



University School for Advanced Studies



EUCENTRE
FOR YOUR SAFETY.

The Different Phenomenology of Dynamic SSI for Buildings, Bridges and Power Plants: Numerical and In-Situ Full-Scale Tests

G. Andreotti and G.M. Calvi

International Workshop on
Large-Scale Shake Table Testing for the Assessment of Soil-Foundation-Structure System Response
for Seismic Safety of DOE Nuclear Facilities



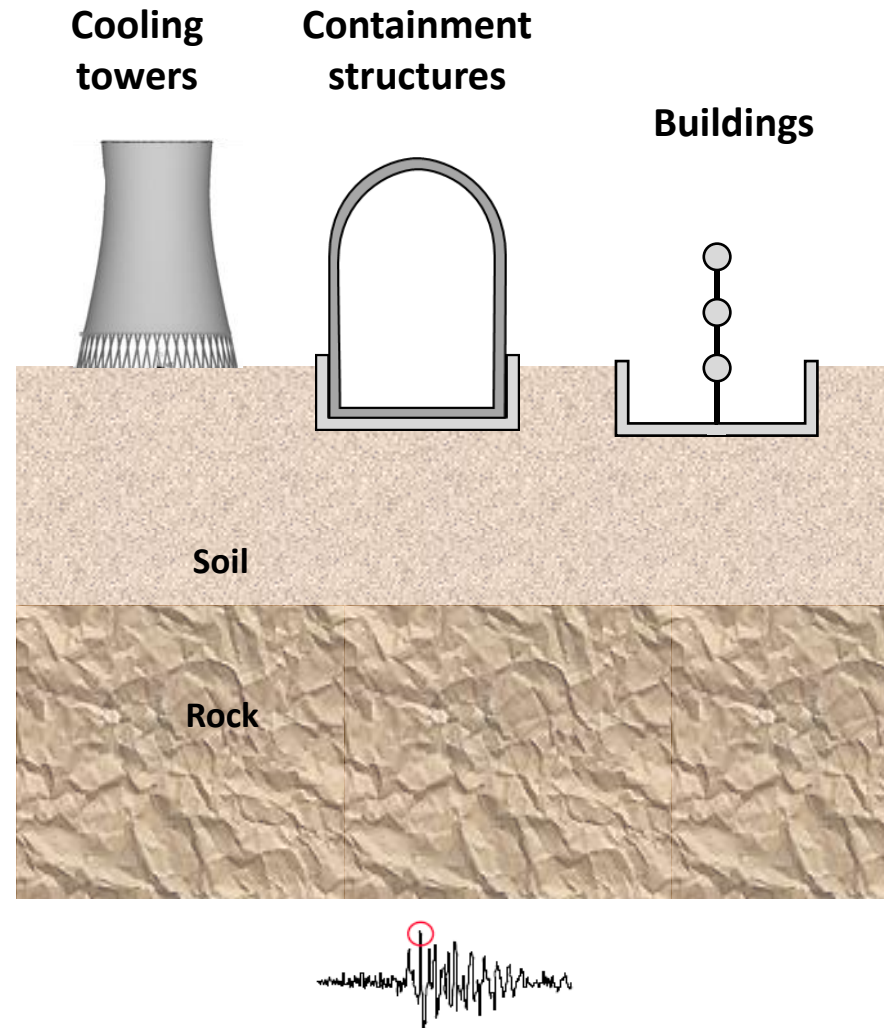
University of Nevada, Reno



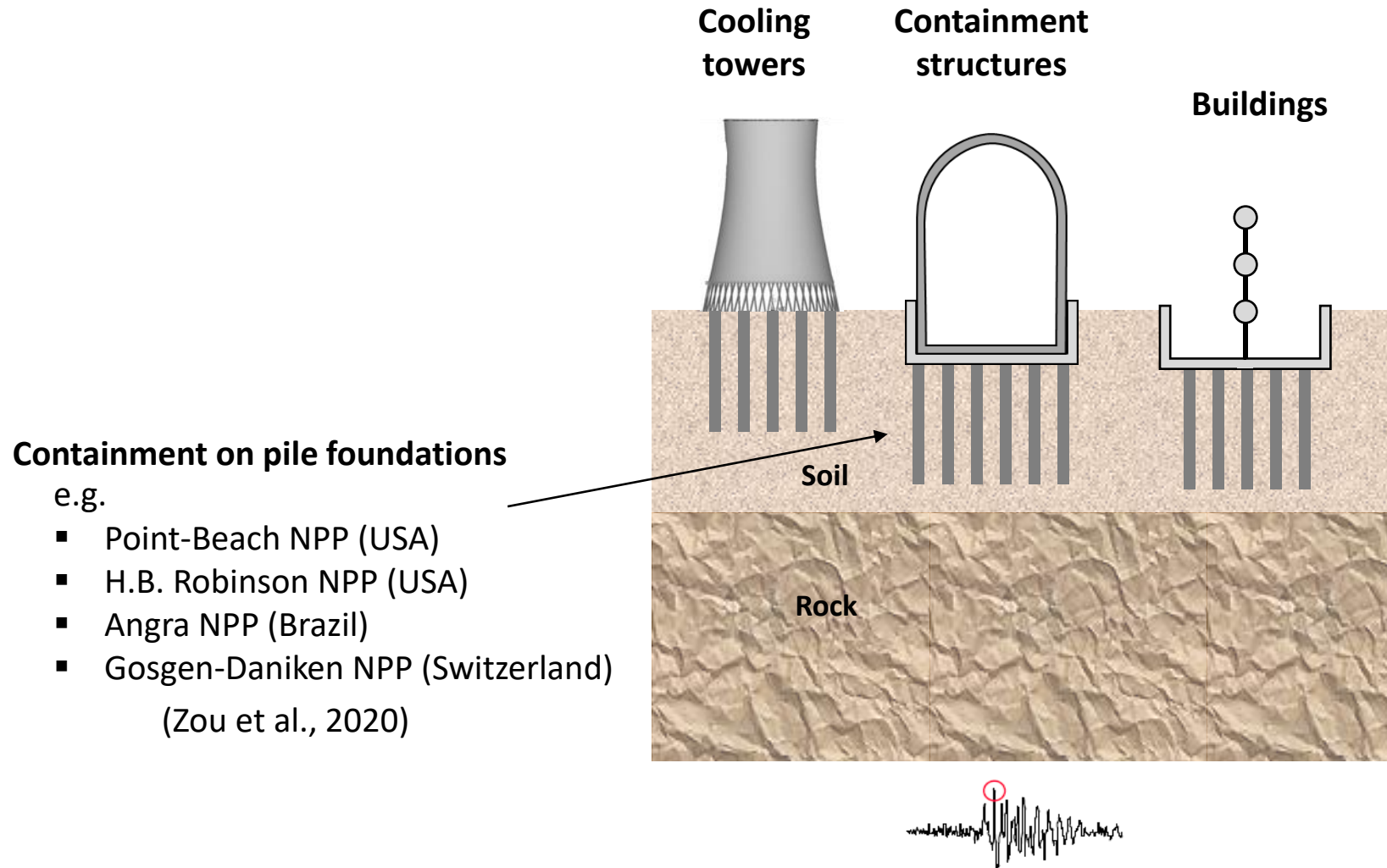
PEER

May 18, 2021

Above-ground structures of NPPs

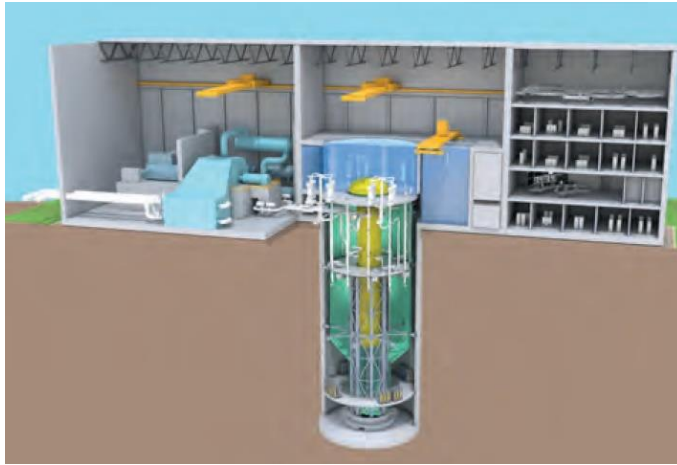


Above-ground structures of NPPs



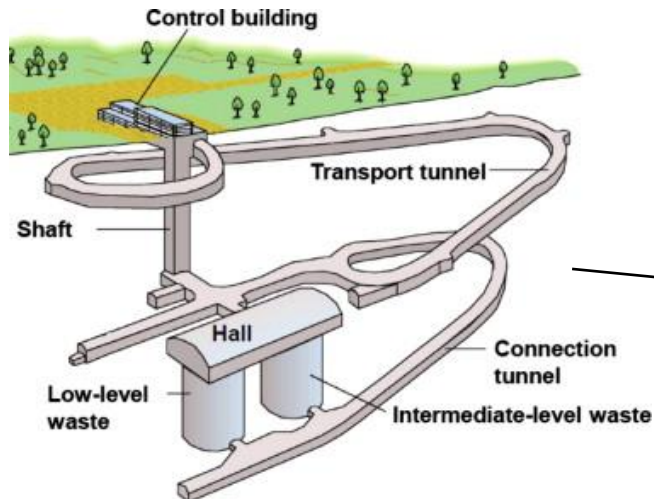
Underground structures of NPPs

Underground reactors

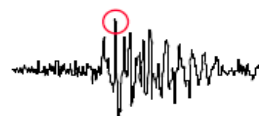
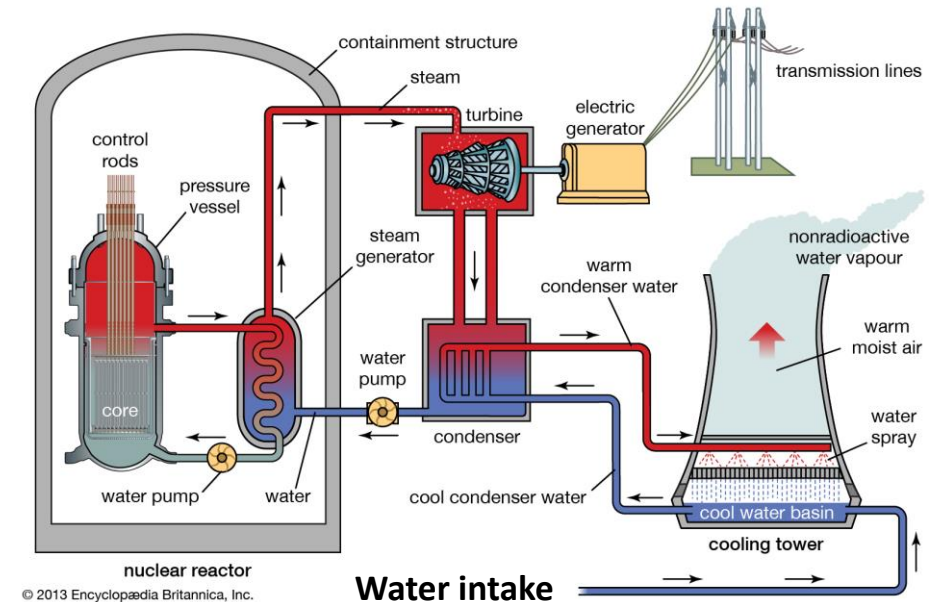
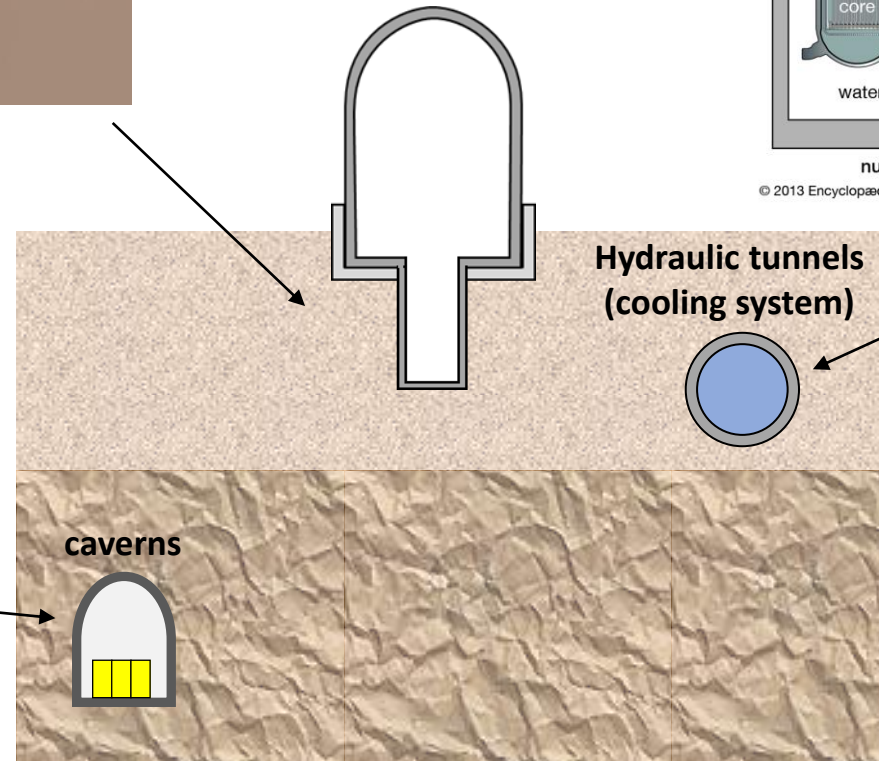


(IAEA, 2020)

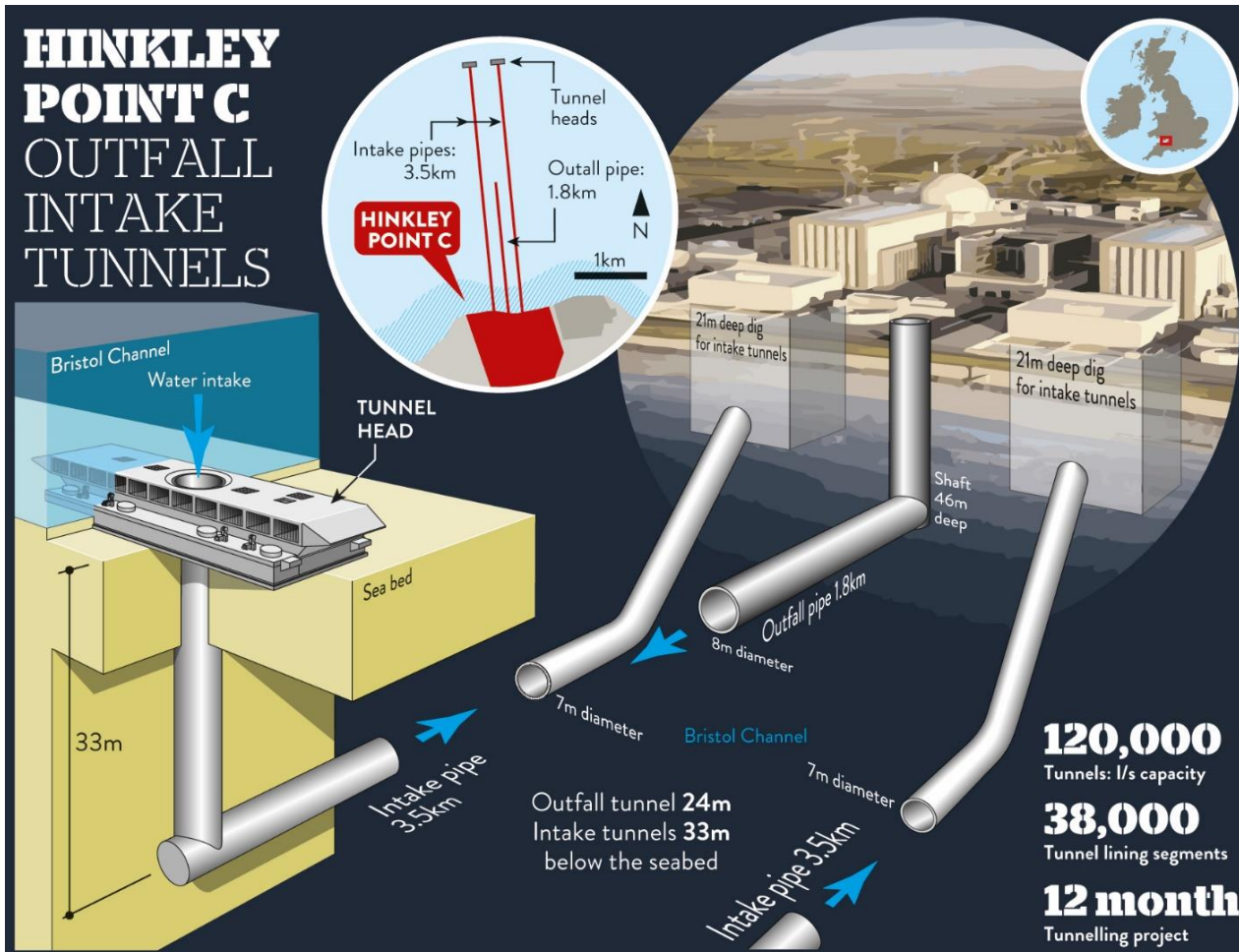
Nuclear waste repositories (e.g. caverns, shafts, tunnels)



(Kari and Puttonen, 2014)



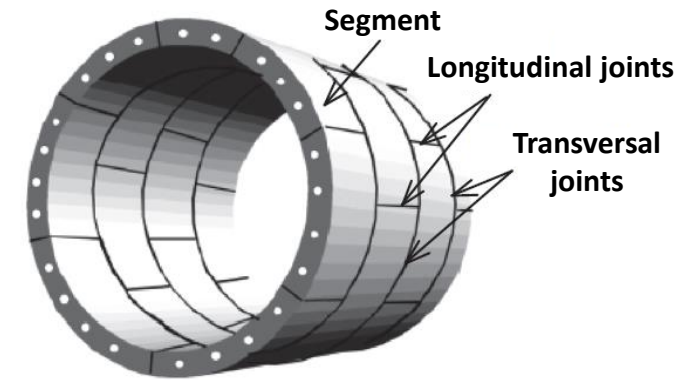
Examples of tunnels and shafts of the cooling system in NPPs



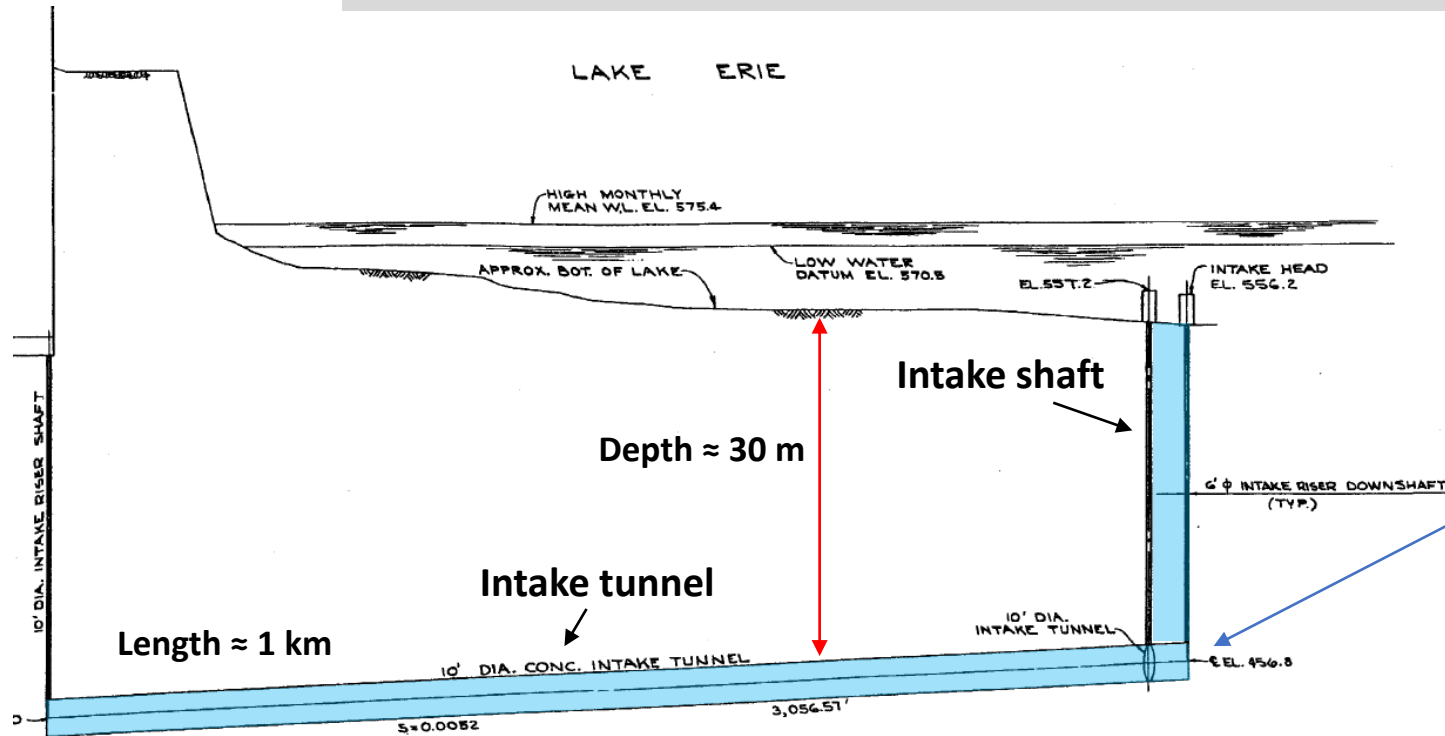
(Kennedy, 2019)

Segmental tunnels (precast segments)

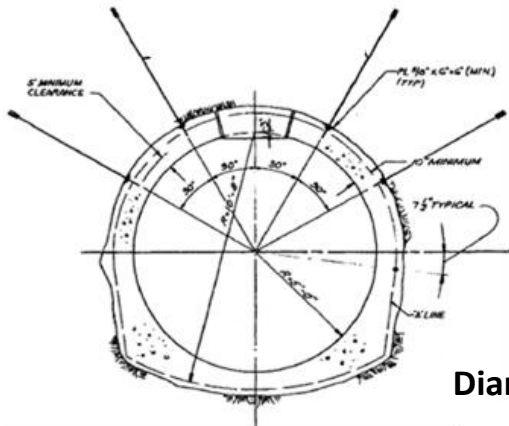
Diameter = 7 m



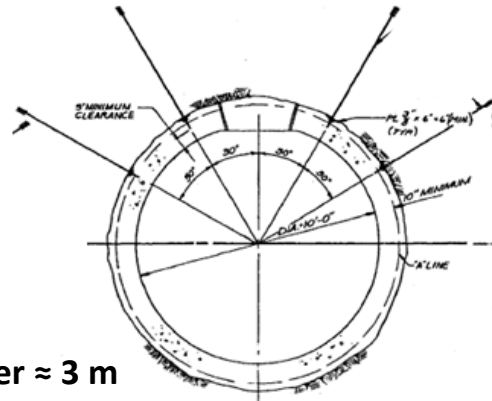
Examples of tunnels and shafts of the cooling system in NPPs



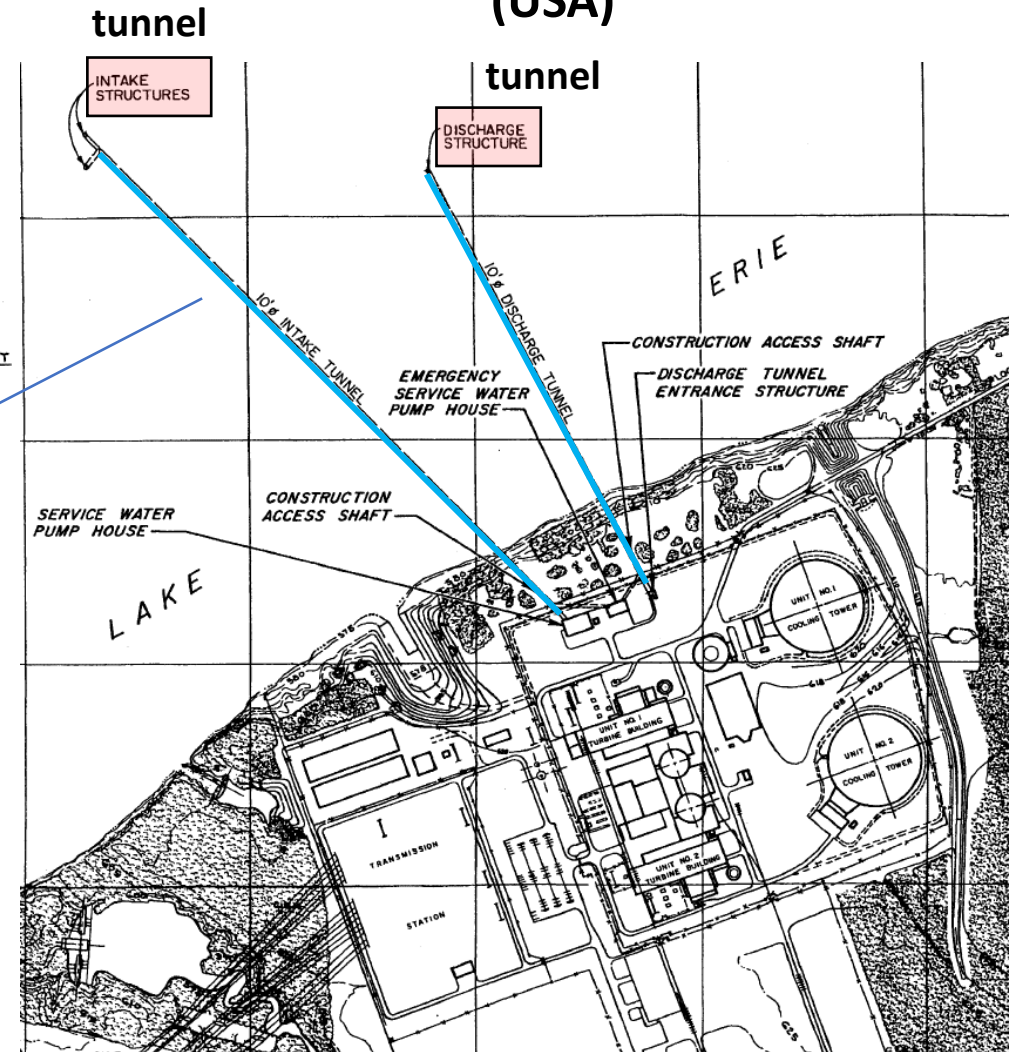
Traditional tunnel



Diameter ≈ 3 m



Perry Nuclear Power Plant (USA)



Nonlinear SSI analysis (Structural nonlinearity)

ASCE 4-16: Seismic Analysis of Safety-Related Nuclear Structures

Chapter 5 - SSI

(5.1 GENERAL REQUIREMENTS): (a) **SSI effects shall be considered for all safety-related nuclear structures.**

Chapter 4 - Analysis of structures

(4.1 GENERAL REQUIREMENTS): (a) The seismic analysis of safety-related structures is **typically** performed by analysis of **linearly elastic** mathematical **models**. **Nonlinear analysis may be performed in some cases**, especially for **beyond design basis calculations** or **evaluation of existing facilities**.



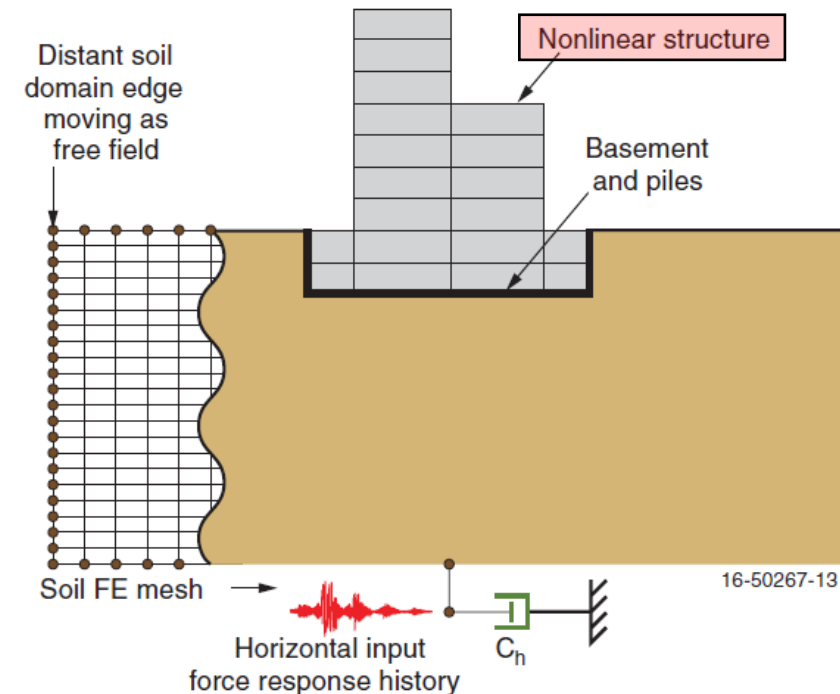
Design peak ground acceleration and recorded peak ground acceleration at NPPs.

	Kashiwazaki-Kariwa, Japan	Fukushima Daiichi, Japan	North Anna, USA
Design value	0.20 g	0.26 g ^a	0.18 g
Recorded value (year)	0.32 g (2007)	0.56 g (2011)	0.26 g (2011)

^a Design basis updated in 2009 to 0.45 g ([The National Diet of Japan, 2012](#)).

(Coleman et al., 2016)

Recorded seismic demand exceeded design value



Nonlinear SSI analysis (Structural nonlinearity)

ASCE 4-16: Seismic Analysis of Safety-Related Nuclear Structures

Chapter 4 - Analysis of structures

(4.1 GENERAL REQUIREMENTS): (a) The seismic analysis of safety-related structures is **typically** performed by analysis of **linearly elastic** mathematical models. **Nonlinear analysis may be performed in some cases**, especially for **beyond design basis calculations** or **evaluation of existing facilities**. (or definition of fragility curves)

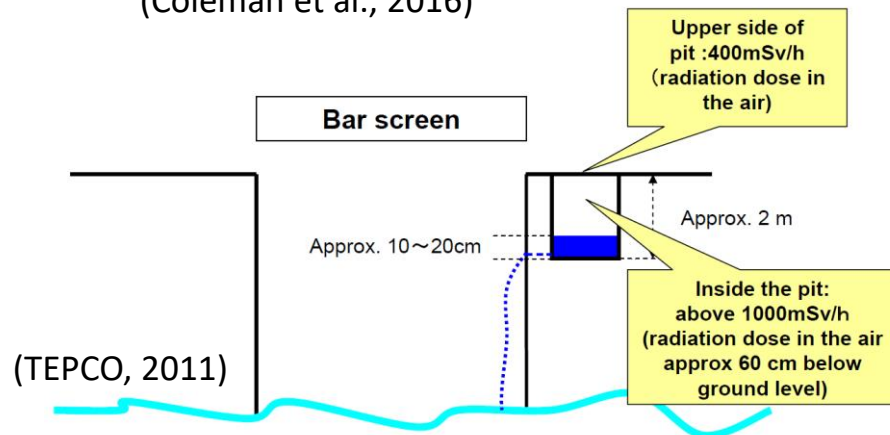


Design peak ground acceleration and recorded peak ground acceleration at NPPs.

	Kashiwazaki-Kariwa, Japan	Fukushima Daiichi, Japan	North Anna, USA
Design value	0.20 g	0.26 g ^a	0.18 g
Recorded value (year)	0.32 g (2007)	0.56 g (2011)	0.26 g (2011)

^a Design basis updated in 2009 to 0.45 g (The National Diet of Japan, 2012).

(Coleman et al., 2016)



Press Releases (TEPCO, 2011)

Press Release (Apr 02,2011)

Out flow of fluid containing radioactive materials to the ocean from areas near intake channel of Fukushima Daiichi Nuclear Power Station Unit 2

Today at around 9:30 am, we detected water containing radiation dose over 1,000 mSv/h in the pit* where supply cables are stored near the intake channel of Unit 2. Furthermore, there was a crack about 20 cm on the concrete lateral of the pit, from where the water in the pit was out flowing. At around 12:20 pm, we reaffirmed the event at the scene.

We have implemented sampling of the water in the pit, together with the seawater in front of the bar screen near the pit. These samples were sent to Fukushima Daini Nuclear Power Station for analysis.

In addition to seawater sampling conducted in the coastal areas of Fukushima Daiichi/Daini Nuclear Power Station (sampling conducted at 4 points), we have initiated additional seawater sampling at 3 points in the areas 15 km offshore from the relevant power stations. Taking into account the result of these monitoring, we are intending to conduct a comprehensive assessment.

Currently, we are preparing to block up the leakage by injecting concrete to the crack. Moreover, we will investigate the influx route of contaminated water in the pit and implement necessary measures to prevent such influx.

*pit: a shaft made of concrete

Underground structures were damaged

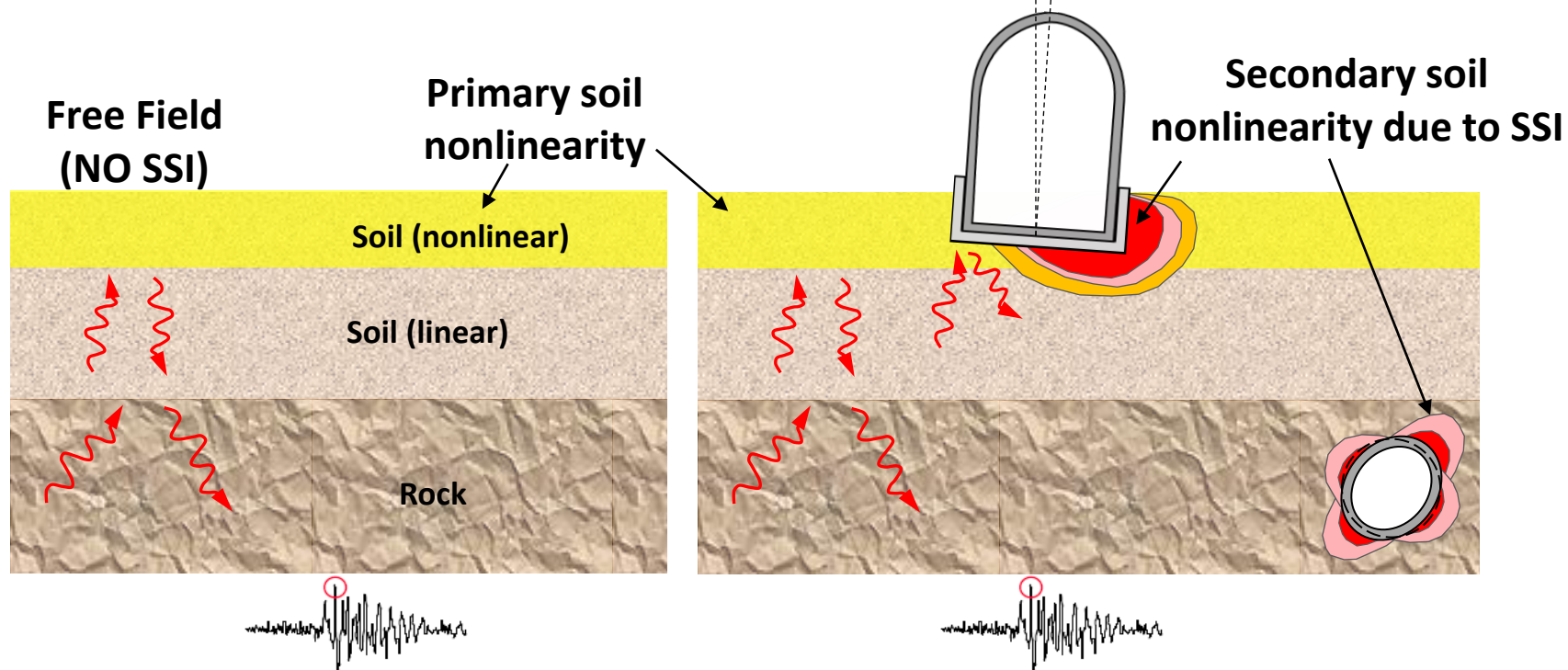


Often designed to remain elastic

Nonlinear SSI analysis (Soil nonlinearity)

ASCE 4-16: Seismic Analysis of Safety-Related Nuclear Structures

Chapter 5 – SSI: Nonlinear Behavior of Soil: **Primary and secondary soil nonlinearity**



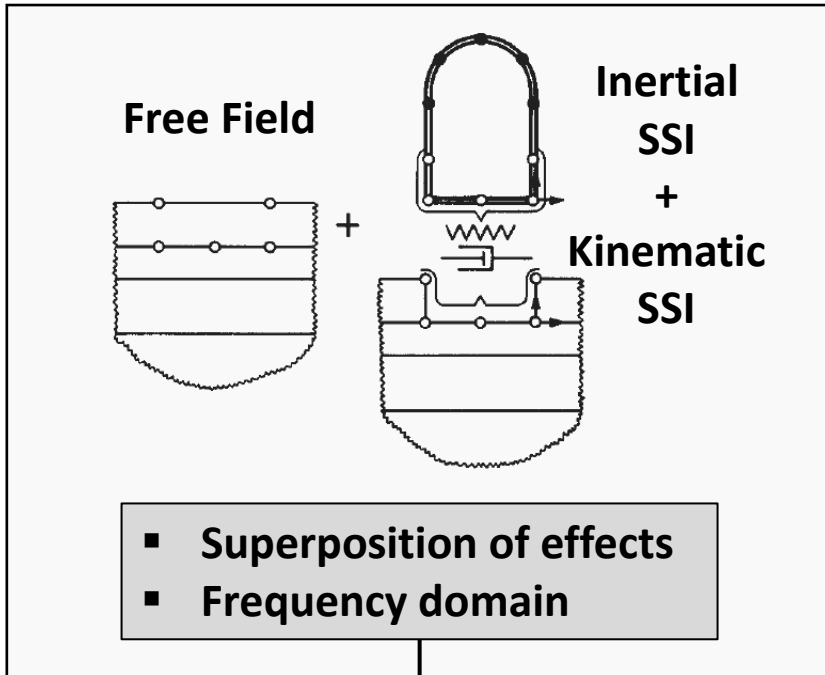
5.1.4 (d) **Primary nonlinearities shall be considered** in the SSI analysis. **Secondary nonlinearities**, including local soil nonlinear behavior in the vicinity of the soil-structure interface, **need not be considered**, except for the calculation of seismic soil pressure.

COMMENTARY: C5.1.4 Nonlinear Behavior of Soil

(...) **rigorous nonlinear analysis** of a typical nuclear structure requires a fully three-dimensional model and an appropriate set of constitutive equations for soil. These requirements **are currently beyond the state of the art for design**.

Solution of dynamic SSI: linear vs nonlinear

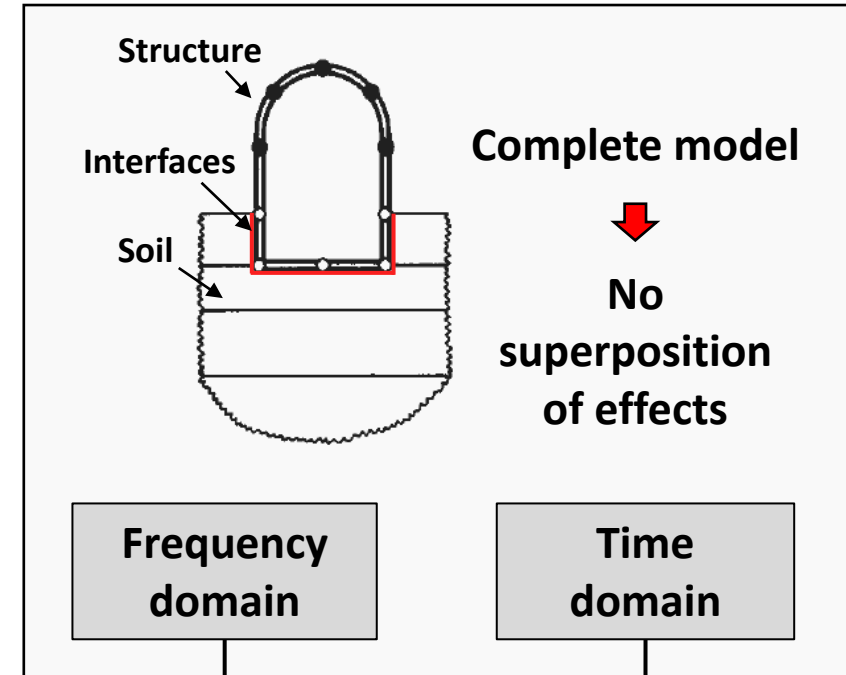
SUBSTRUCTURE METHOD



**Linear analysis
(equivalent-linear)**

**Problems to capture
moderate-to-high nonlinearities**

DIRECT METHOD



**Fully nonlinear
dynamic analysis**

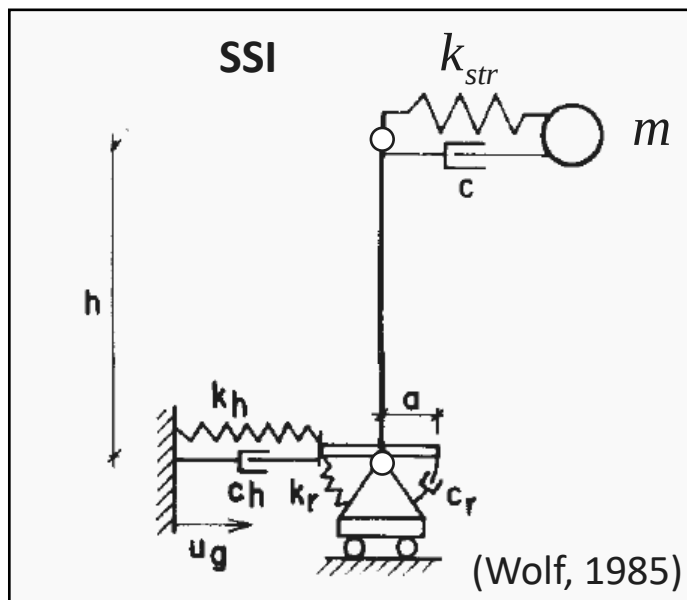
**NL structure
NL soil
NL interfaces**

NLSSI

Some questions

Soil-structure stiffness ratio $\frac{K_{\text{struct}}}{K_{\text{soil}}}$  One of the main variables of SSI

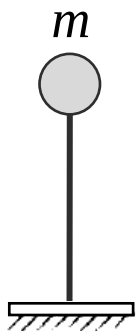
Simple models for above-ground structures



Fixed base

$$\omega_{FixB} = \sqrt{\frac{k_{str}}{m}}$$

$$\xi_{str}$$



Equivalent SSI

$$\omega_{SSI} = \sqrt{\frac{k_{eq}}{m}}$$

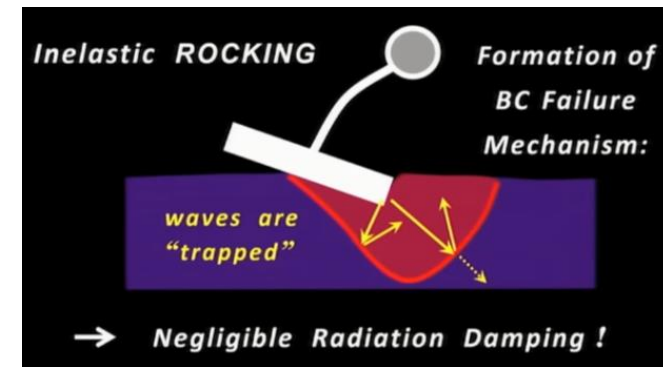
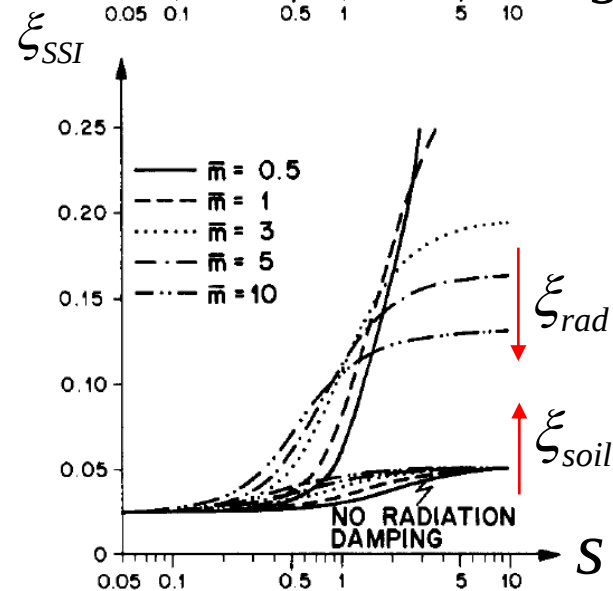
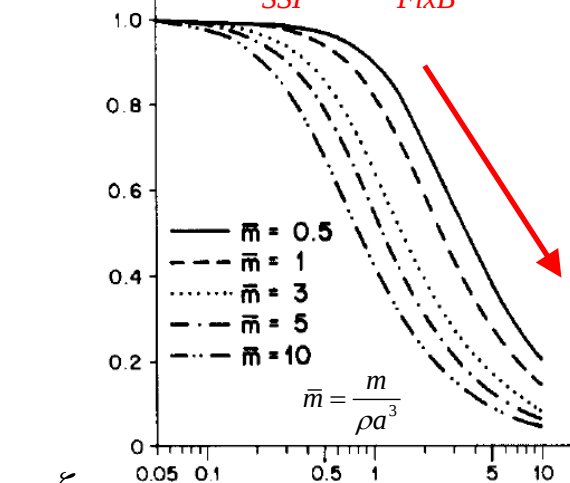
$$\xi_{SSI} = \xi_{str} + \xi_{soil} + \xi_{rad}$$

$$\frac{1}{k_{eq}} = \frac{1}{k_{str}} + \frac{1}{k_h} + \frac{h^2}{k_r}$$

Reference model → Fixed base

$\frac{\omega_{SSI}}{\omega_{FixB}}$

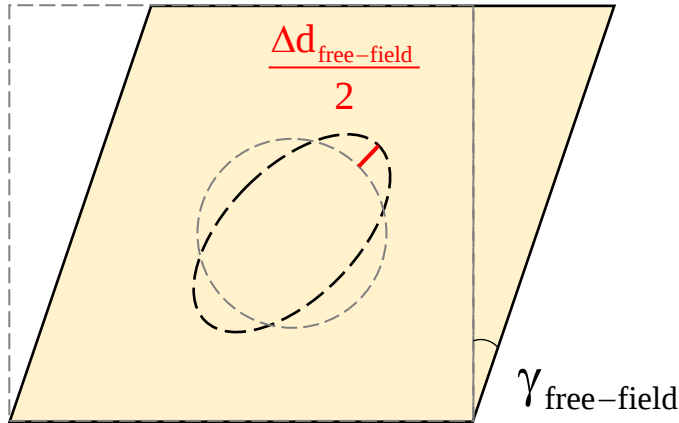
Fixed Base (NO SSI)
 $\omega_{SSI} = \omega_{FixB}$



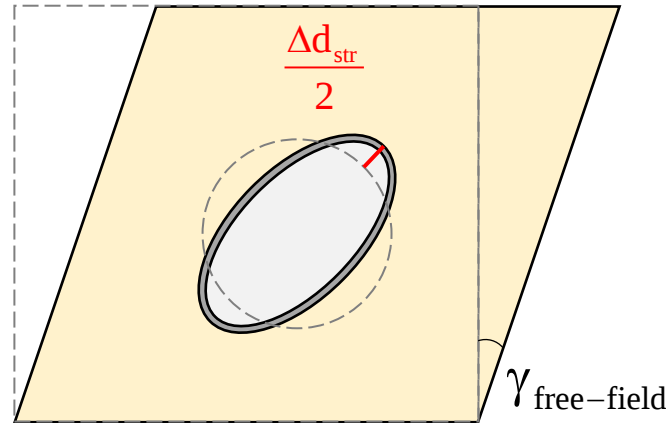
(Prof. Gazetas, Rankine lecture 2019)

Simple models for underground structures

Free-field



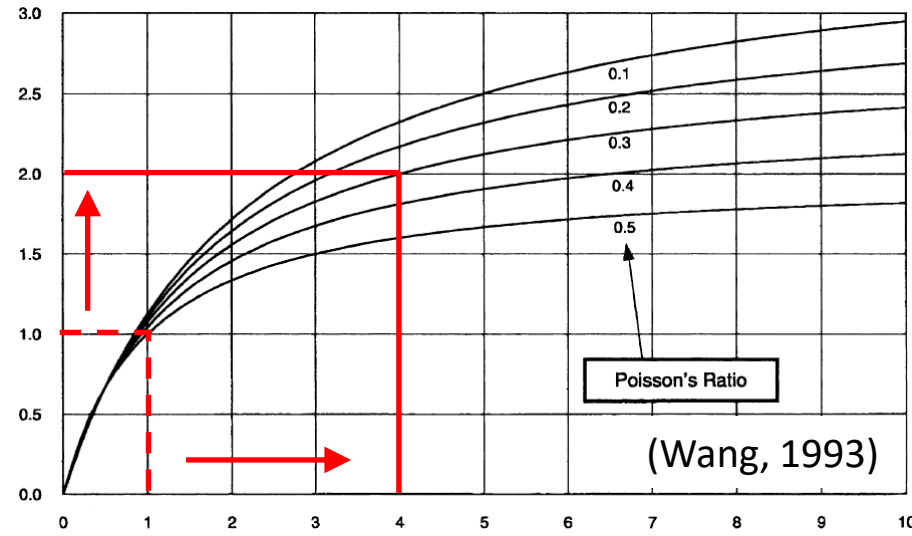
Presence of the structure



Reference model → Free-field
(no structure)

Displacement
structural demand

$$\frac{\Delta d_{\text{str}}}{\Delta d_{\text{free-field}}}$$



Flexibility ratio

$$F = \frac{E_{\text{soil}} \cdot (1 - \nu_{\text{str}}^2) r^3}{(1 + \nu_{\text{soil}}) \cdot 6E_{\text{str}} I_{\text{str}}} = \frac{K_{\text{soil}}}{K_{\text{str}}}$$

Stiffness contrast

Could not be constant
during earthquakes

Evolution of soil and
structural nonlinearity

Some questions

Soil-structure stiffness ratio $\frac{K_{\text{struct}}}{K_{\text{soil}}}$ ➡ One of the main variables of SSI

NLSSI implies nonlinearity of the whole system (structure + soil) ➡ Stiffness ratio is not constant

- What happens to the whole system with the evolution of structural damage and soil nonlinearity?

- Does structural nonlinearities affect soil nonlinearity?

- Does soil properties affect structural capacity?

YES
numerical evidence

Two case studies:

1) Tunnels ➡ 2D fully nonlinear time history analysis

2) CIDH bridge columns ➡ 3D detailed modelling with experimental benchmark

- Is the gap between geotechnical and structural engineers detrimental to solve NLSSI problems?

1) Fragility analysis of underground tunnels: fully nonlinear SSI

$M_w=7.9$

Epicentral distance ≈ 14.2 Km

2008 Wenchuan earthquake (China)



(Li, 2012)

$M_w=6.9$

Epicentral distance < 15 Km

1980 Irpinia earthquake (Italy)



(Cotecchia, 1986)

$M_w=7.4$

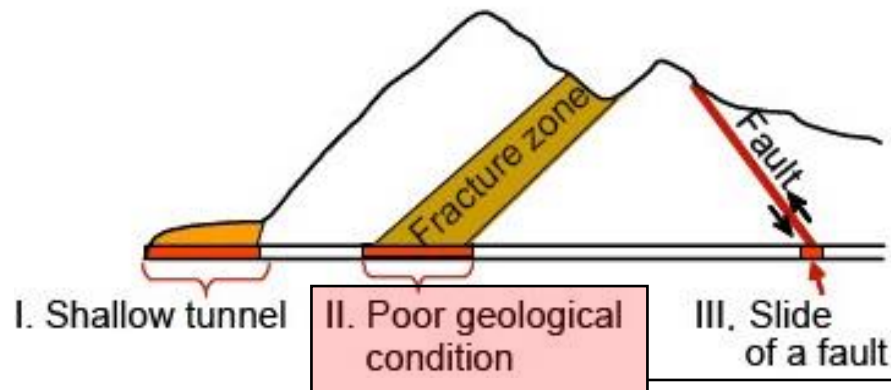
Epicentral distance < 32 Km

1990 Manjil earthquake (Iran)



(Wieland, 2011)

Critical scenarios for tunnels



Early objective

Definition of numerical fragility curves considering variability of seismic input, structural and geotechnical nonlinearities, depth of tunnel.

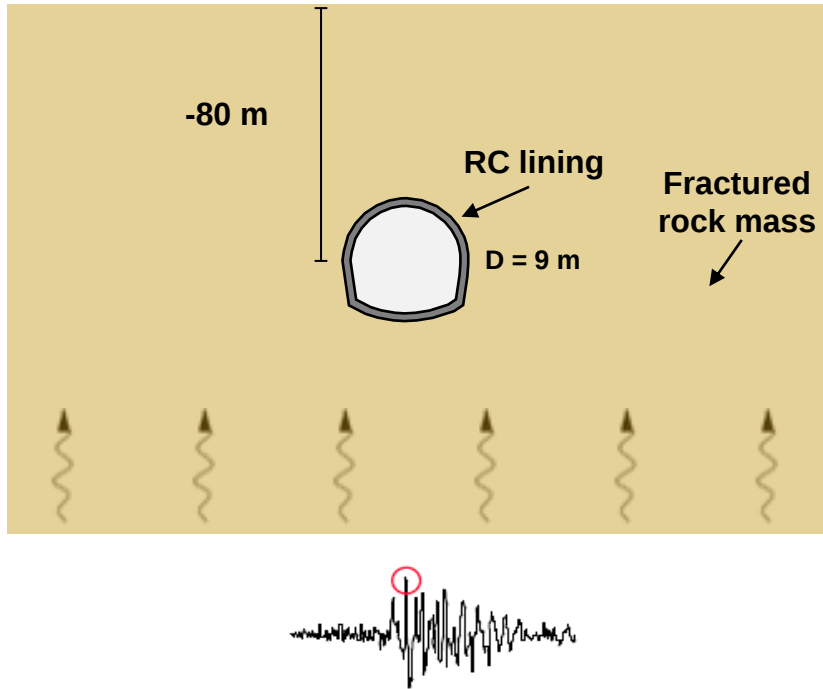
(see Andreotti and Lai, 2017a, 2017b, 2019)



From the suite of analysis: investigation on NLSSI effects

Fragility analysis of underground tunnels: fully nonlinear SSI

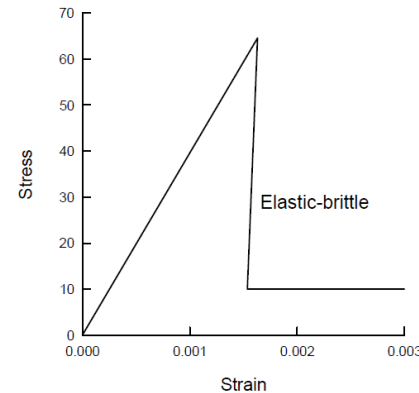
Selected scenario to evaluate NLSSI



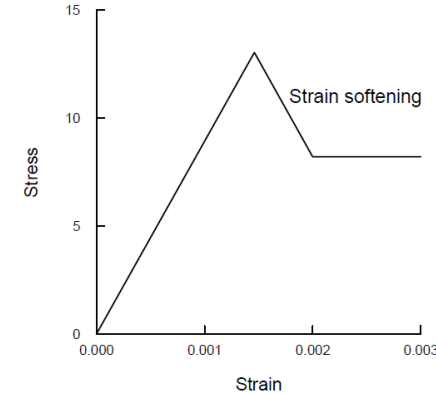
Rock mass parameters

GSI	E	ν	ϕ	dilatancy	c	γ	K_0
	[MPa]		[°]	[°]	[MPa]	[kN/m ³]	
25	1100	0.3	22	0	0.5	24	0.6

Very good quality (GSI=75)

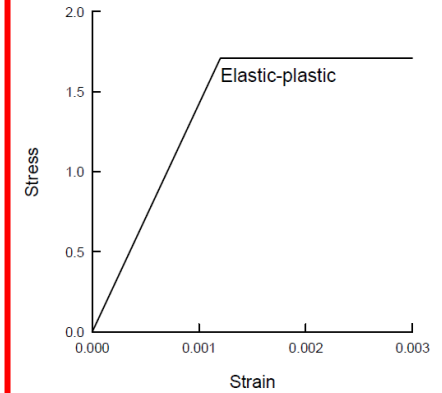


Average quality (GSI=50)



Hoek and Brown (1997)

Very poor (GSI=30)



Mohr-Coulomb model

RC Tunnel lining

Type	Reinforcement			Concrete			Steel	
Section	Thickness	Steel rebars	Stirrups	E_c	f_c	f_t	E_s	f_s
	[m]	[kg/m ³]	[cm ²]	[MPa]	[MPa]	[MPa]	[MPa]	[MPa]
S1	0.7	50	14.13	33000	25.5	2.55	210000	450
S2	1	80	14.13					

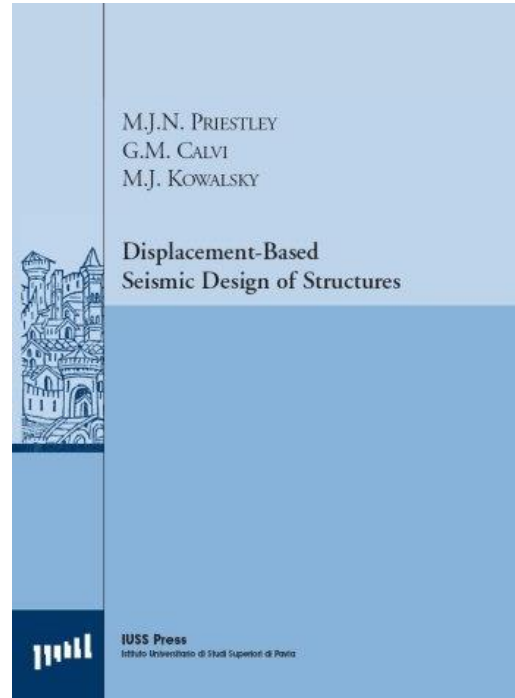
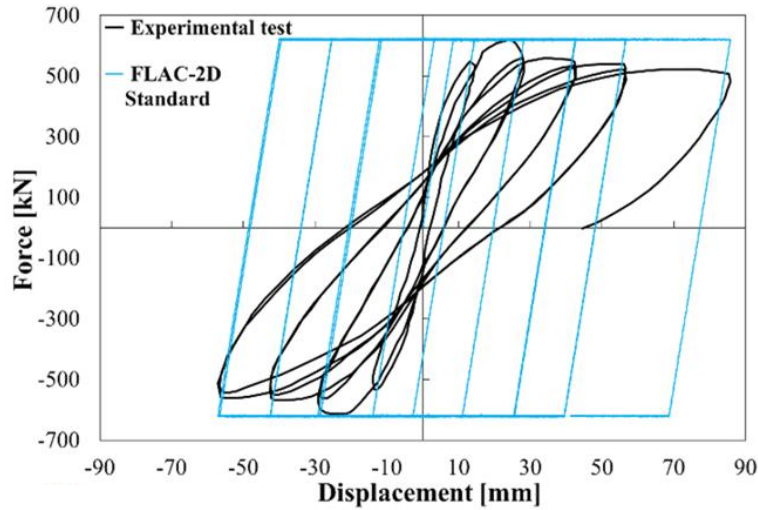
FLAC 2D



Problems to model cyclic nonlinear behaviour of RC structures

Modelling nonlinear cyclic behaviour of structural elements and damage assessment

FLAC 2D Standard Model

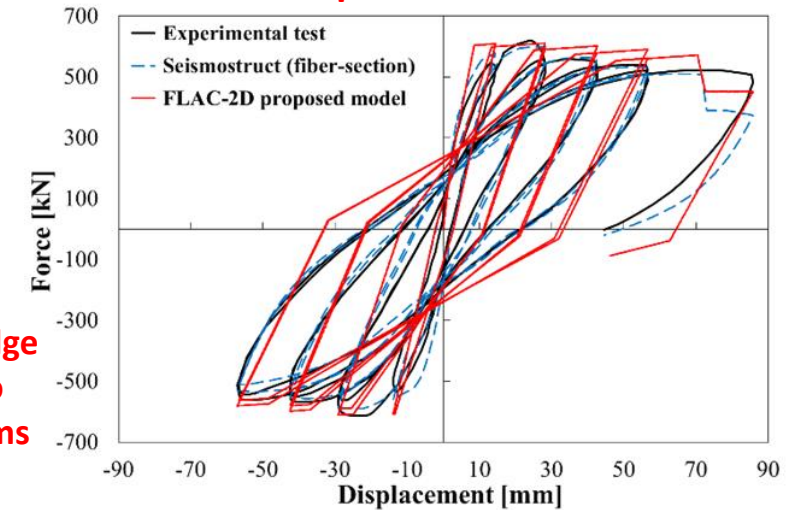


Application of
concepts

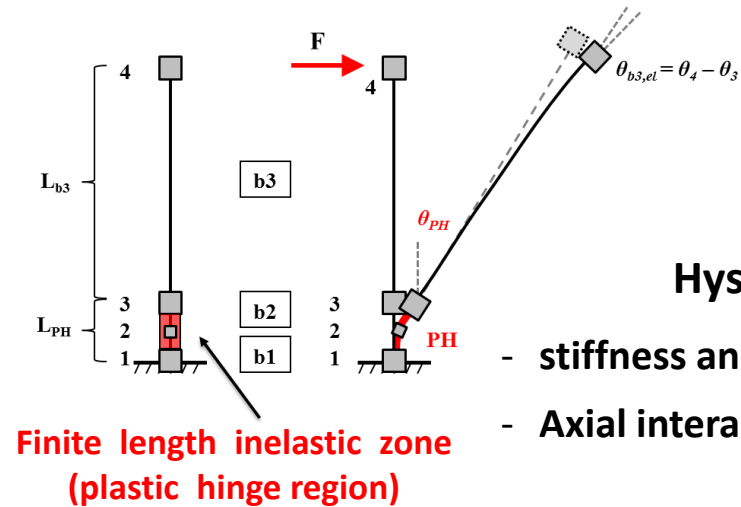
Transfer of knowledge
from structural to
geotechnical systems



Implemented Model



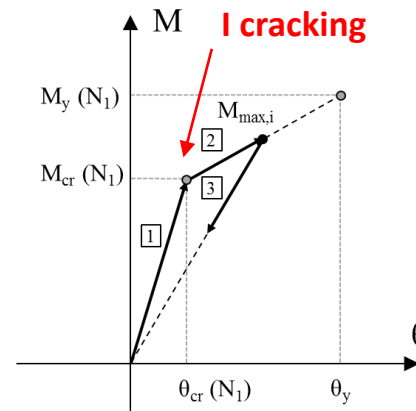
Elementary part



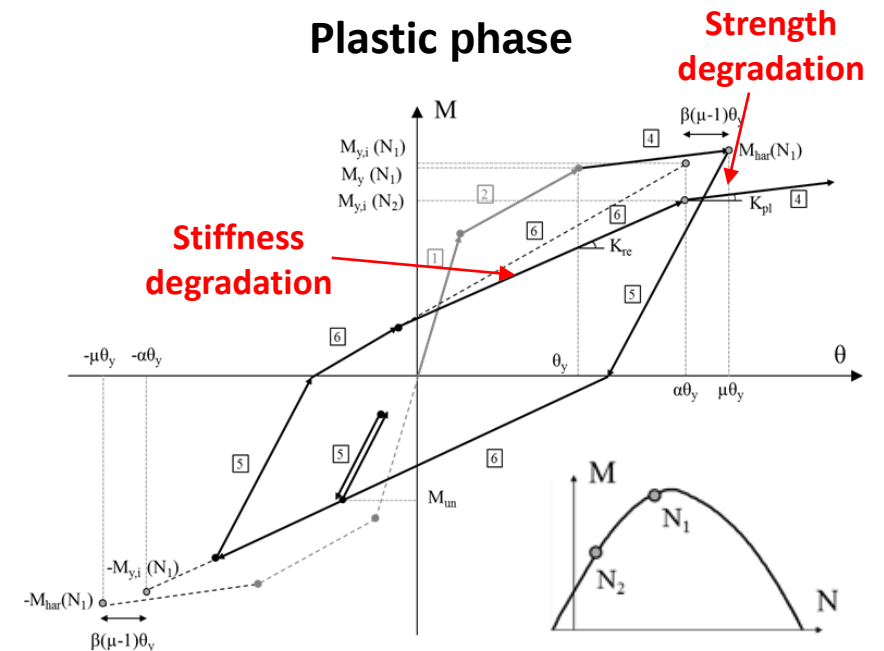
Hysteretic law

- stiffness and strength degradation
- Axial interaction (M-N)

Bi-linear elastic phase



Plastic phase



FLAC 2D numerical model

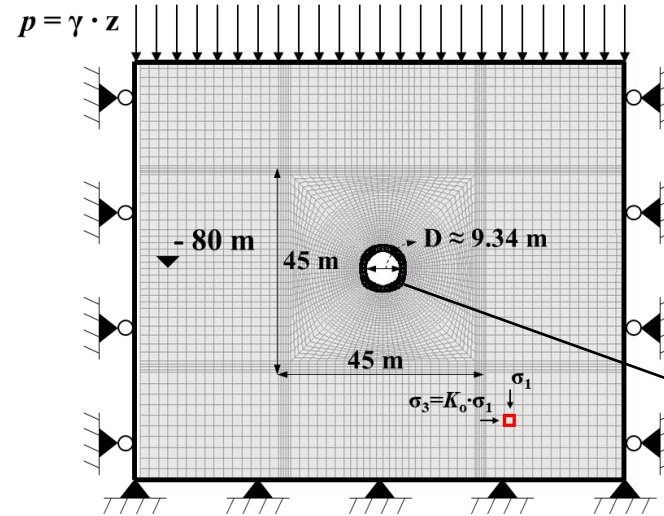
Multi-step
static analysis



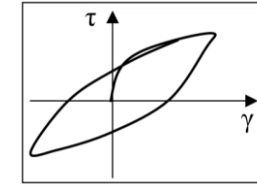
Initial
conditions



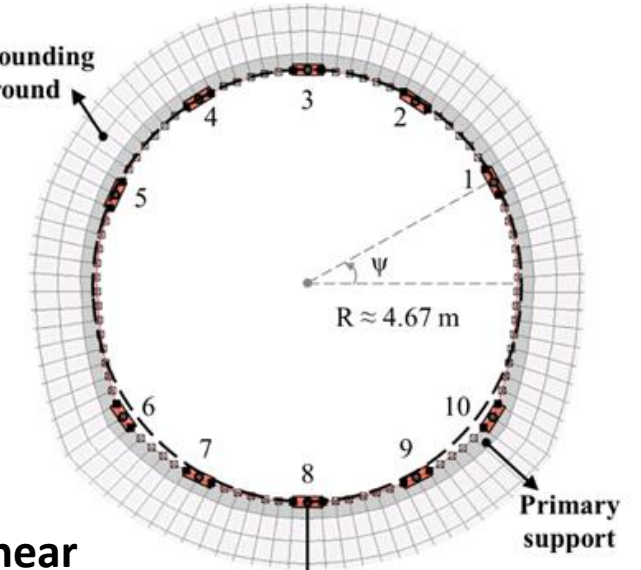
Nonlinear time
history analysis



Nonlinear soil

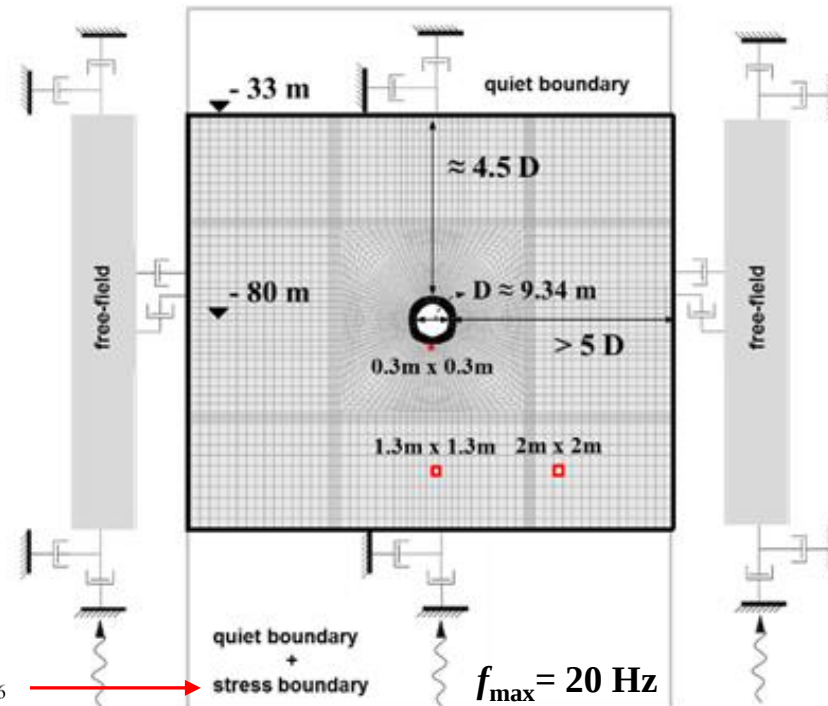
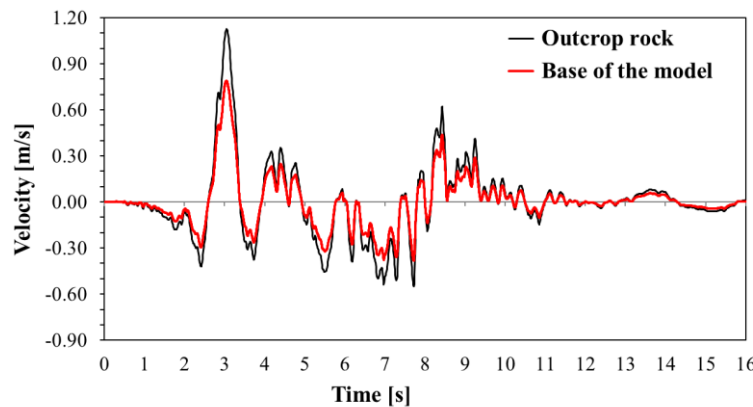
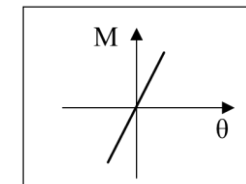
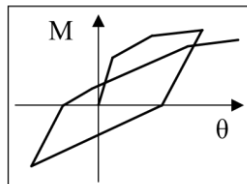


Surrounding
ground



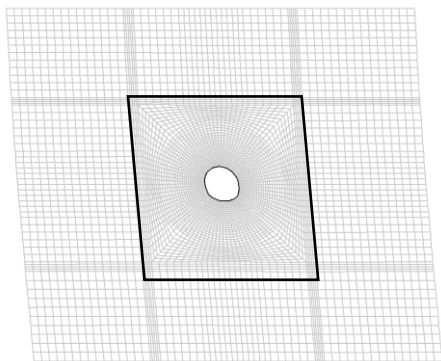
Nonlinear
structure

elastic beams
($L \approx 0.3$ m)

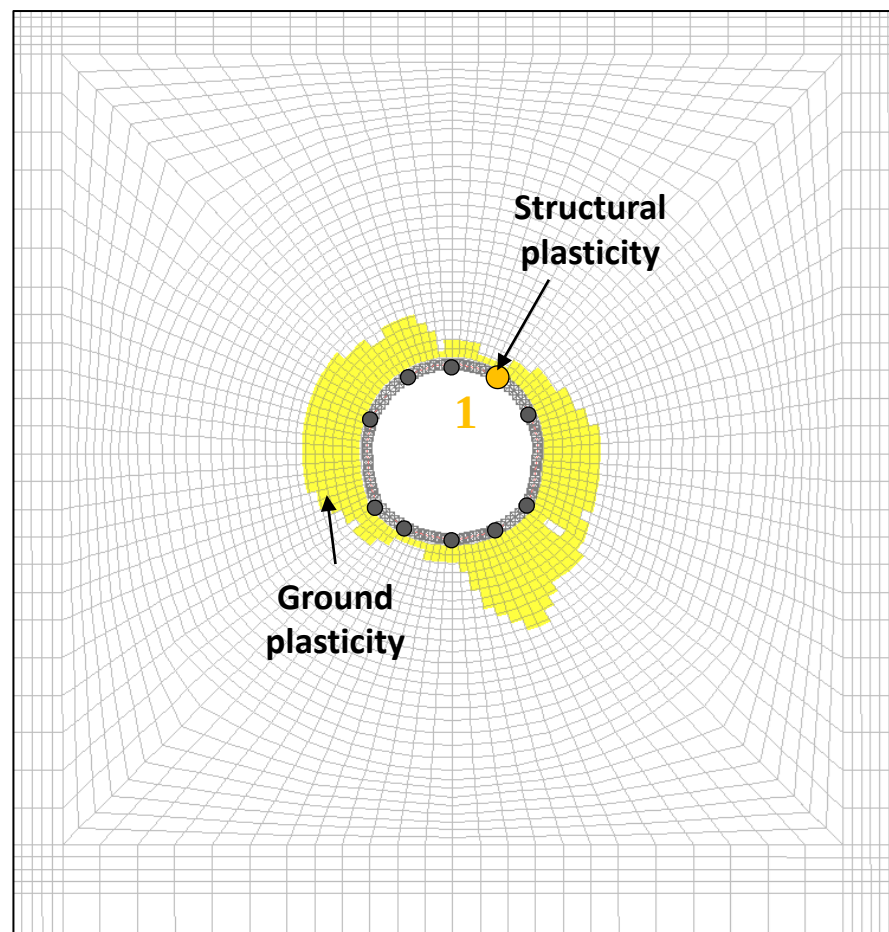


Results: NLSSI tunnel

Evolution of ground and structural nonlinearity



Activation of
1st nonlinear zone



Ground Plasticity Index

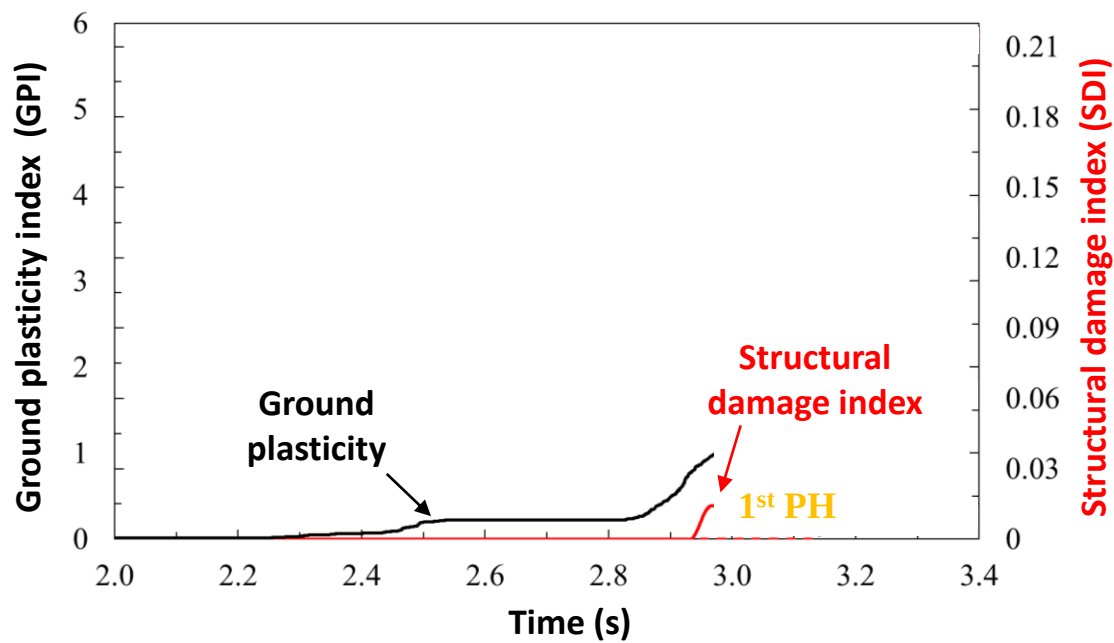
$$GPI = \frac{N_{dyn}^{pl}}{N_{static}^{pl}} - 1$$

N_{dyn}^{pl} ← n° plastic zones dyn analysis
 N_{static}^{pl} ← n° plastic zones static analysis

Structural Damage Index

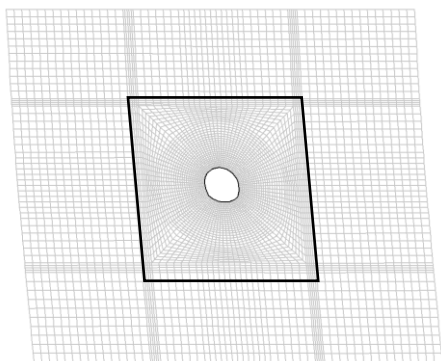
$$SDI = \sum_{i=1}^n \frac{\theta_{pl}^i}{\theta_{pl,u}^i}$$

n ← n° of PH
 θ_{pl}^i ← Plastic rotation
 $\theta_{pl,u}^i$ ← Plastic capacity

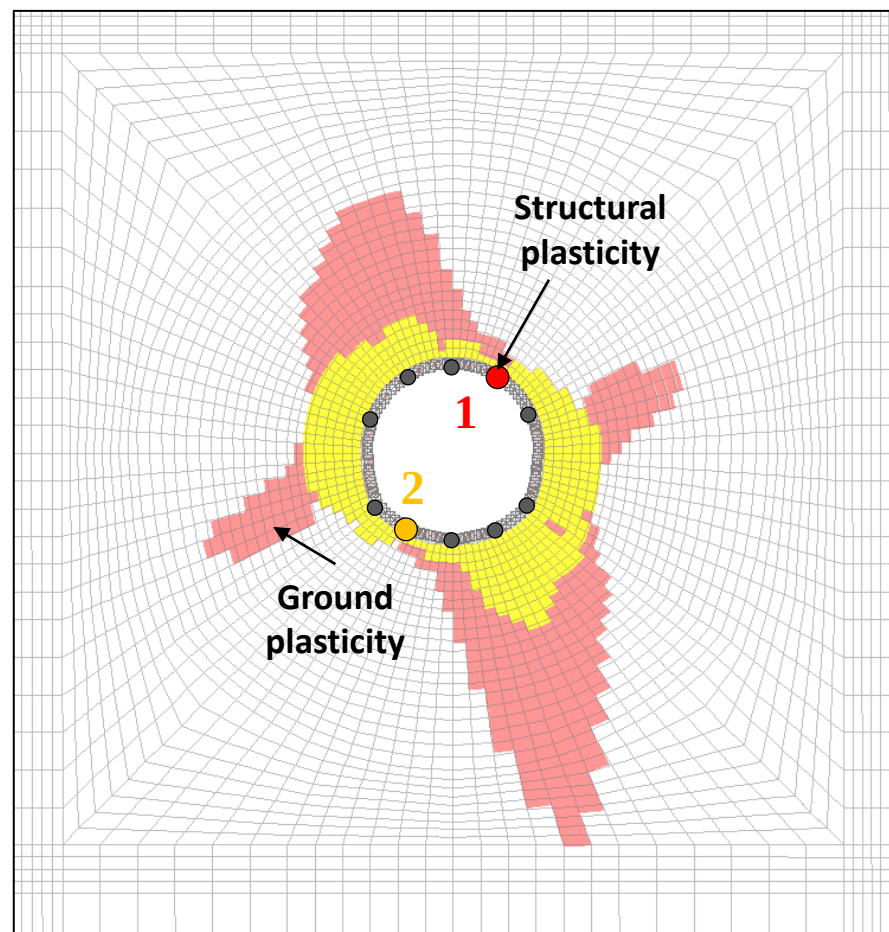


Results: NLSSI tunnel

Evolution of ground and structural nonlinearity



Activation of
2nd nonlinear zone



Ground Plasticity Index

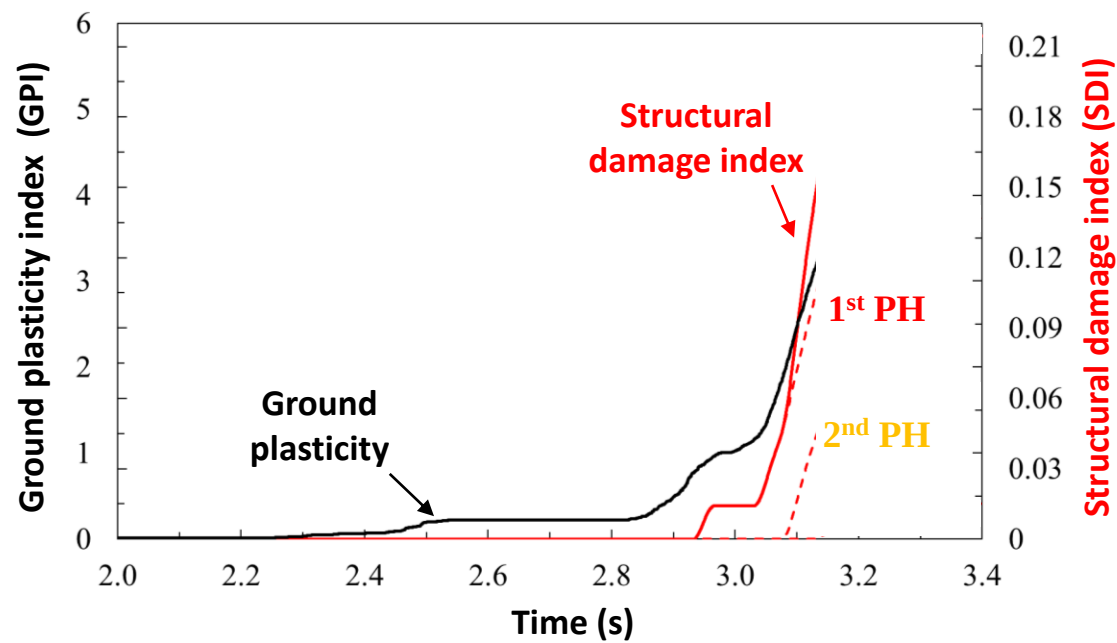
$$GPI = \frac{N_{dyn}^{pl}}{N_{static}^{pl}} - 1$$

N_{dyn}^{pl} : n° plastic zones dyn analysis
 N_{static}^{pl} : n° plastic zones static analysis

Structural Damage Index

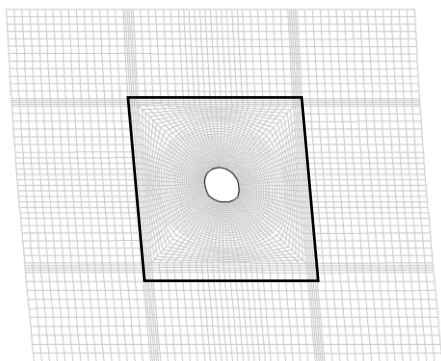
$$SDI = \sum_{i=1}^n \frac{\theta_{pl}^i}{\theta_{pl,u}^i}$$

n : n° of PH
 θ_{pl}^i : Plastic rotation
 $\theta_{pl,u}^i$: Plastic capacity

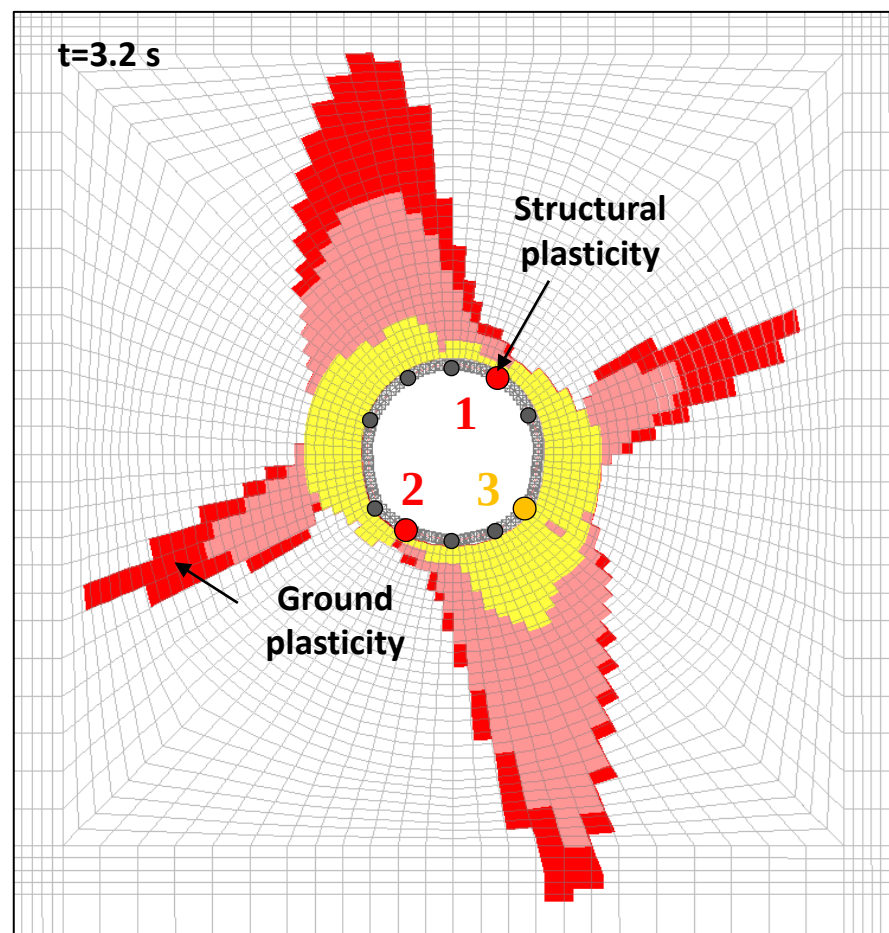


Results: NLSSI tunnel

Evolution of ground and structural nonlinearity



Activation of
3rd nonlinear zone



Ground Plasticity Index

$$GPI = \frac{N_{dyn}^{pl}}{N_{static}^{pl}} - 1$$

n° plastic zones
dyn analysis

n° plastic zones
static analysis

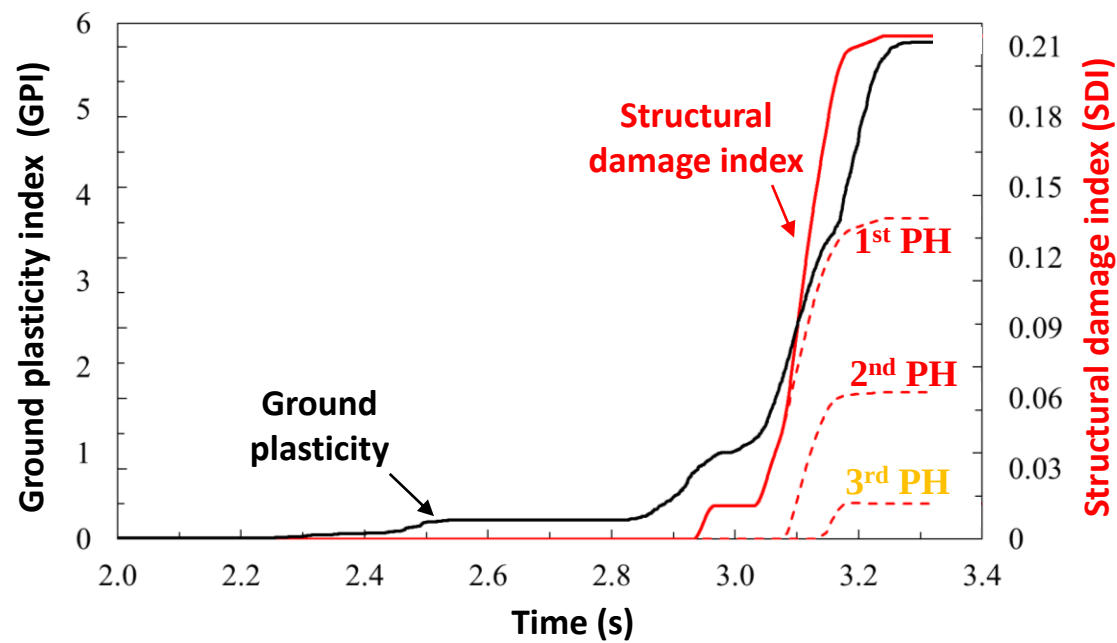
Structural Damage Index

$$SDI = \sum_{i=1}^n \frac{\theta_{pl}^i}{\theta_{pl,u}^i}$$

n° of PH

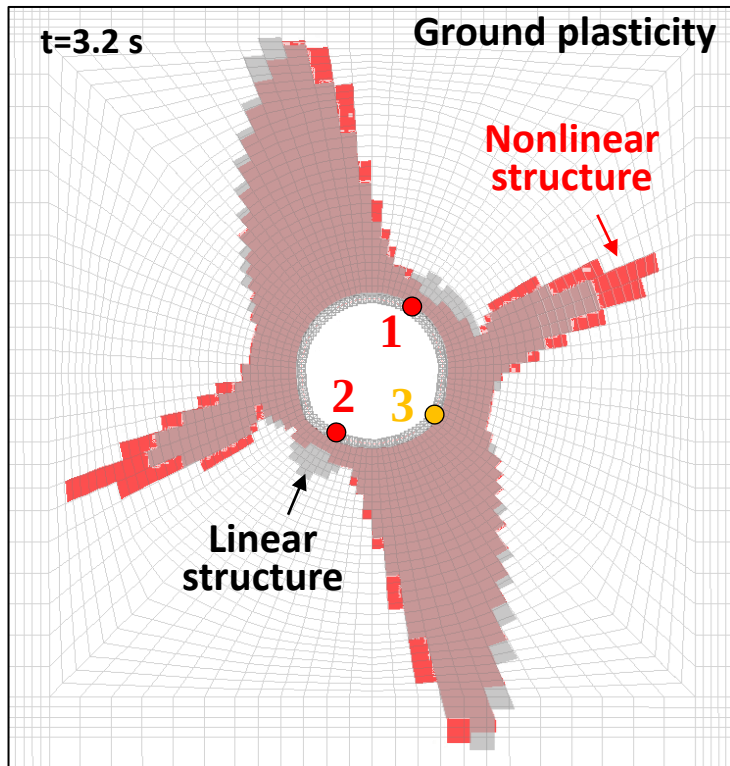
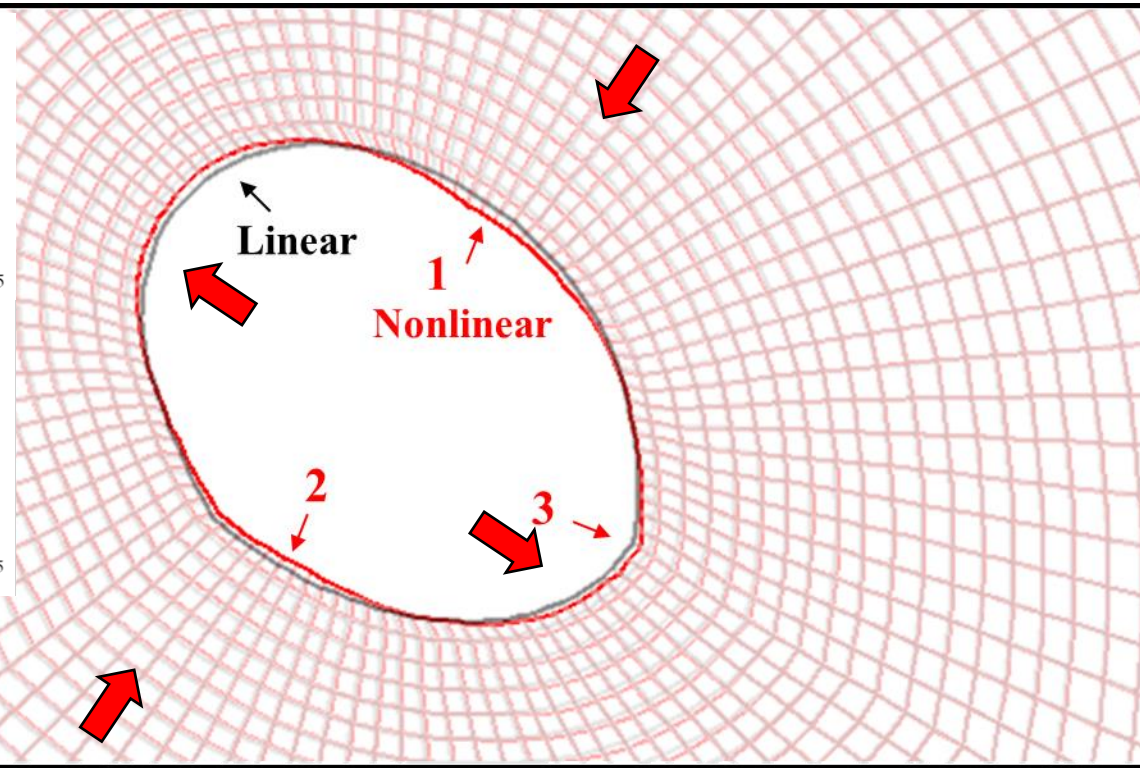
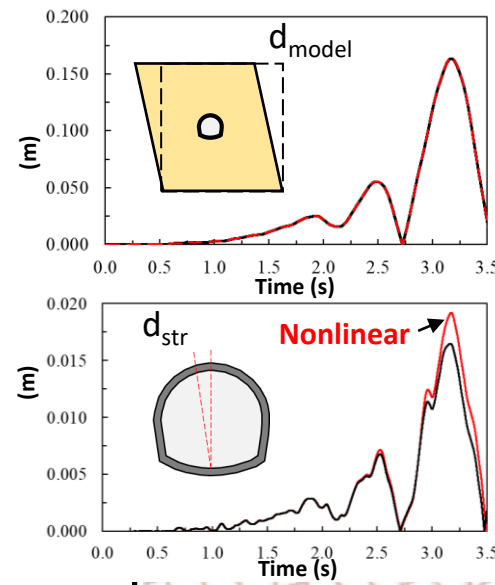
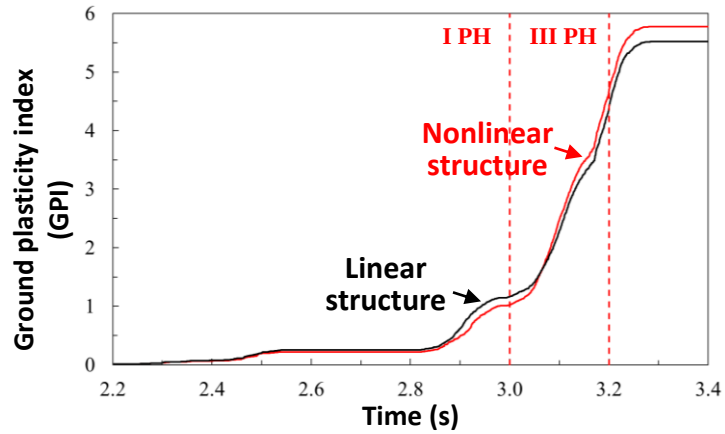
Plastic rotation

Plastic capacity



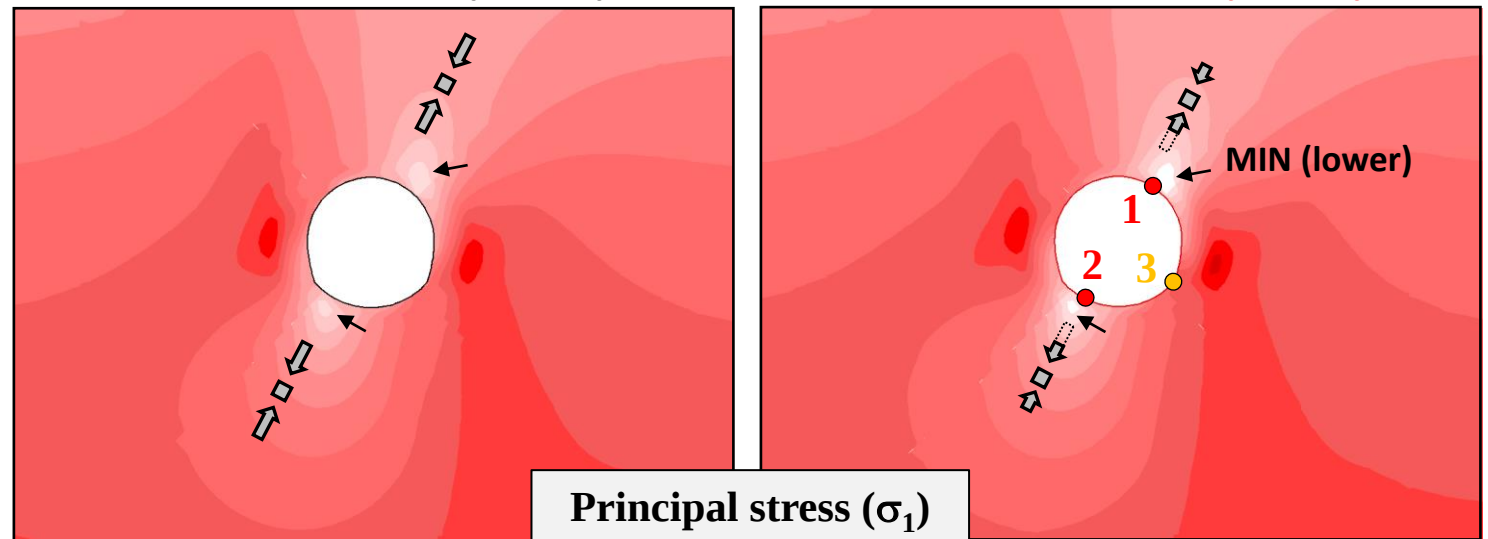
Results: NLSSI tunnel

Linear vs Nonlinear structure



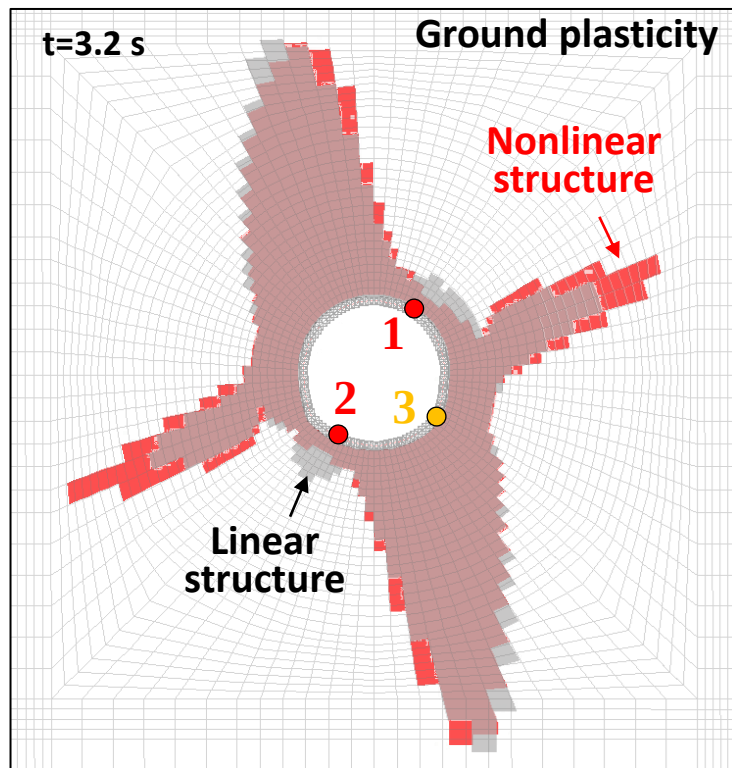
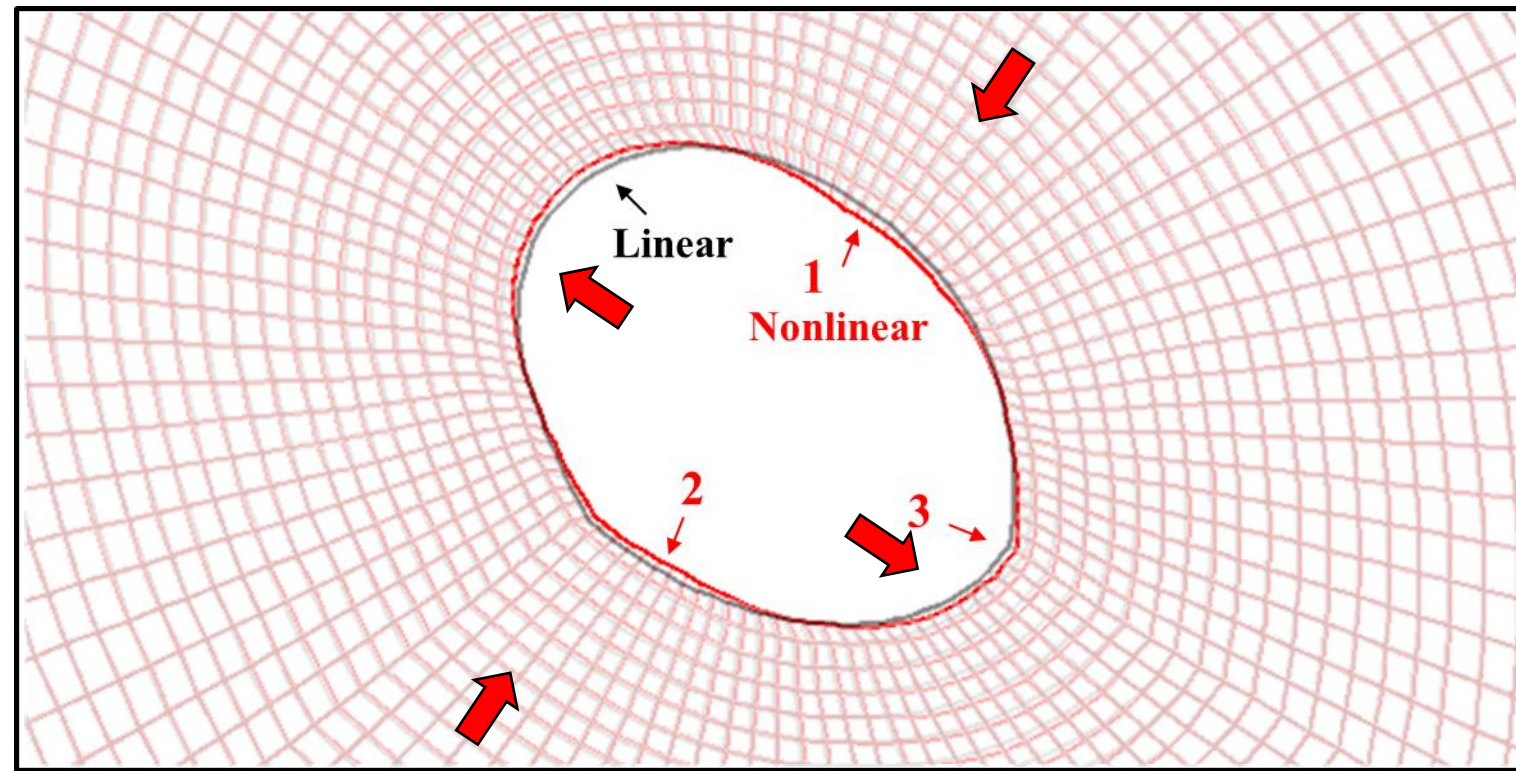
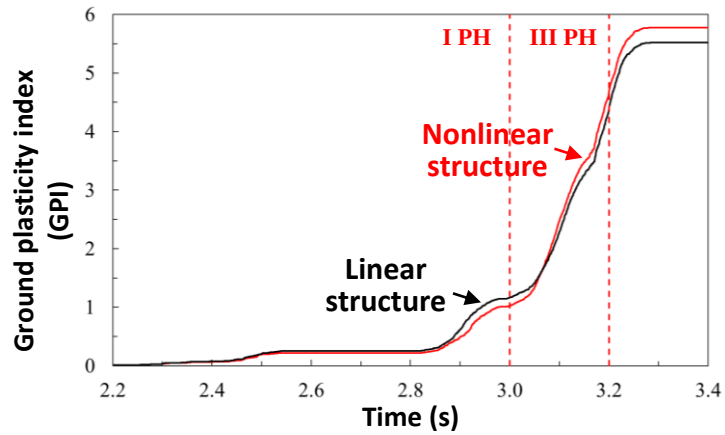
Linear structure ($t=3.2$ s)

Nonlinear structure ($t=3.2$ s)



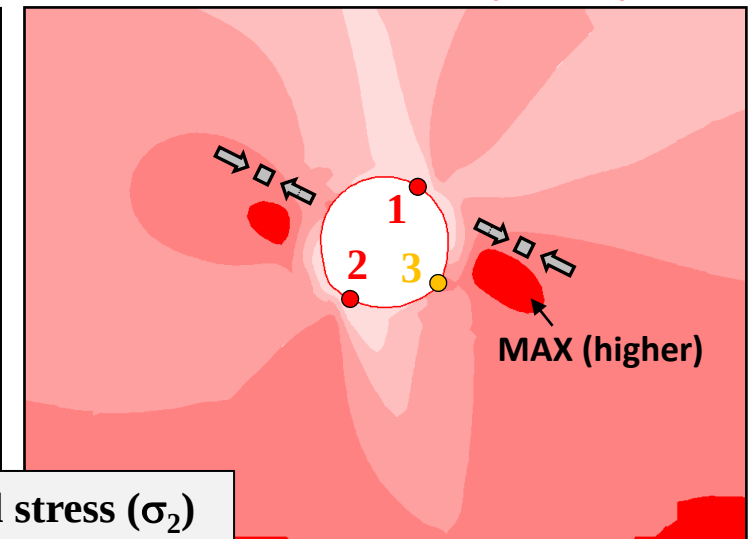
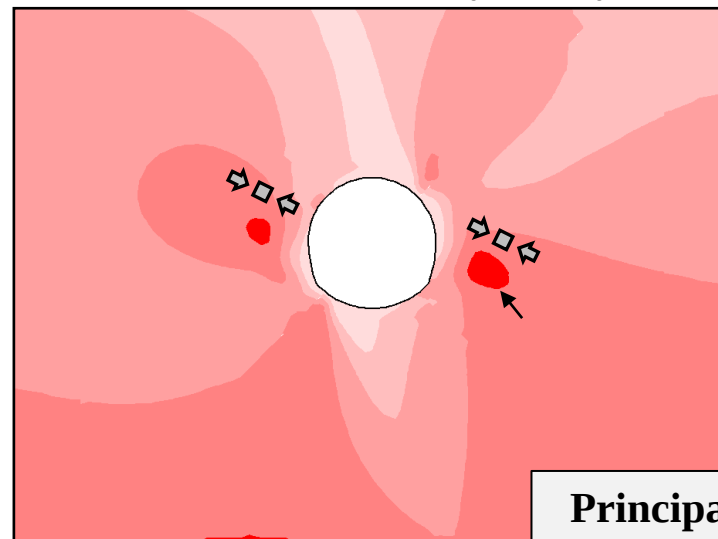
Results: NLSSI tunnel

Linear vs Nonlinear structure



Linear structure ($t=3.2$ s)

Nonlinear structure ($t=3.2$ s)

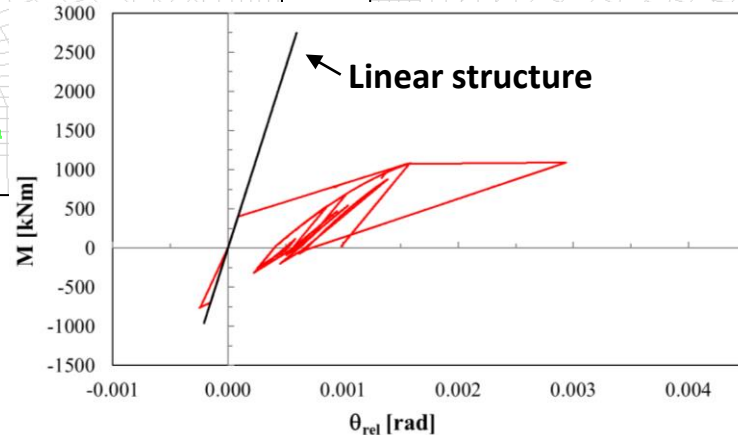
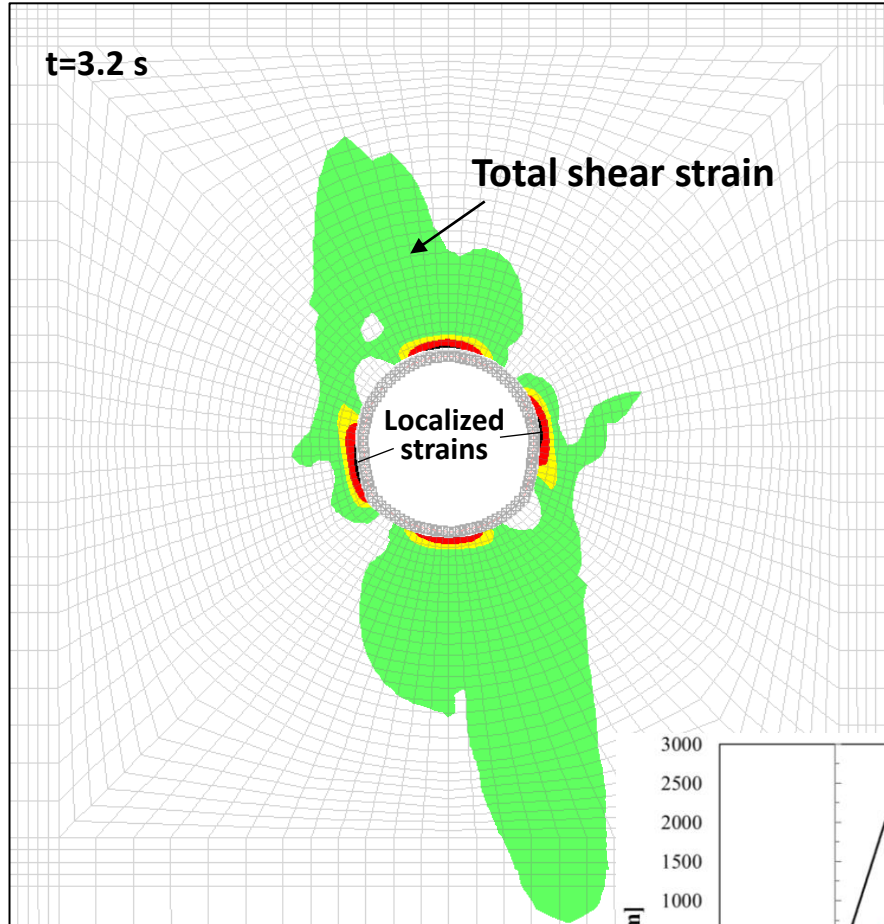


Principal stress (σ_2)

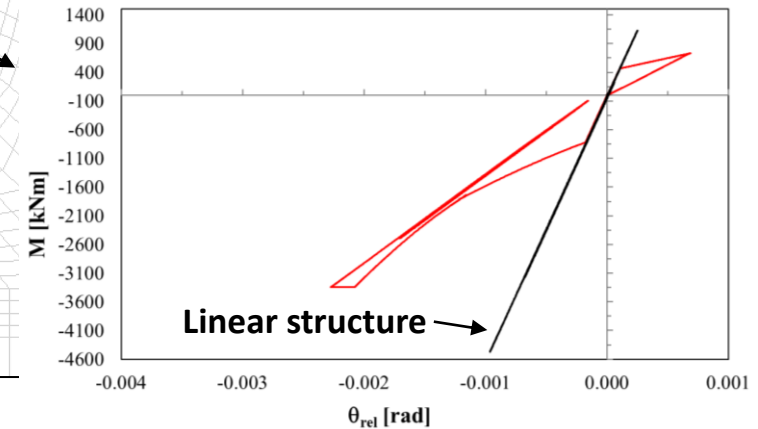
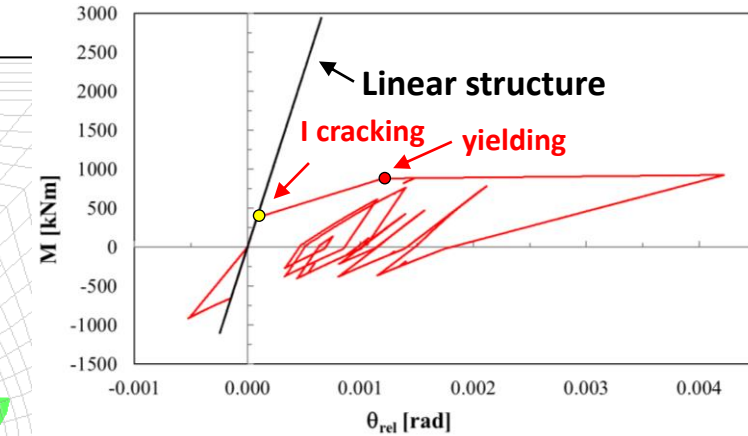
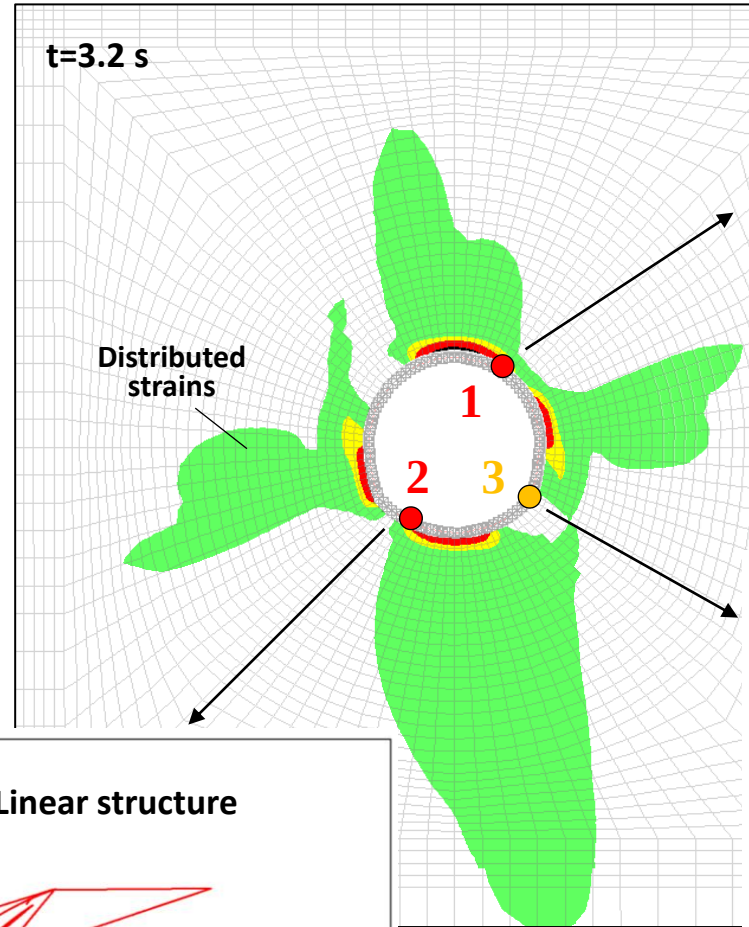
Results: NLSSI tunnel

Linear vs Nonlinear structure: shear strains and structural deformations

Linear structure



Nonlinear structure



Numerical evidence
Structural nonlinearity affects soil nonlinearity

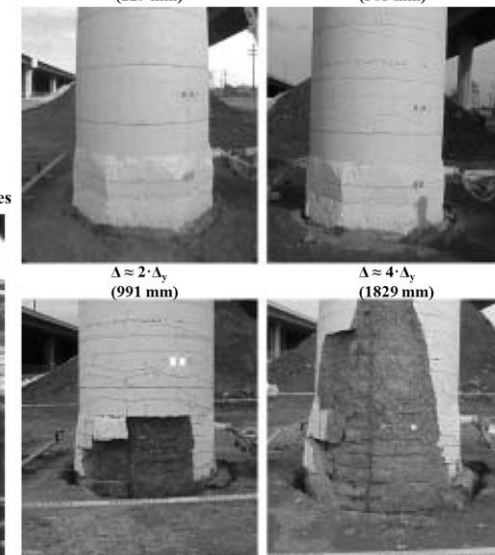
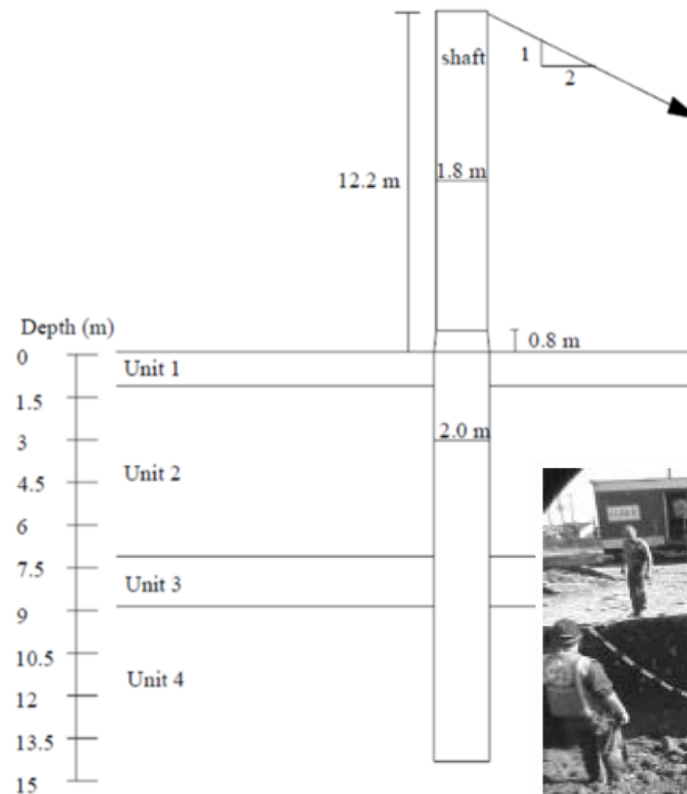
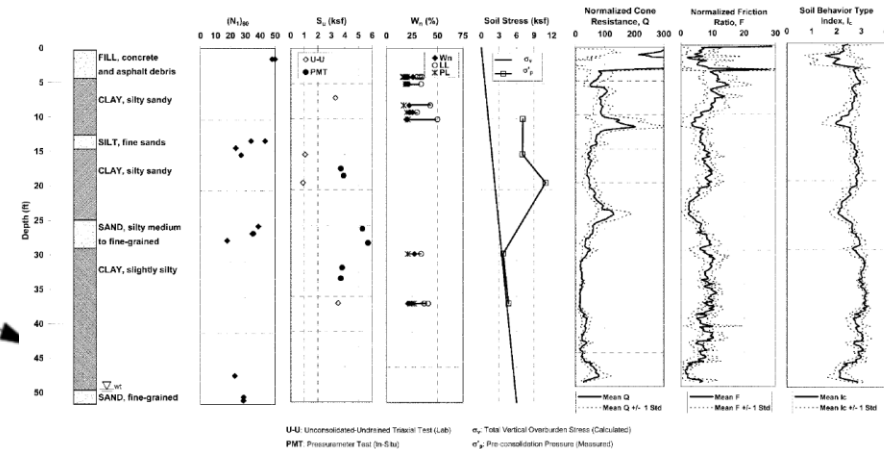
2) Detailed modelling of CIDH bridge column

Experimental benchmark: full-scale cyclic test by UCLA (Janoyan, Wallace and Stuart, 2006)



Why this test?

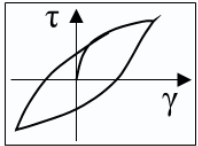
- Severe nonlinearity of both soil and structure
- Full-scale test
- High quality experimental data: soil + structure



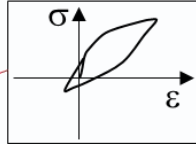
2) Detailed modelling of CIDH bridge column

3D MODEL (ABAQUS)

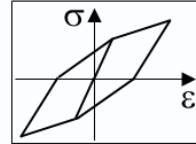
Nonlinear soil



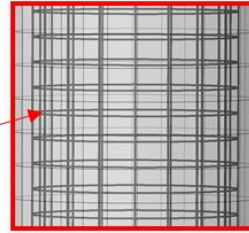
Nonlinear concrete



Nonlinear steel



Embedded longitudinal and transversal reinforcement



Soil-Pile interface elements

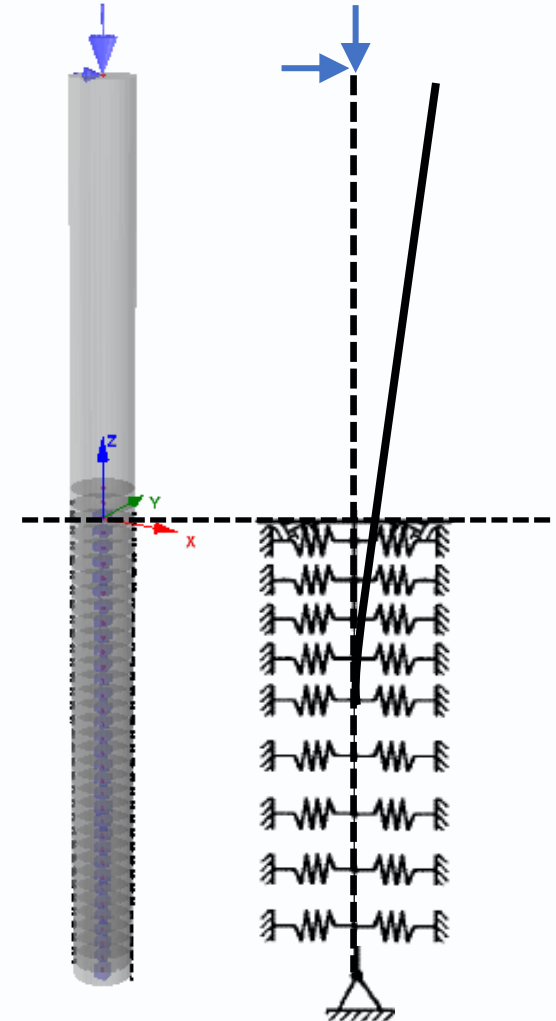
- Frictional model
- Allow separation

Models

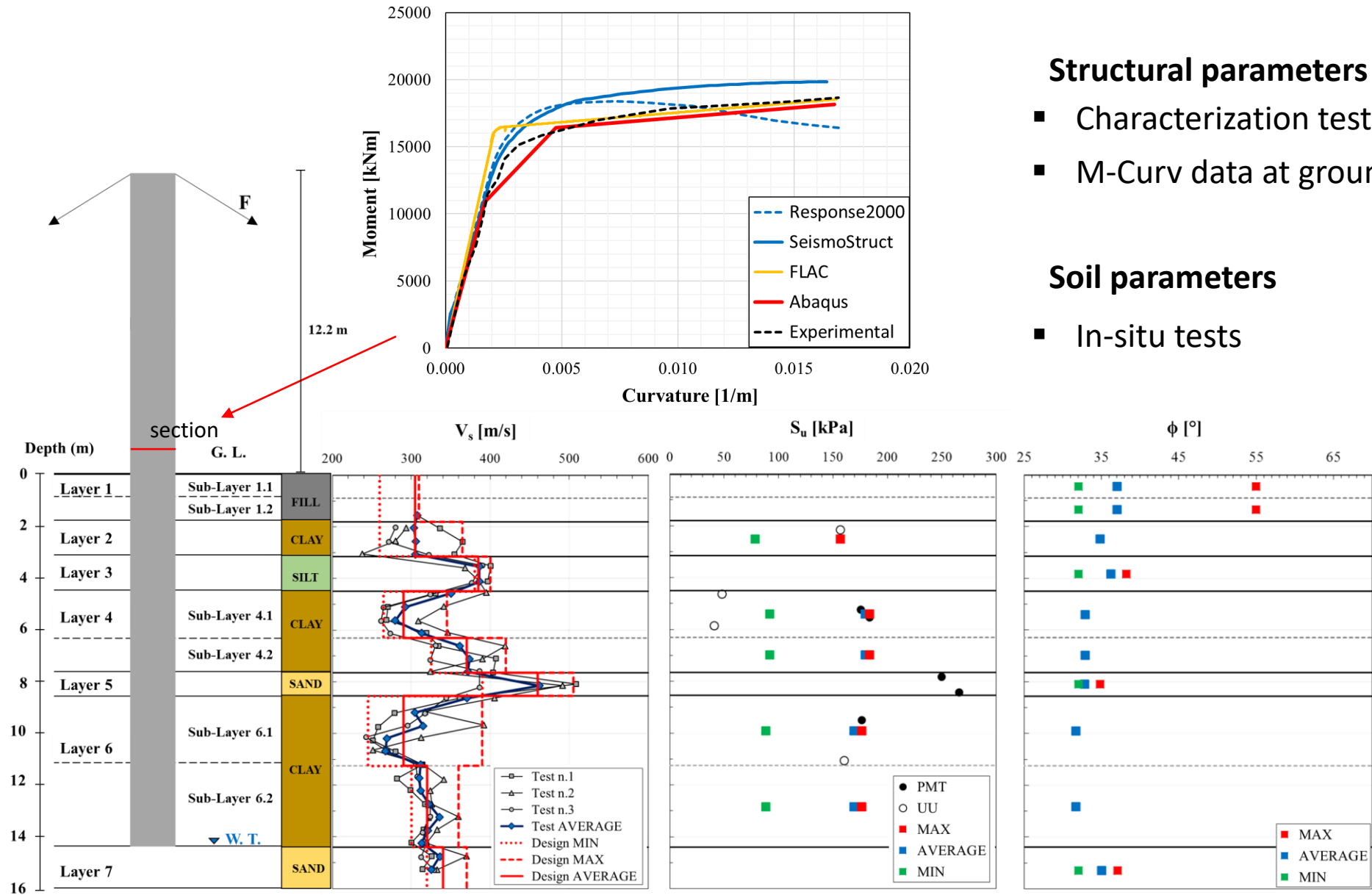
- Soil: Mohr-Coulomb plasticity
- Concrete: Concrete damaged plasticity
- Steel: bi-linear with hardening
- Interface: Frictional model allowing separation

(Andreotti and Calvi, 2021)

Fiber sections and p-y curves (SeismoStruct)



Calibration of model parameters



Structural parameters

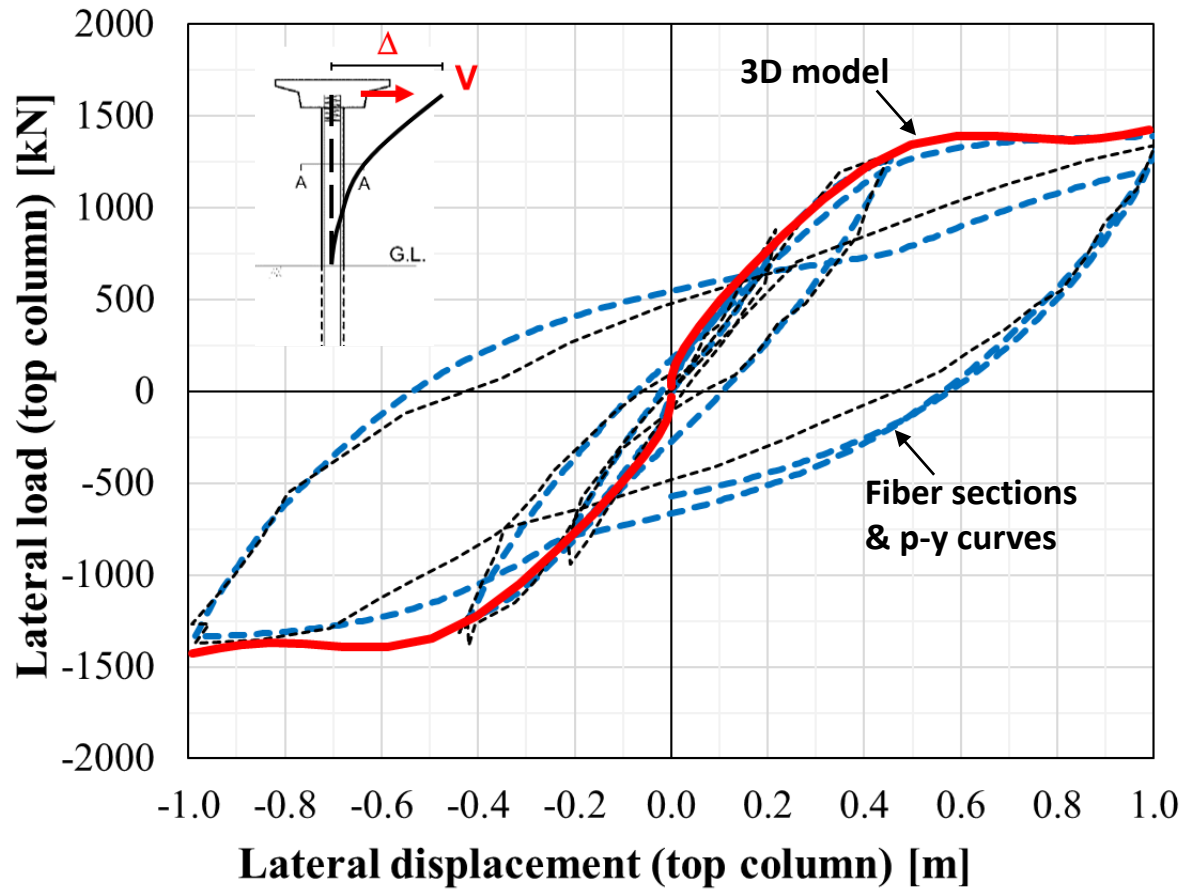
- Characterization tests small specimens
- M-Curv data at ground level

Soil parameters

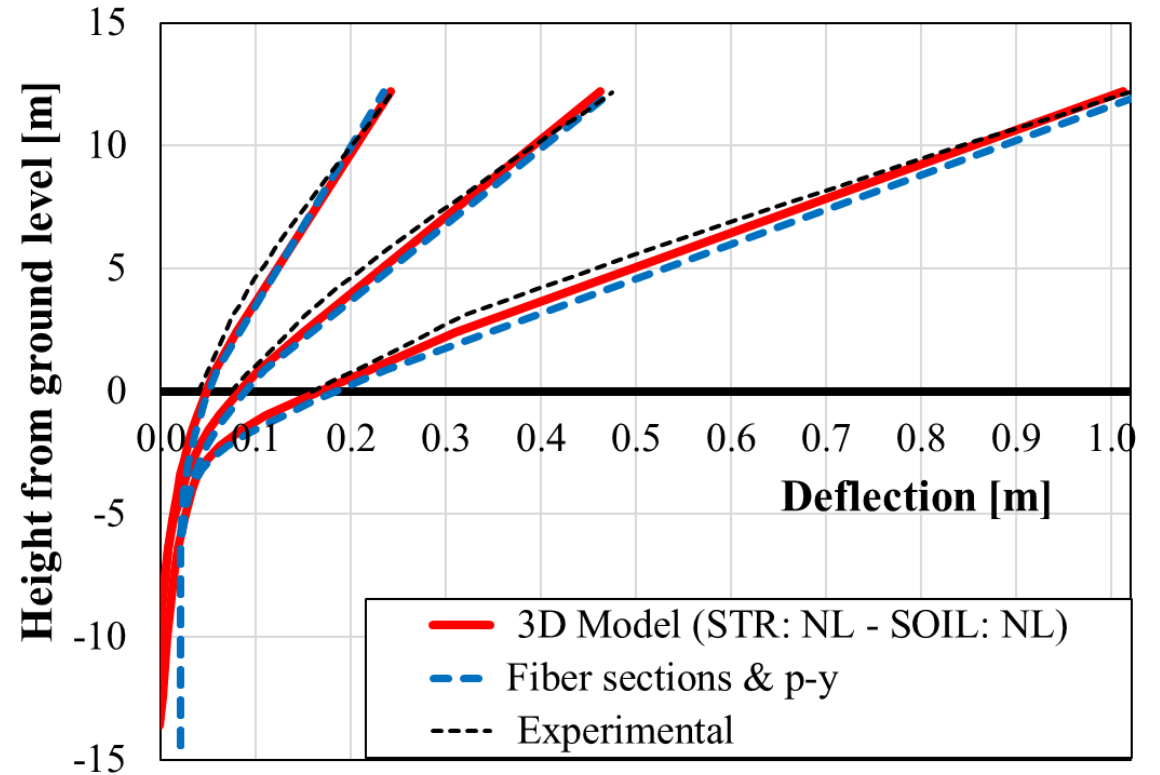
- In-situ tests

Comparison 3D model and fiber sections/p-y curves

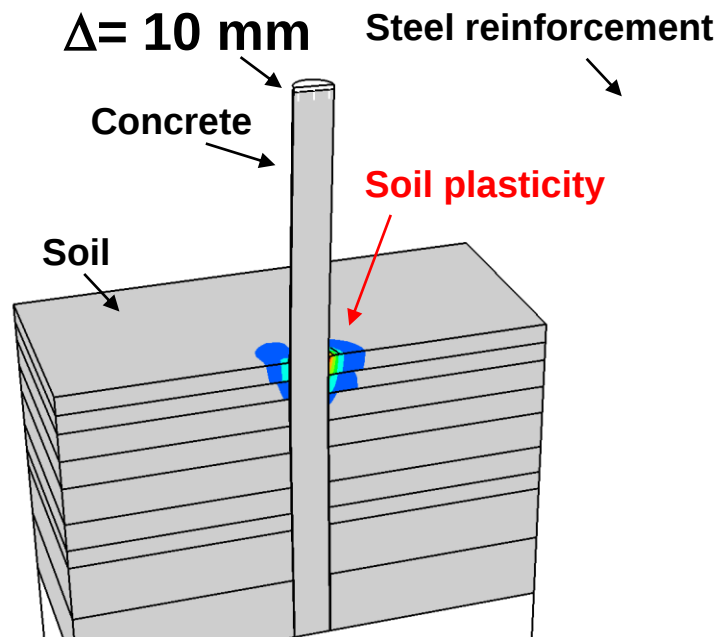
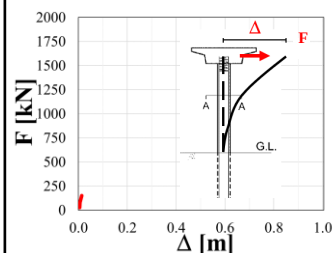
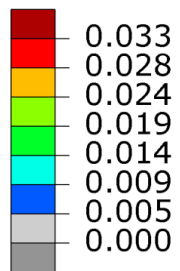
Force-displacement



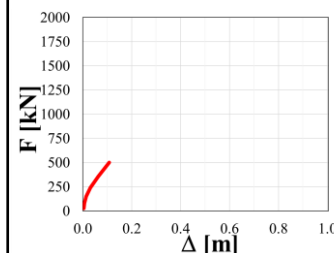
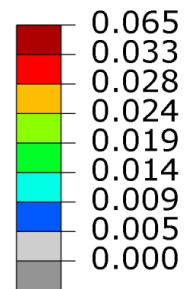
Displacement profile



**Plastic strain
(PE max principal)**



$\Delta = 103$ mm

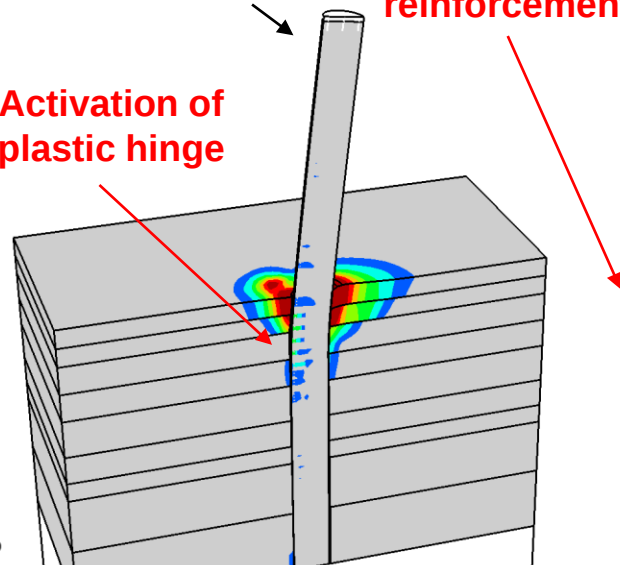
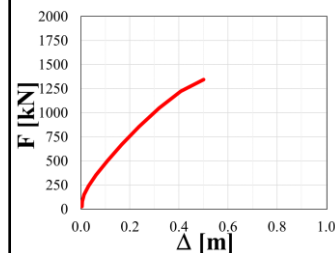
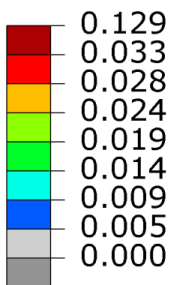


Tensile cracks in concrete

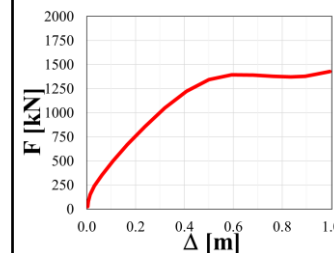
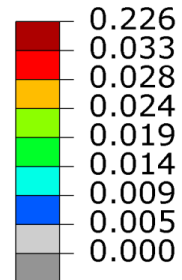
$\Delta = 490$ mm

Yielding of steel reinforcement

Activation of plastic hinge



$\Delta = 991$ mm

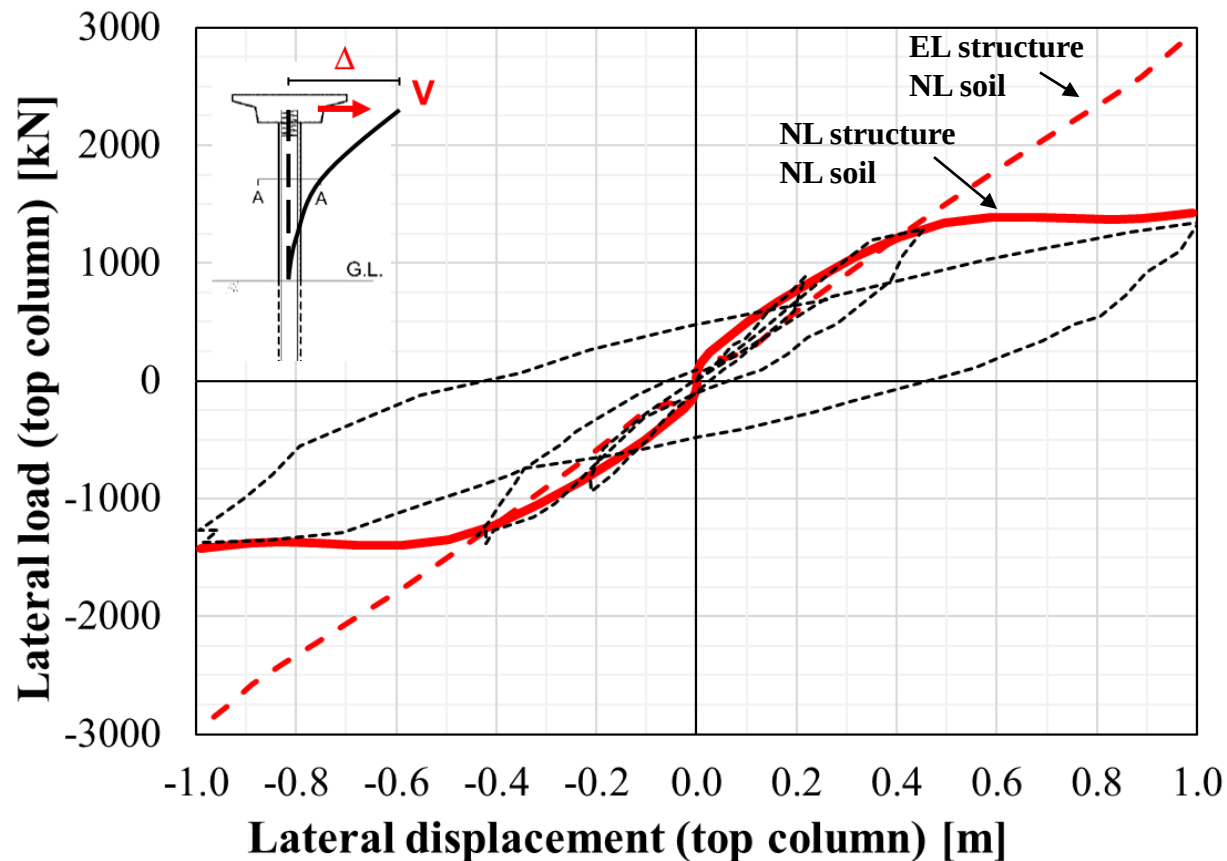


Plastic hinge

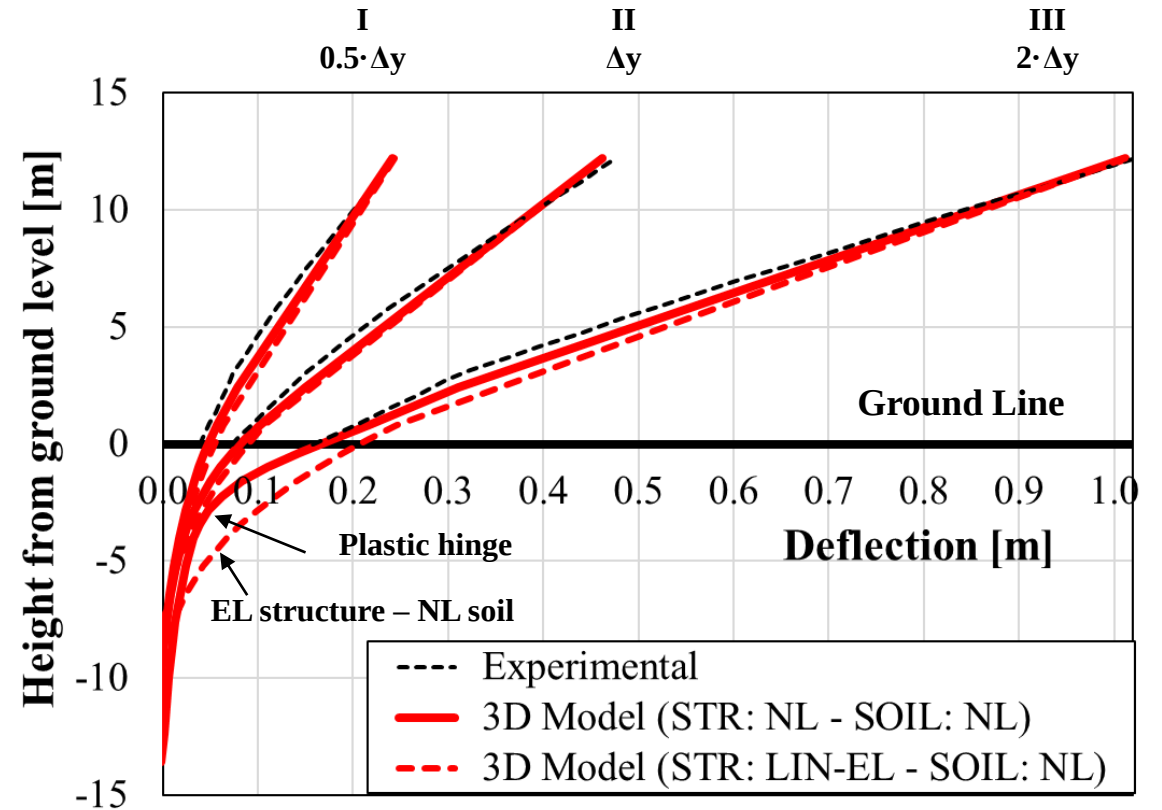
3D model: Elastic vs Nonlinear structure

Results with identical soil and different structural behaviour (LIN vs NL)

Force-displacement



Displacement profile

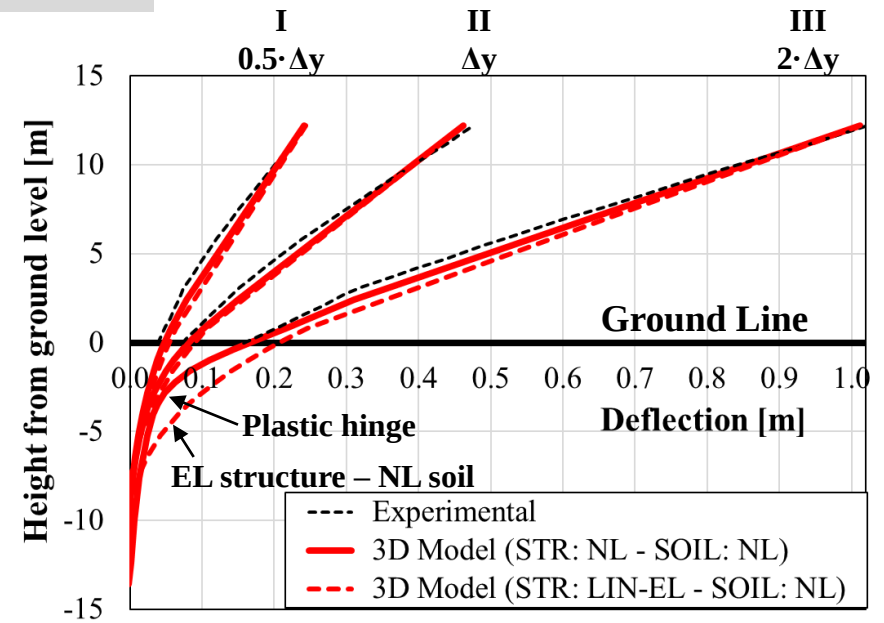


Structural influence on soil nonlinearity

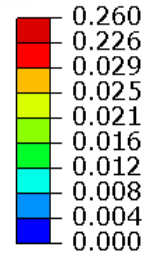
Results with identical soil and different structural behaviour (LIN vs NL)

NL structure
(decreasing structural stiffness)

EL structure
(constant structural stiffness)



Plastic strains



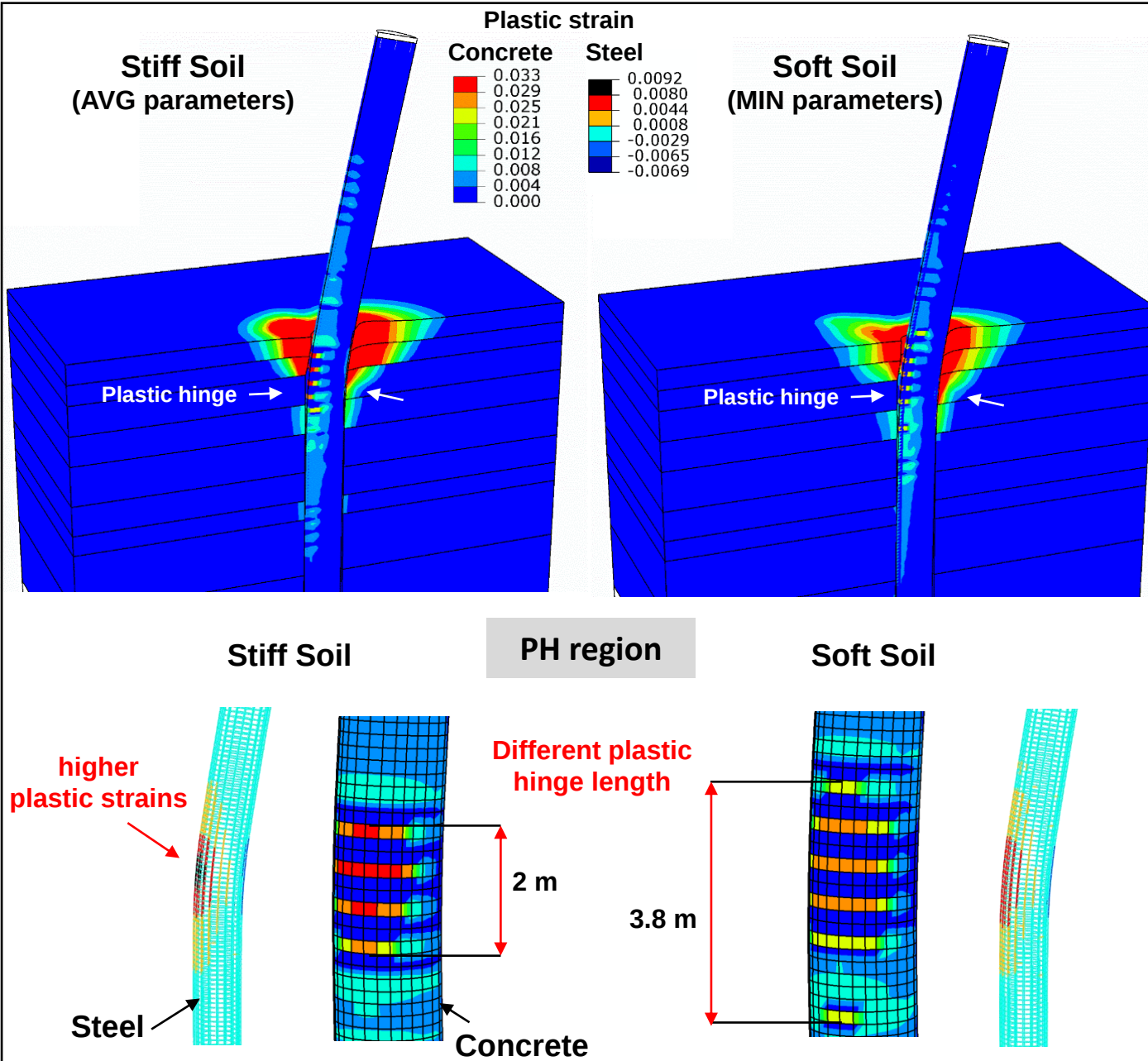
Plastic hinge →

- Greater volume of nonlinear soil
- Soil nonlinearity goes deeper

▪ Evaluation of inertial interaction only!

Identical structure
different soil

Influence of soil stiffness on structural nonlinearity



Stiff soils

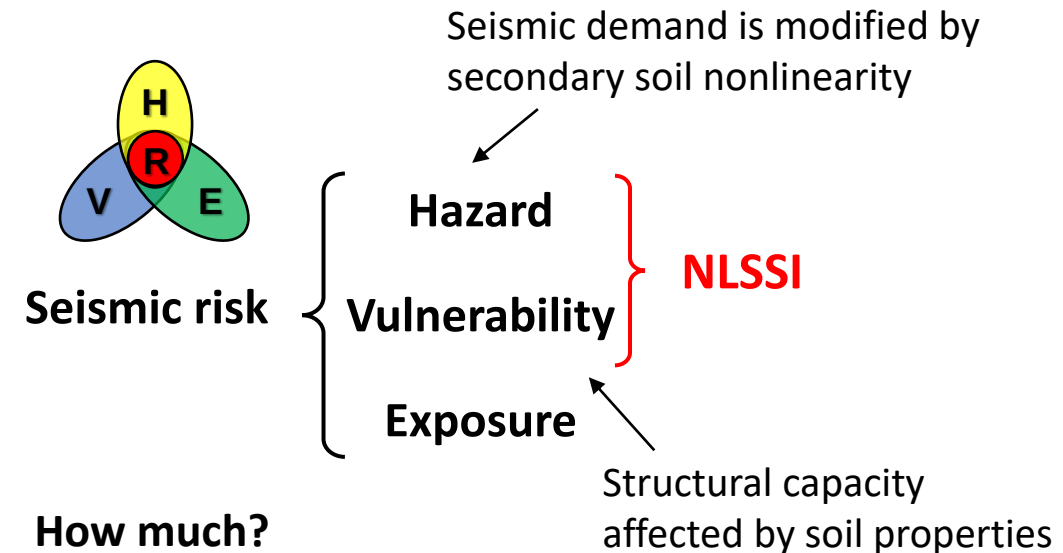
- Concentration of strains (soil & structure)
- Smaller plastic hinge length**
- Higher curvature demand

Soft soils

- Distribution of strains
- Larger plastic hinge length**
- Lower curvature demand

Numerical evidence

Soil properties affect structural capacity



Experimental tests: issues of NLSSI

- Centrifuge tests

Artificial gravity field

Small scale structural models (1/20 – 1/50)

Correct reproduction of soil properties and confinement



Problems to reproduce detailing and damage of reinforced concrete elements

- Shake tables with small soil boxes

Larger structural models (scale 1/10 – 1/5)

Small soil vertical stress

Less problems to reproduce RC elements



Problems to reproduce soil properties and confinement

- Mobile laboratory for in-situ dynamic tests

(Calvi et al., 2021)

Full scale tests in-situ (dynamic inertial SSI interaction)



Feasibility study to reproduce kinematic SSI interaction



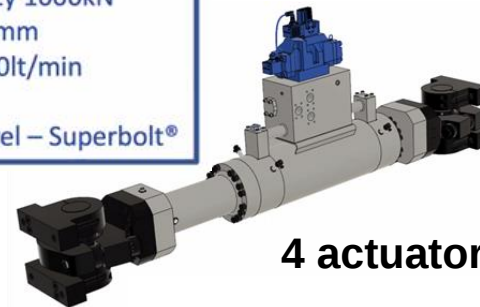
TRAILER

- Pressure unit
- Reservoir
- Axial piston pumps
- Cooling & Filtering system
- Warming system
- Accumulators
- Distribution

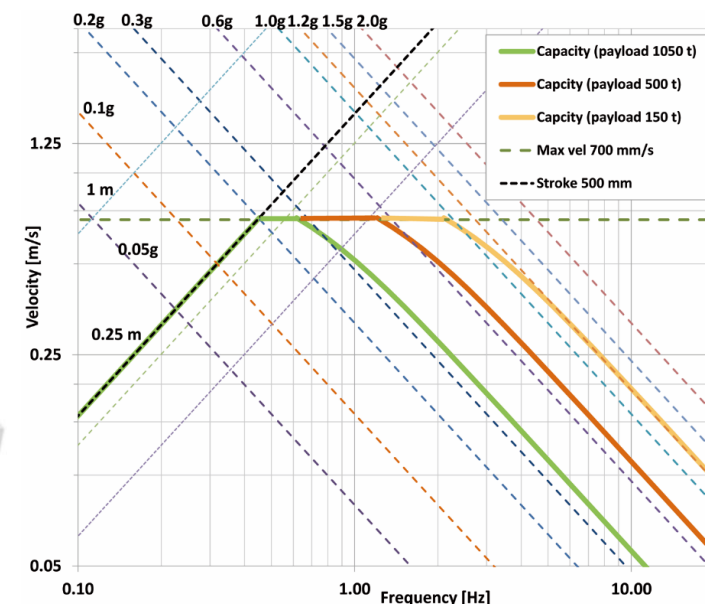
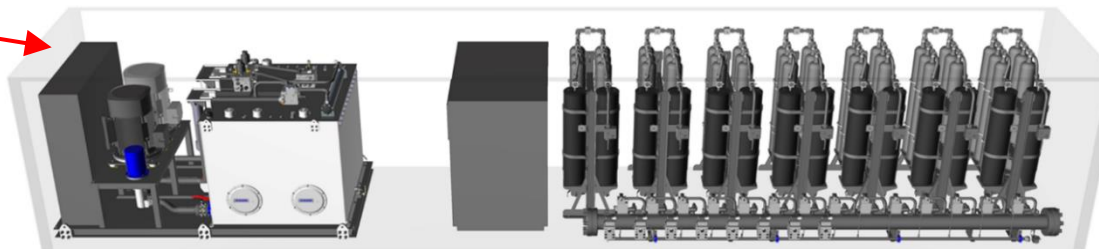
ACTUATOR

Force capability 1000kN
Stroke +/-250mm
Servovalve 890lt/min

Spherical Swivel – Superbolt®

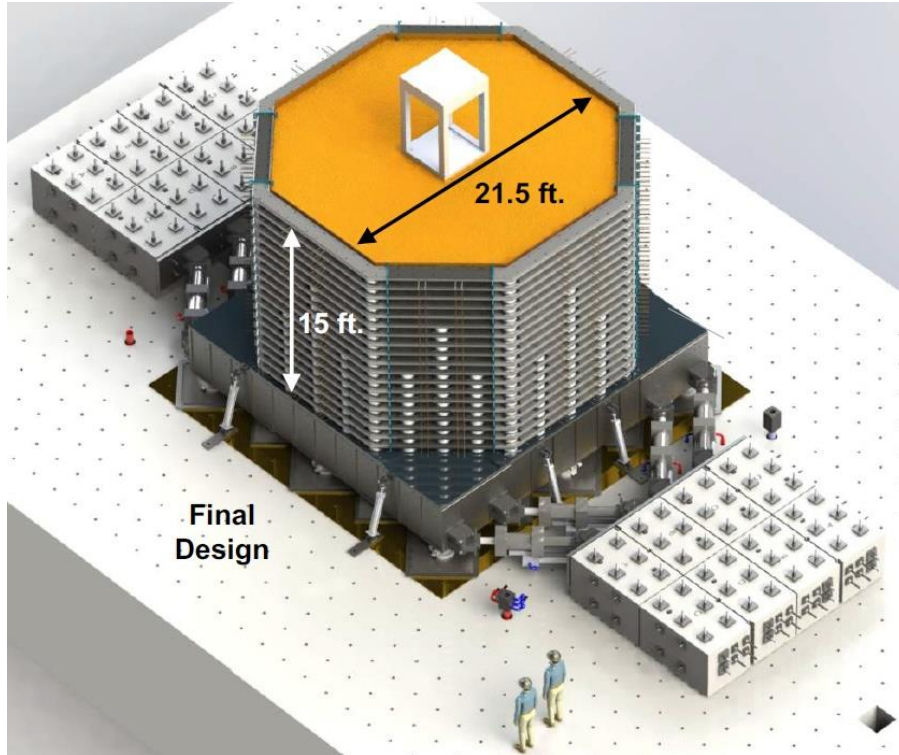


4 actuators



Experimental tests on NLSSI: fill the gap between research and practice

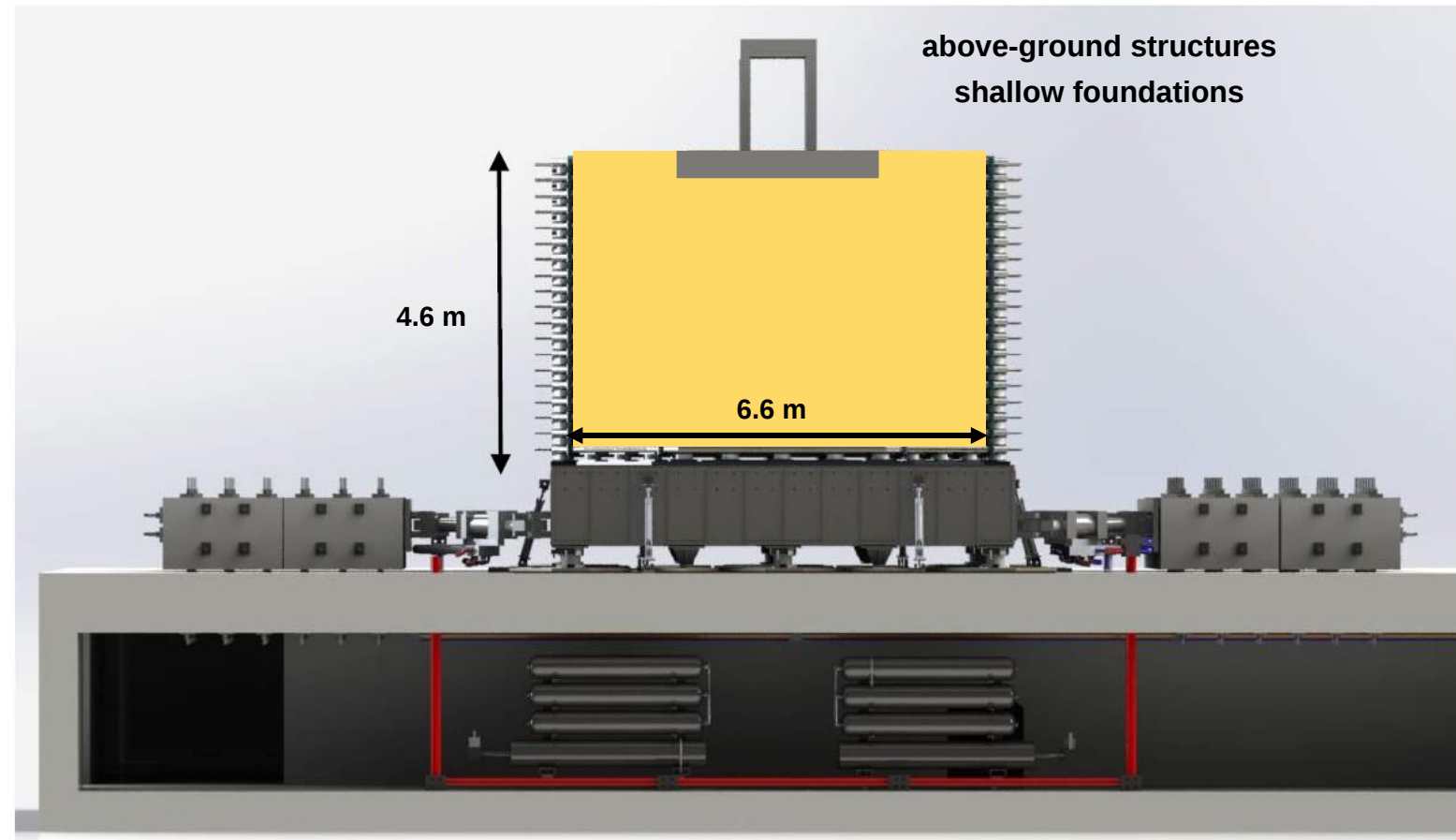
New shake table with big soil box University of Nevada, Reno



Important contributions to dynamic NLSSI

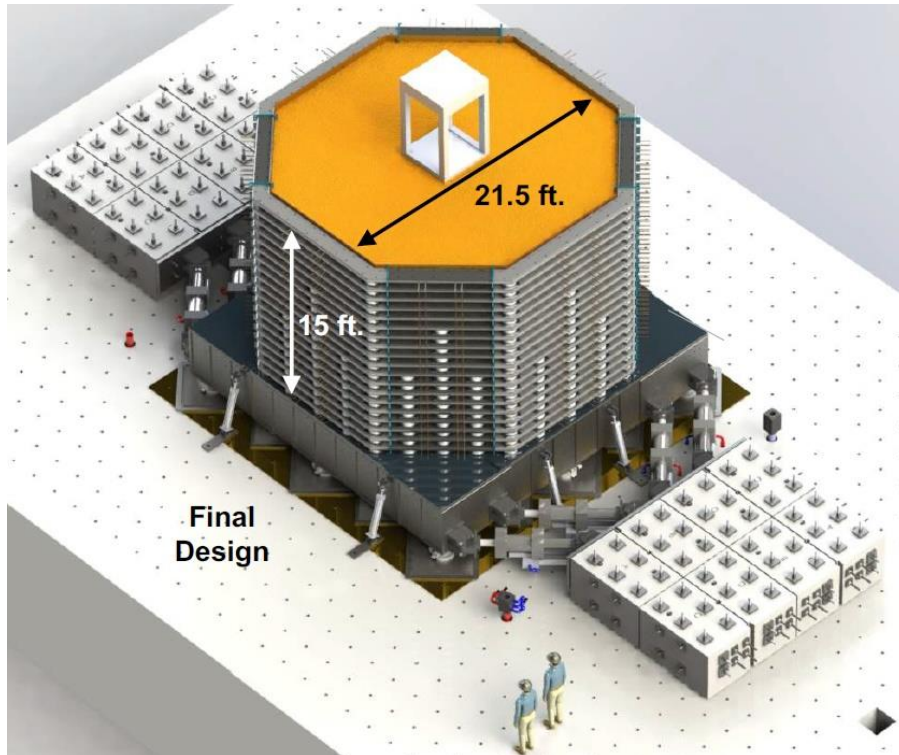


- Structural damage of RC elements
- Failure mechanisms of the system
- Kinematic and inertial interaction
- Soil properties
- Primary and secondary soil nonlinearity
- Damping (e.g. radiation)



Experimental tests on NLSSI: fill the gap between research and practice

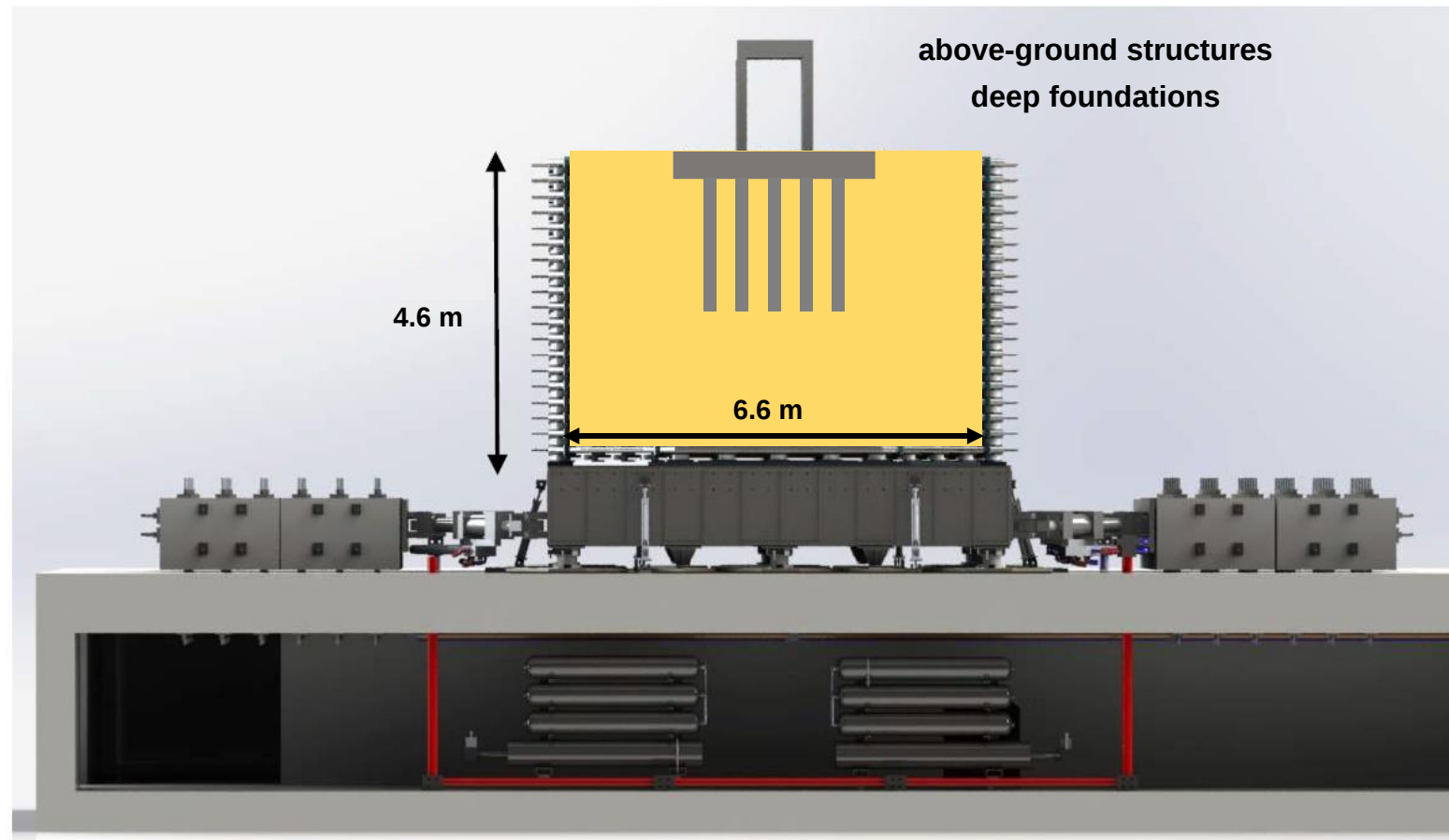
New shake table with big soil box University of Nevada, Reno



Important contributions to dynamic NLSSI

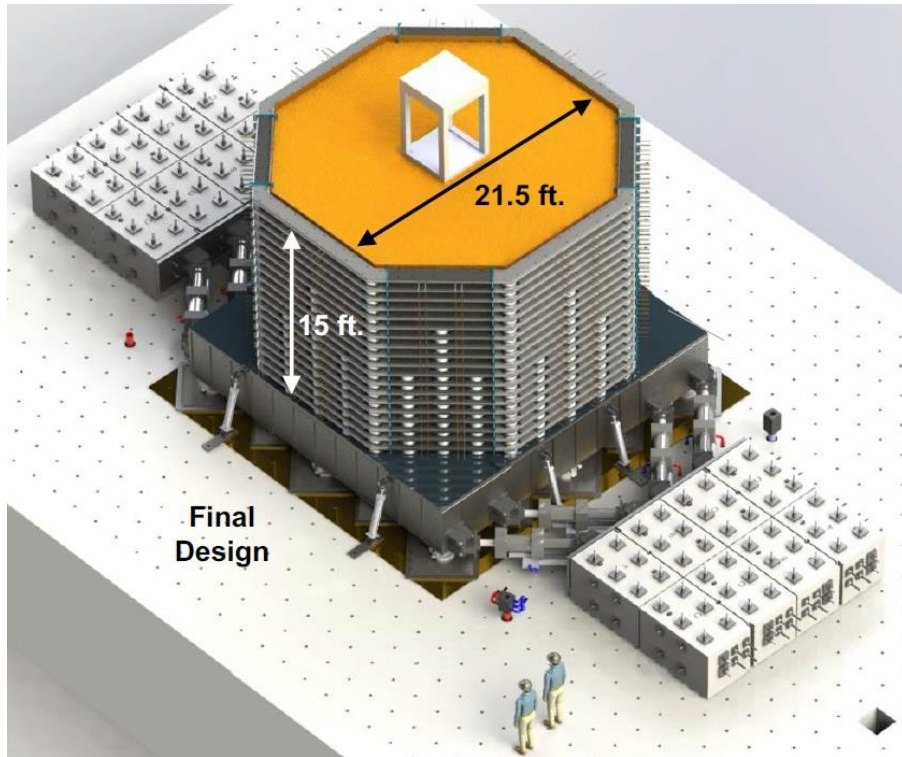


- Structural damage of RC elements
- Failure mechanisms of the system
- Kinematic and inertial interaction
- Soil properties
- Primary and secondary soil nonlinearity
- Damping (e.g. radiation)



Experimental tests on NLSSI: fill the gap between research and practice

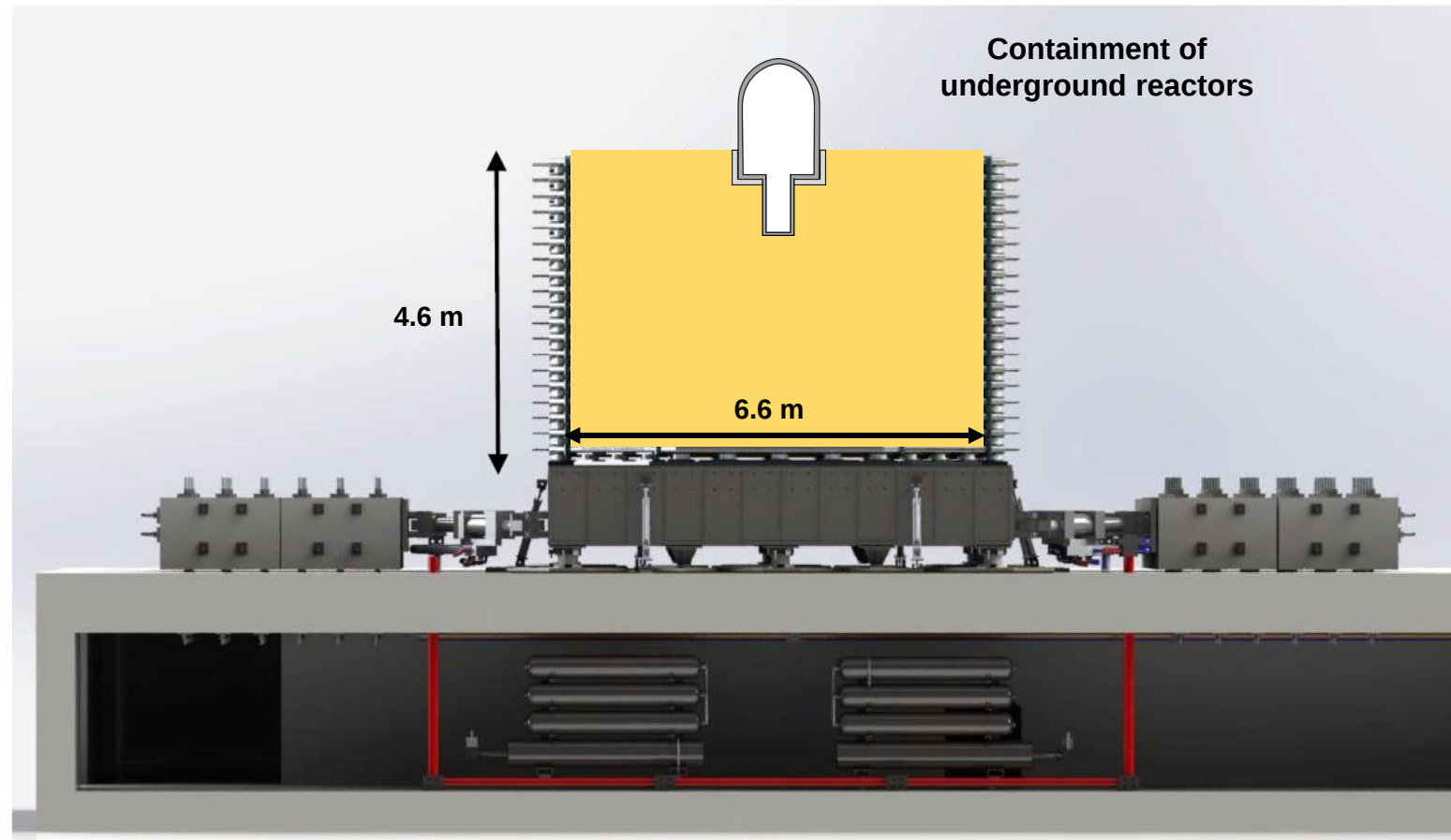
New shake table with big soil box University of Nevada, Reno



Important contributions to dynamic NLSSI

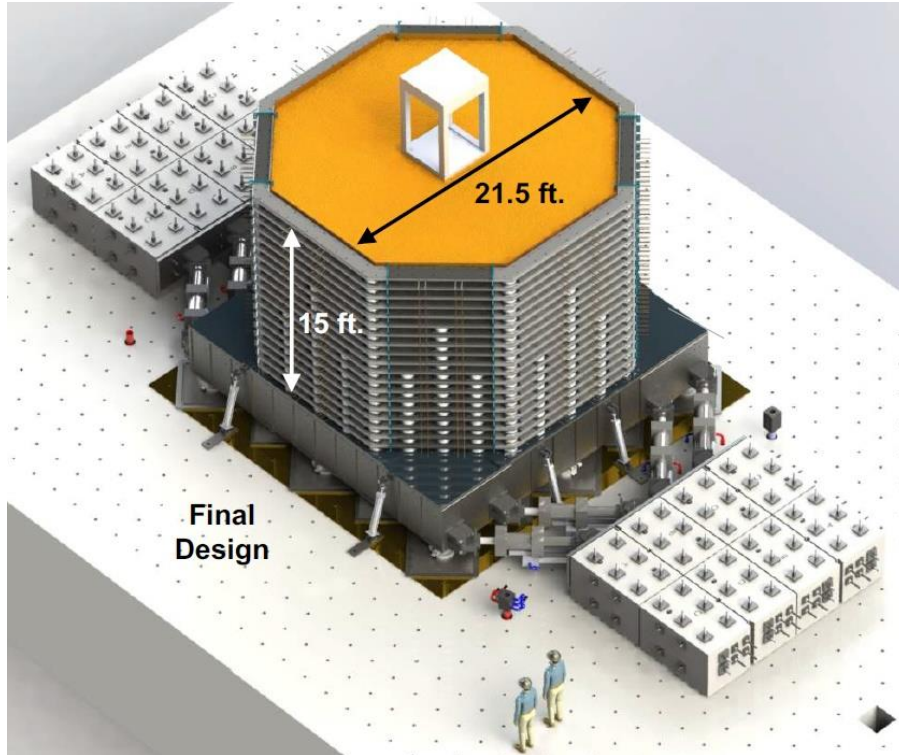


- Structural damage of RC elements
- Failure mechanisms of the system
- Kinematic and inertial interaction
- Soil properties
- Primary and secondary soil nonlinearity
- Damping (e.g. radiation)



Experimental tests on NLSSI: fill the gap between research and practice

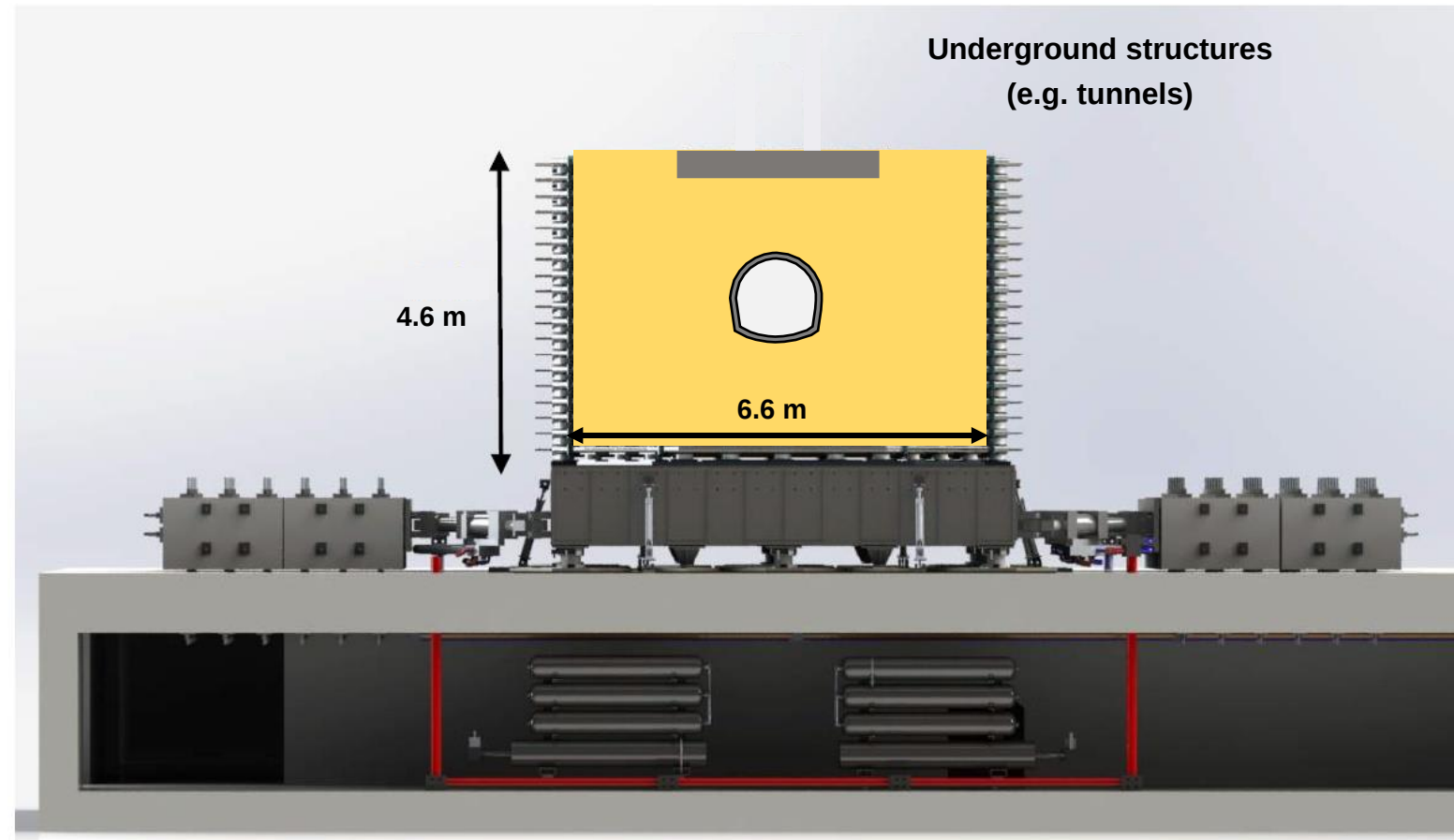
New shake table with big soil box University of Nevada, Reno



Important contributions to dynamic NLSSI

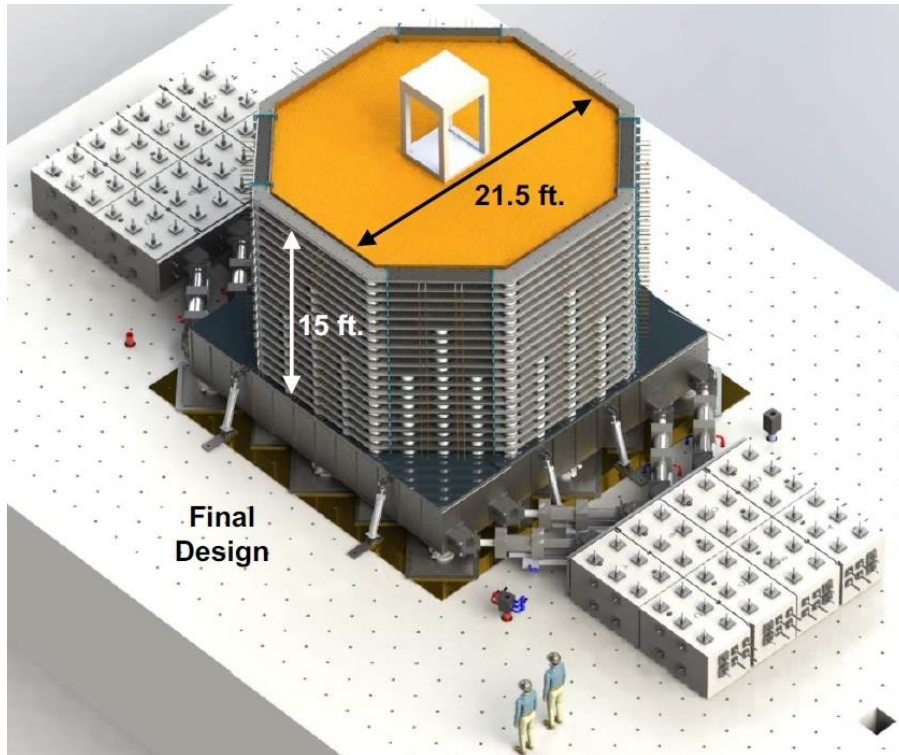


- Structural damage of RC elements
- Failure mechanisms of the system
- Kinematic and inertial interaction
- Soil properties
- Primary and secondary soil nonlinearity
- Damping (e.g. radiation)



Experimental tests on NLSSI: fill the gap between research and practice

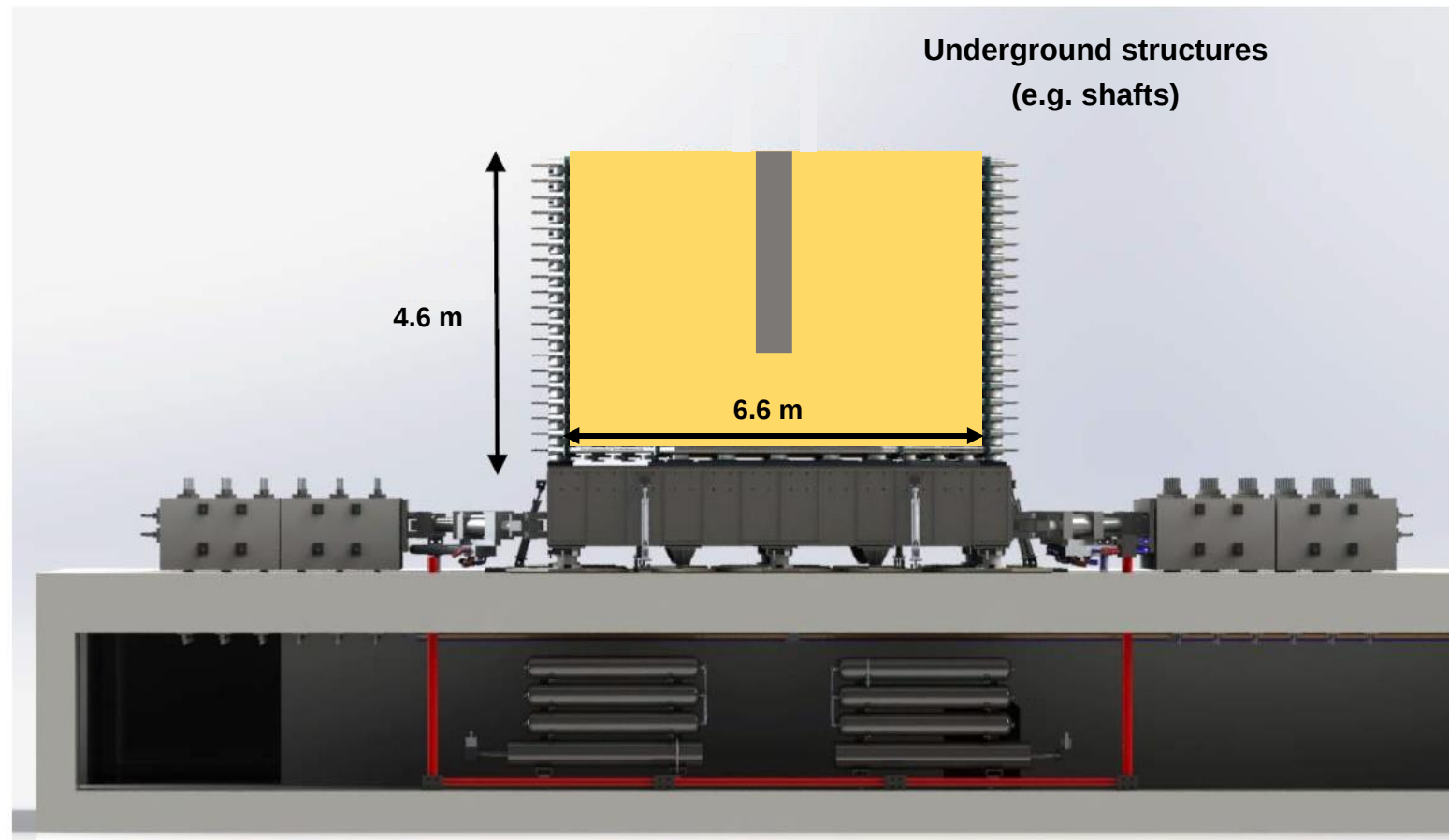
New shake table with big soil box University of Nevada, Reno



Important contributions to dynamic NLSSI

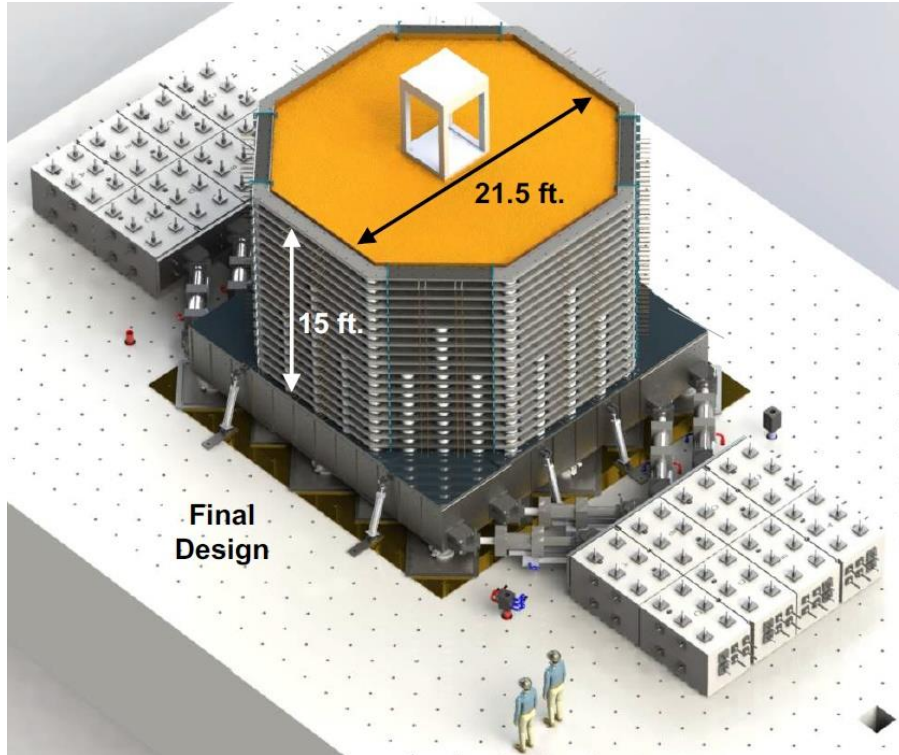


- Structural damage of RC elements
- Failure mechanisms of the system
- Kinematic and inertial interaction
- Soil properties
- Primary and secondary soil nonlinearity
- Damping (e.g. radiation)



Experimental tests on NLSSI: fill the gap between research and practice

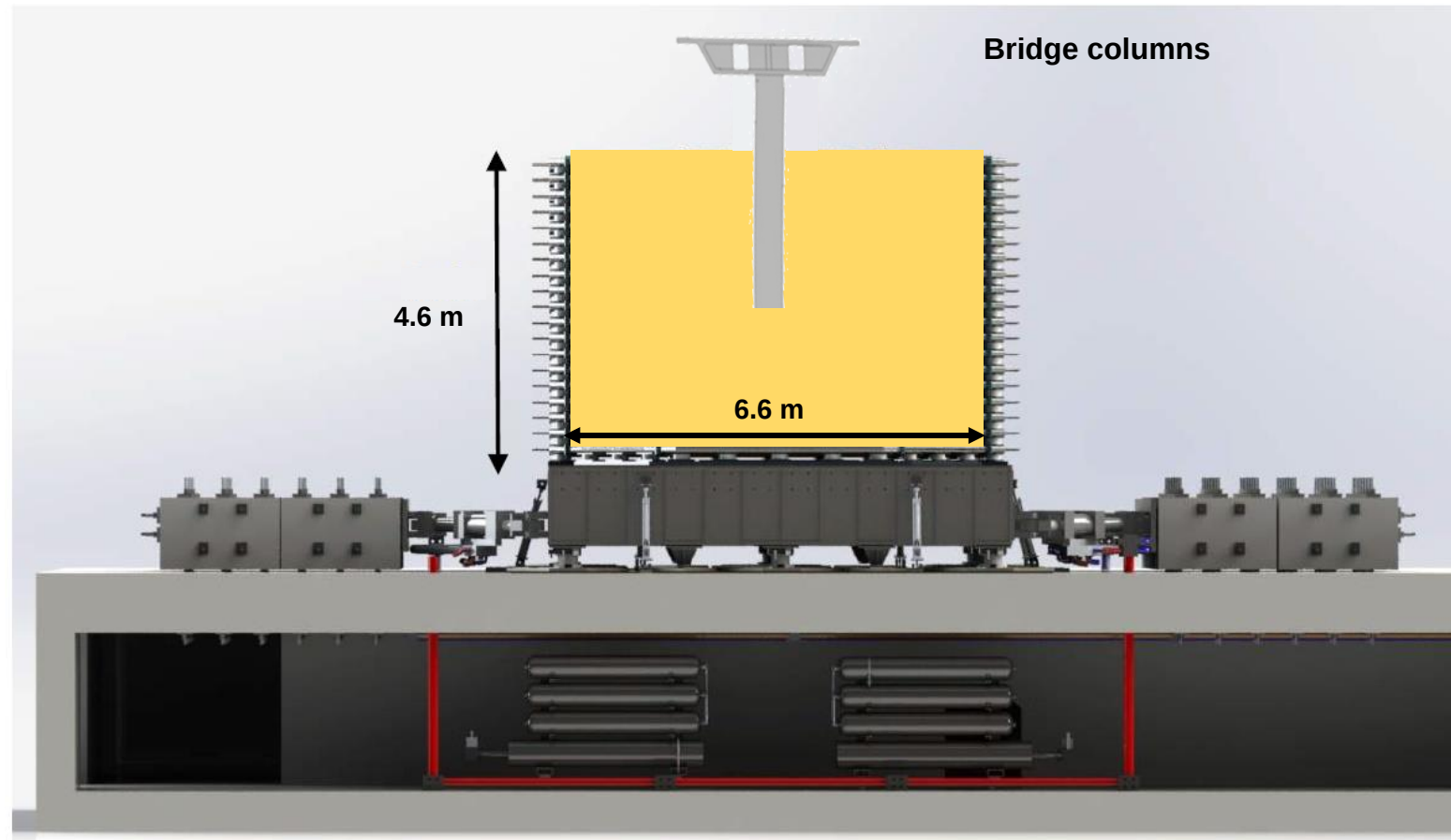
New shake table with big soil box University of Nevada, Reno



Important contributions to dynamic NLSSI



- Structural damage of RC elements
- Failure mechanisms of the system
- Kinematic and inertial interaction
- Soil properties
- Primary and secondary soil nonlinearity
- Damping (e.g. radiation)



Is the gap between geotechnical and structural engineers detrimental to solve NLSSI problems?

“If our small minds, for some convenience, divide this glass of wine, this universe, into parts -- physics, biology, geology, astronomy, psychology, and so on -- remember that nature does not know it! So let us put it all back together, not forgetting ultimately what it is for. Let it give us one more final pleasure; drink it and forget it all!”

Prof. Richard P. Feynman

Guido Andreotti^{1,2} - Assistant Professor (guido.andreotti@iusspavia.it)

Gian Michele Calvi^{1,2} - Professor (gm.calvi@iusspavia.it)

¹ University School for Advanced Studies IUSS Pavia, Piazza della Vittoria n.15, 27100 Pavia, Italy

² European Centre for Training and Research in Earthquake Engineering, Via A. Ferrata 1, 27100 Pavia, Italy

References (1/2)

1. Andreotti G., Calvi G.M., (2021). Design of laterally loaded pile-columns considering SSI effects: Strengths and weaknesses of 3D, 2D, and 1D nonlinear analysis. *Earthquake Engineering & Structural Dynamics*, 50(3):863-888.
2. Andreotti G., Lai C.G., (2019). Use of fragility curves to assess the seismic.
3. Andreotti G., Lai C.G., (2017a). A nonlinear constitutive model for beam elements with cyclic degradation and damage assessment for advanced dynamic analyses of geotechnical problems. Part I: theoretical formulation. *Bulletin of Earthquake Engineering*, 15(7): 2785–2801
4. Andreotti G., Lai C.G., (2017b). A nonlinear constitutive model for beam elements with cyclic degradation and damage assessment for advanced dynamic analyses of geotechnical problems. Part II: validation and application to a dynamic soil-structure interaction problem. *Bulletin of Earthquake Engineering*, 15(7):2803–2825.
5. ASCE 4-16, 2017 Edition, (2017). *Seismic Analysis of Safety-Related Nuclear Structures*.
6. Calvi G.M. , Moratti M., Dacarro F., Andreotti G., Bolognini D., (2021). Feasibility Study for In-situ Dynamic Testing of Structures and Geotechnical Systems. *Engineering Structures*, 235(112085).
7. Coleman J.L., Bolisetti C., Whittaker A.S., (2016). Time-domain soil-structure interaction analysis of nuclear facilities. *Nuclear Engineering and Design* 298: 264–270.
8. Cotecchia, V., 1986. Effects of the November 23, 1980 Earthquake on the lining of Pavoncelli tunnel, Apulian water supply, as related to soils in the area served by the system. *Proceedings of the International Congress on Large Underground Openings*, Florence, Italy.
9. Hoek E., Brown E., (1997) Practical estimates of rock mass strength. *Int J Rock Mech Min Sci* 34(8):1165–1186.
10. IAEA, (2020). *Advances in Small Modular Reactor Technology Developments*. A Supplement to: IAEA Advanced Reactors Information System (ARIS).
11. Janoyan K.D., Wallace J.W., Stewart J.P., (2006). Full-scale cyclic lateral load test of reinforced concrete pier-column. *ACI Struct J*. 2006;103(2s):178–187.

References (2/2)

12. Kari O.P., Puttonen J., (2014). Simulation of concrete deterioration in Finnish rock cavern conditions for final disposal of nuclear waste. *Annals of Nuclear Energy* 72:20–30.
13. Kennedy C., (2019). Delivering Hinkley Point C's cooling system – Tunnels. *New Civil Engineer*.
14. Li T., (2012). Damage to mountain tunnels related to the Wenchuan earthquake and some suggestions for aseismic tunnel construction. *Bulletin of Engineering Geology and the Environment*. 71(2):297–308.
15. Priestley M.J.N., Calvi G.M., Kowalsky M.J. (2007) Displacement-based seismic design of structures. IUSS Press, Pavia.
16. TEPCO, (2011). Press release: <https://www.tepco.co.jp/en/press/corp-com/release/11040203-e.html>
17. Wang J.N., (1993). Seismic Design of Tunnels: A State-of-the-Art Approach, Monograph 7. Parsons Brinckerhoff Quade & Douglas, Inc., New York, NY.
18. Wieland M., (2011). Seismic Aspects of Underground Structures of Hydropower Plants. First Asian and 9th Iranian Tunnelling Symposium, Tehran, Iran, November 1-2, 2011.
19. Wolf, J. P. (1985). Dynamic soil structure interaction, Prentice-Hall Inc.
20. Zou D., Sui Y., Chen K., (2020). Plastic damage analysis of pile foundation of nuclear power plants under beyond-design basis earthquake excitation. *Soil Dynamics and Earthquake Engineering* 136 – 106179