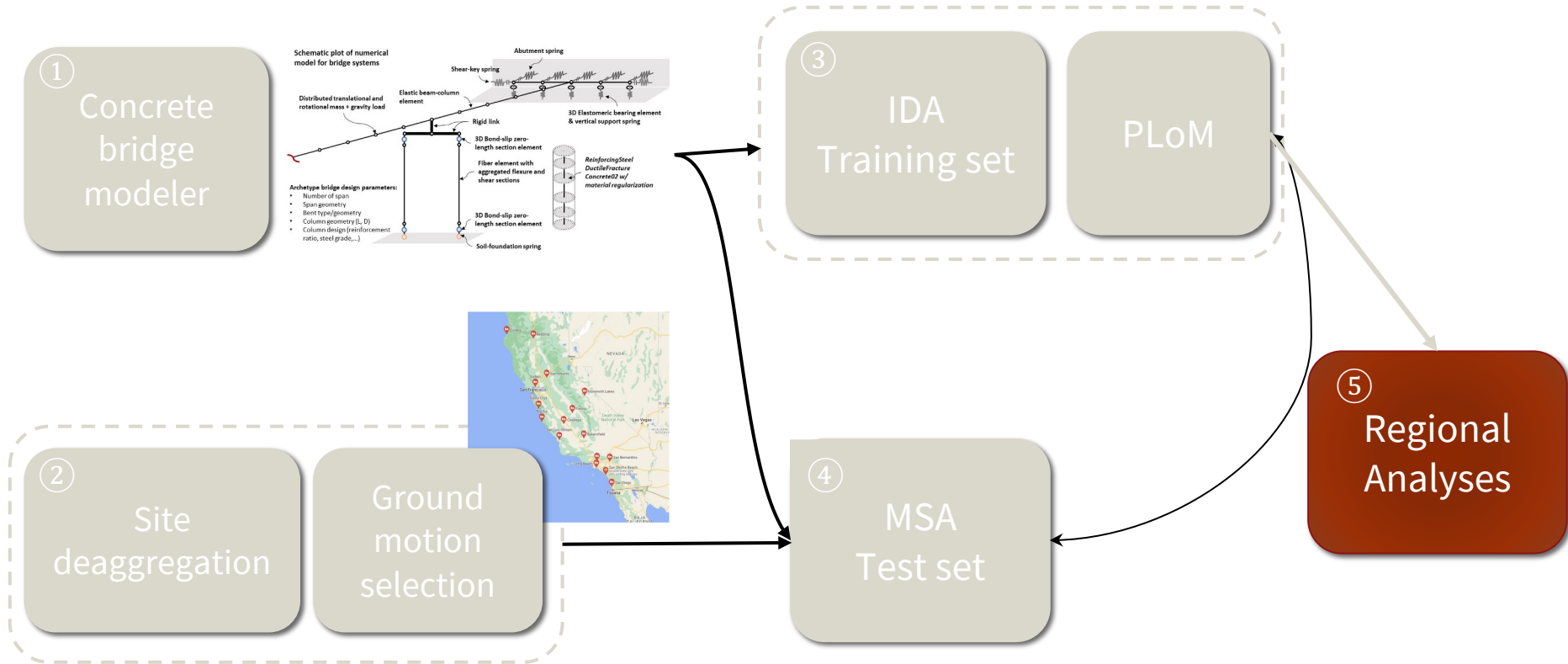
## Response Quantities ( $X_R$ ):

- Curvature (top/bot)
- Strain Range (top/bot)
- Fracture Index (top/bot)
- *Collapse*

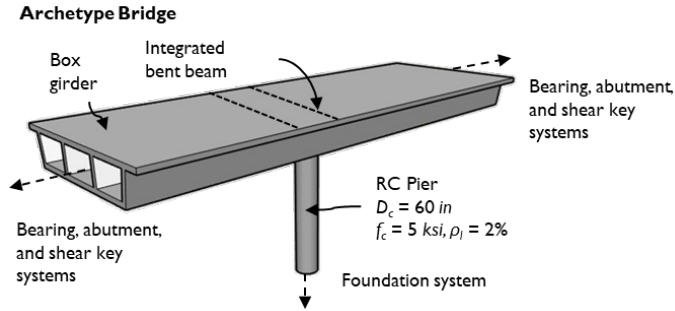
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# Bridge Surrogate Models - PLoM



# Trial Study – R2D



## 12 Bridges - from NBI database:

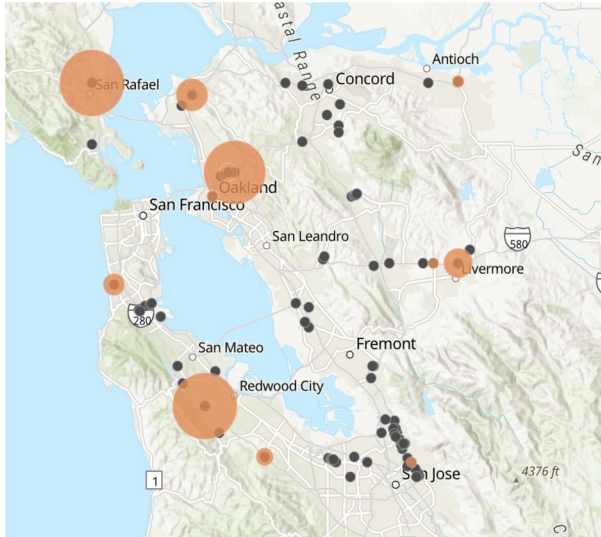
- Single Pier - 2 Span
- Built between 1970 and 1979
- Range of  $V_{s30}$

## Haywired EQ Scenario:

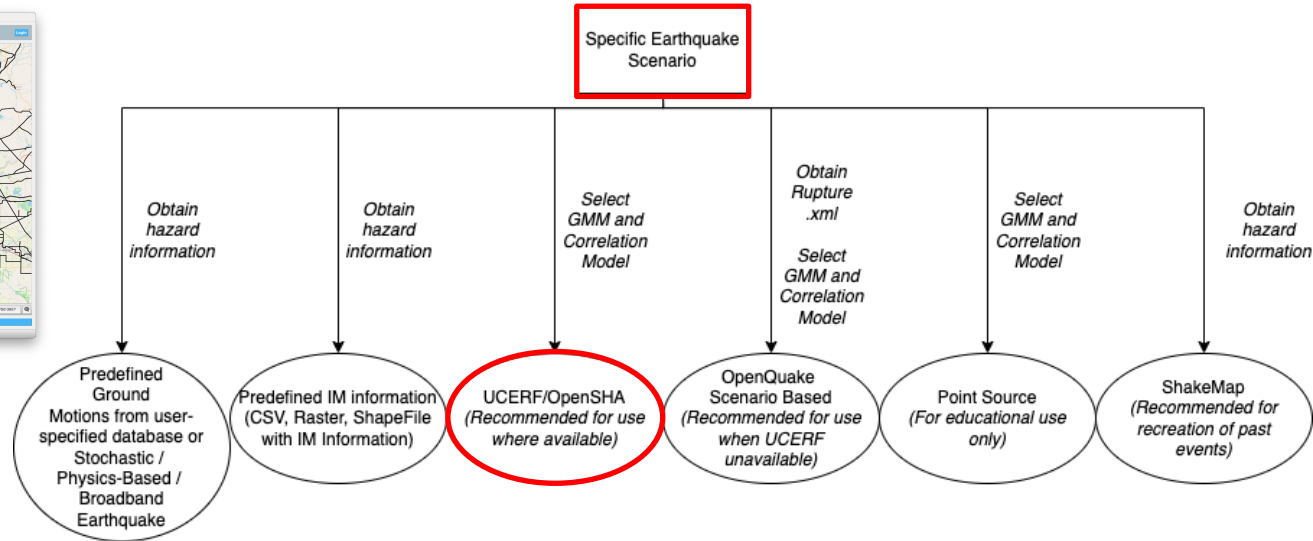
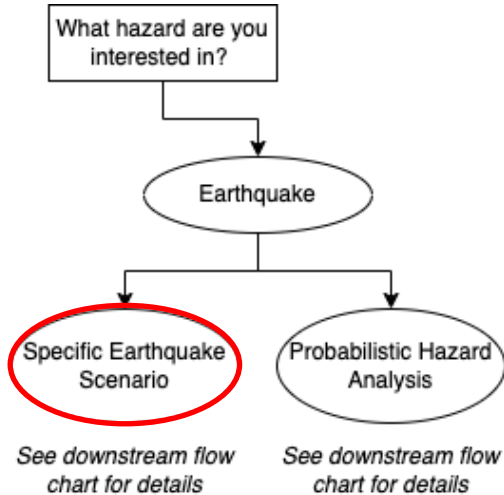
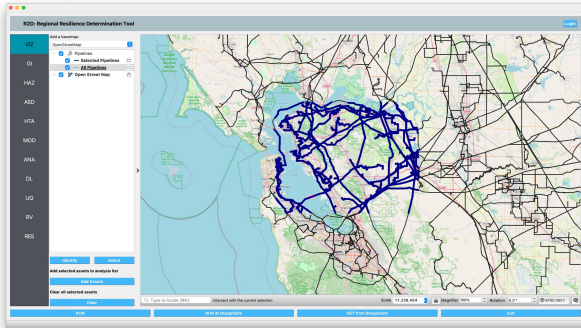
- M7, Hayward-Rodgers Creek

## Response Simulations:

- OpenSees: NLRHA w/site specific GM's
- PLoM: site specific  $S_a$ ,  $S_a \text{ Ratio}$ ,  $D_{s5-75}$



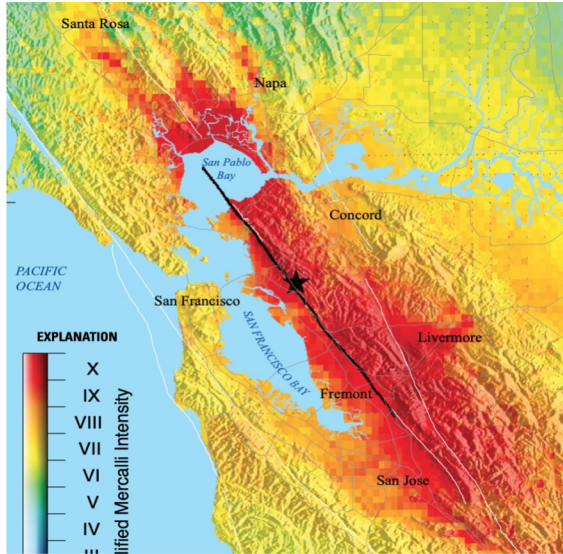
# R2D – Hazard Module



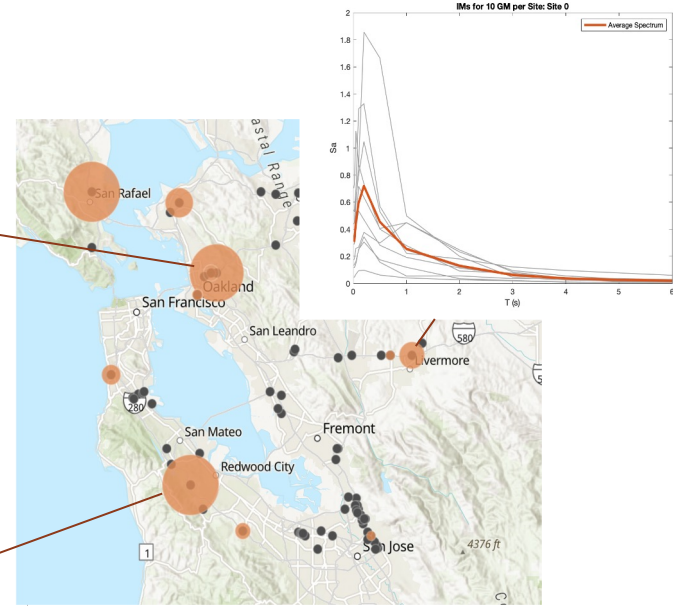
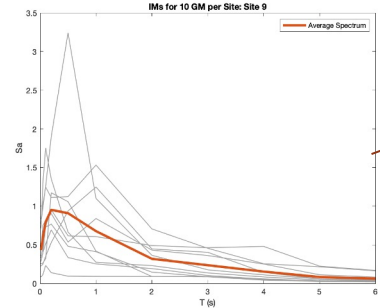
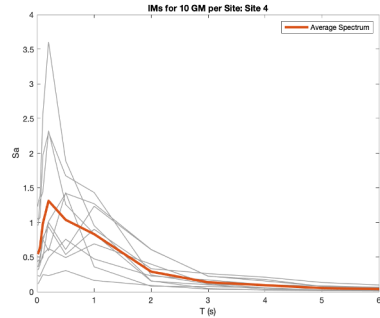
- EQ Scenario (one/more M,R realizations)
- Site Response Spectra (#realizations/scenario)
- Ground Motions (#GM/spectra realization)

# R2D - Earthquake Hazard Tool

HayWired scenario was “Hayward-Rodgers Creek”



HN+HS in the UCERF2 catalogue  
Magnitude 7.05 (Rupture 4, Source 28)

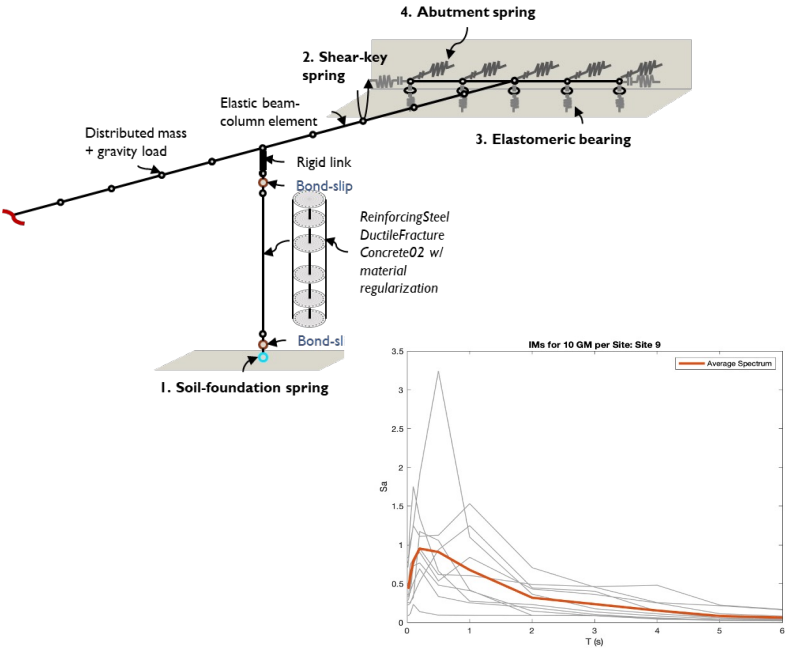


**Ground Motion Spectra Realizations**

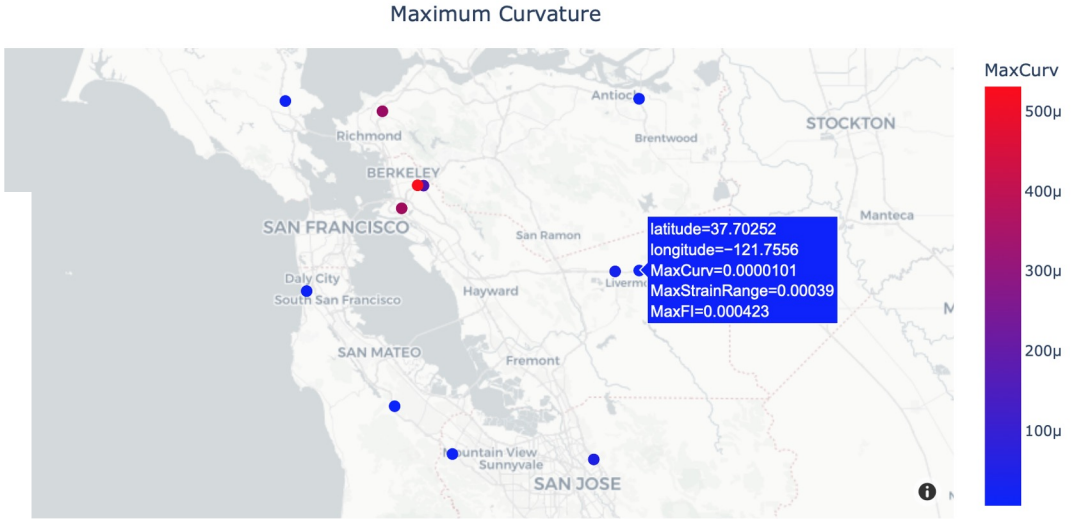
*Including correlations within and between EQ events*  
*- between periods (spectral shape)*  
*- spatial between sites*



# Trial Study – OpenSees Simulations



OpenSees NLRHA  
*X spectra realizations*  
*Y ground motions/spectra*



Bridge Response Data (Curvatures)

# Summary and Next Steps

- In Progress
  - Training and validation of PLoM surrogate model (EE-UQ)
  - Integration of bridge models into regional analysis (R2D)
- Future – short to longer term
  - Seamless integration with bridge inventory data
  - Augment bridge inventory data (e.g., design features)
  - Exercise site/design specific OpenSees, SAF-IDA, PLoM, and GP(?)
  - Streamline surrogate modeling techniques and workflows
    - › *Researchers/Developers -- training/calibration of new models*
    - › *Application Users -- bridge models for transportation network analyses*