



# NGL Models for Triggering and Manifestation of Liquefaction

*PEER Annual Meeting*

*Banatao Auditorium, UC Berkeley | March 25, 2025*

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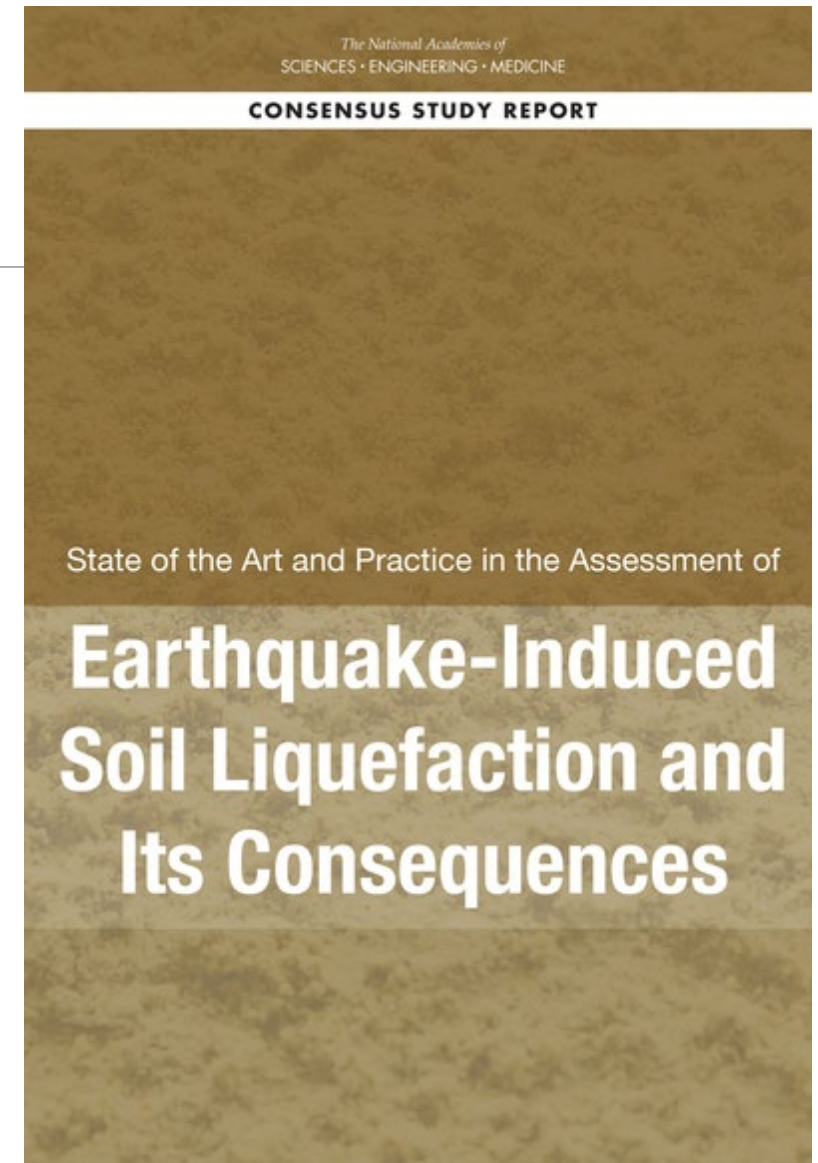
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Scott J. Brandenburg, Steven L. Kramer, and Jonathan P. Stewart



# NGL

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## Vision



# NGL

## Vision

Database – Supporting Studies –  
Model Development



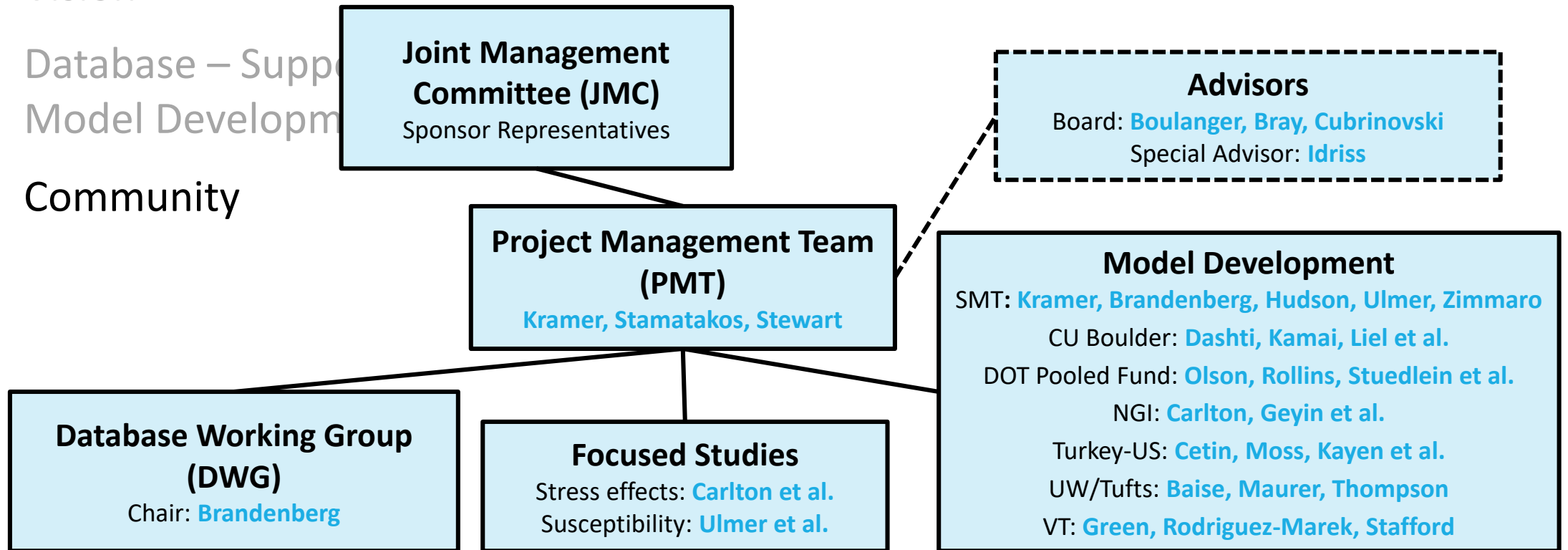
<https://nextgenerationliquefaction.org/>

# NGL

Vision

Database – Support  
Model Development

Community



# Modeling: General approach

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**NGL project provides unique opportunities relative to prior work:**

Data: more case histories, more information per case history, efficient utilization

Fully probabilistic: models account for and characterize epistemic uncertainty and aleatory variability

Ground motions: derived in a consistent manner to their evaluation in forward analyses (PSHA) for new and legacy events

Profile behavior: accounts for “system effects” on profile response (e.g. Cubrinovski et al. 2019)

# Terminology & Philosophy

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Susceptibility: potential of soil to experience significant pore pressure generation and strength loss; evaluated as a fundamental material characteristic.

Triggering: occurs in liquefaction-susceptible soils when the liquefaction demand exceeds capacity; produces high pore pressures and temporary strength loss.

Manifestation: surface evidence of liquefaction triggering (e.g., sediment ejecta, instabilities).

*Observed field performance = manifestation (or lack thereof) –  
should be distinguished from triggering*

# Outline

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Bayesian approach

Triggering “prior”  $P(T|S)$

Manifestation models derived from case histories

Updated  $P(T|S)$  model

# Outline

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## **Bayesian approach**

Triggering “prior”  $P(T|S)$

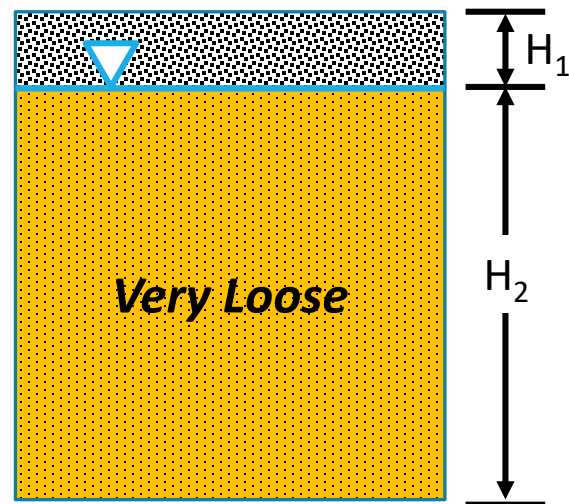
Manifestation models derived from case histories

Updated  $P(T|S)$  model



# Triggering and Manifestation

1) Manifestation observed



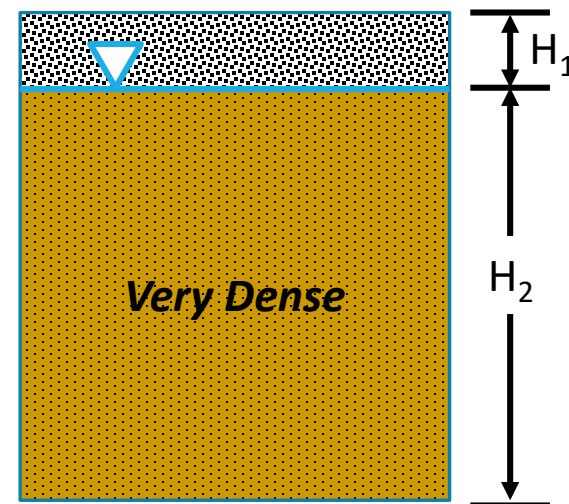
Thin crust, thick susceptible layer

$P[T]$  very high

$P[M|T]$  very high

$P[M] = P[M|T] P[T]$  very high

2) Manifestation **not** observed



Thin crust, thick susceptible layer

$P[T]$  very low

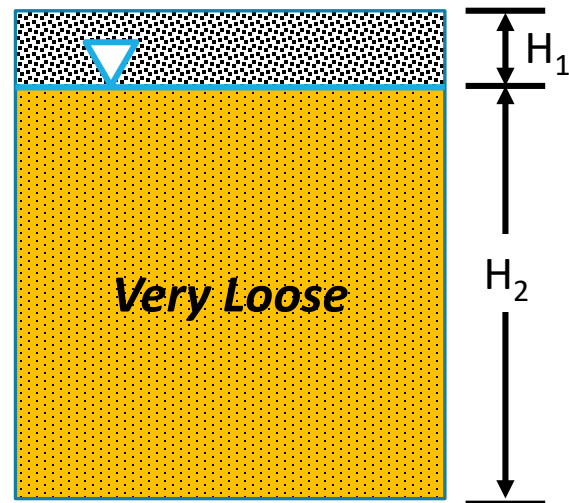
$P[M|T]$  high

$P[M] = P[M|T] P[T]$  very low

$P[NM] = 1 - P[M]$  very high

# Triggering and Manifestation

1) Manifestation observed



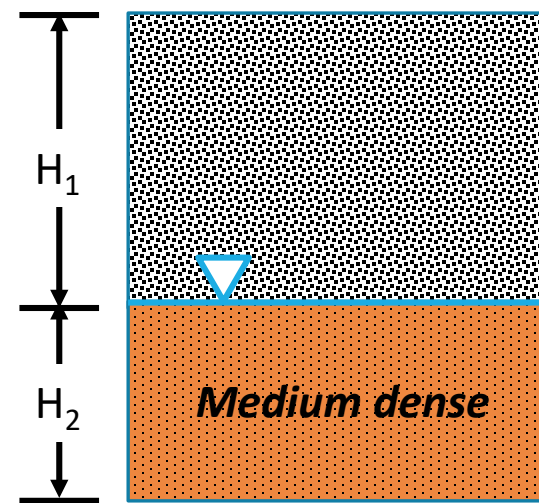
Thin crust, thick susceptible layer

$P[T]$  very high

$P[M|T]$  very high

$P[M] = P[M|T] P[T]$  very high

3) Manifestation **not** observed



Intermediate crust, Intermediate susceptible layer

$P[T]$  intermediate

$P[M|T]$  intermediate

$P[M] = P[M|T] P[T]$  intermediate

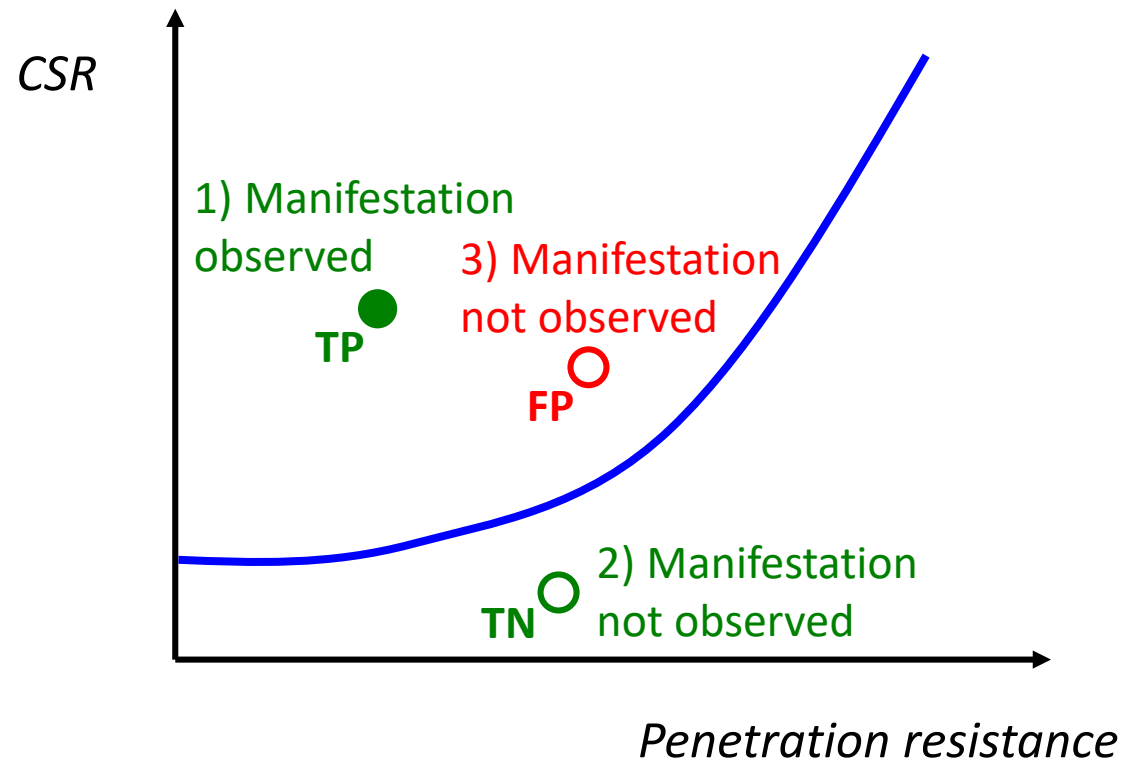
No manifestation – why not?  
Because soil was too dense to trigger?  
Because manifestation was inhibited?

# Triggering and Manifestation

Legacy models represent profile with a critical layer

Case histories plot as a point in CSR-PR space

Boundary curve typically interpreted as triggering “strength”



# Probabilistic Approach: Required Elements

## Bayes theorem:

$$P[T | M] = \frac{P[M | T]P[T]}{P[M]}$$

Need three probabilities:

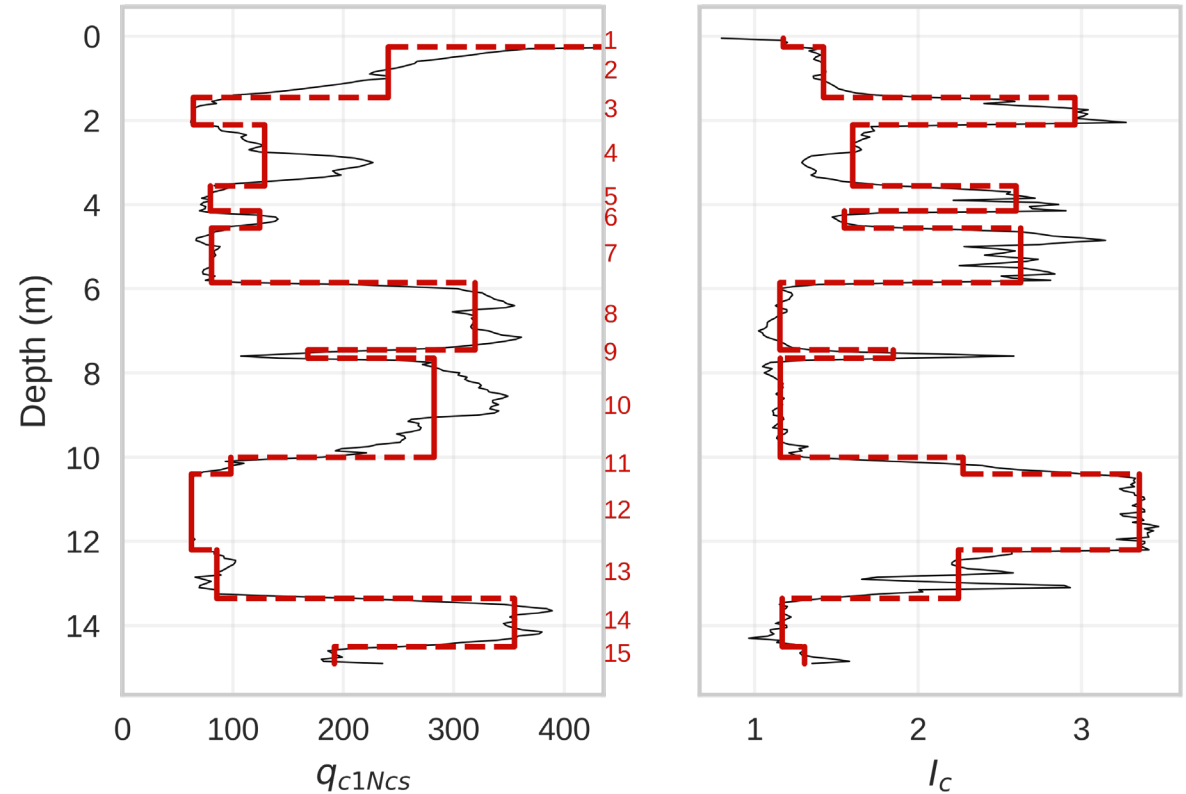
- Probability of manifestation given triggering,  $P[M | T]$
  - Probability of manifestation without triggering,  $P[M | NT]$
  - Probability of triggering before seeing this data,  $P[T]$  - prior probability
- } Probabilistic manifestation models

# Profile based approach

Automated discretization of CPT profiles (available at [ngl\\_tools](#))

Susceptibility and triggering evaluated layer-by-layer

Surface manifestation model derived using profile



*Hudson et al. (2023)*

# Modelling approach

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Bayesian approach

**Triggering “prior”  $P(T|S)$**

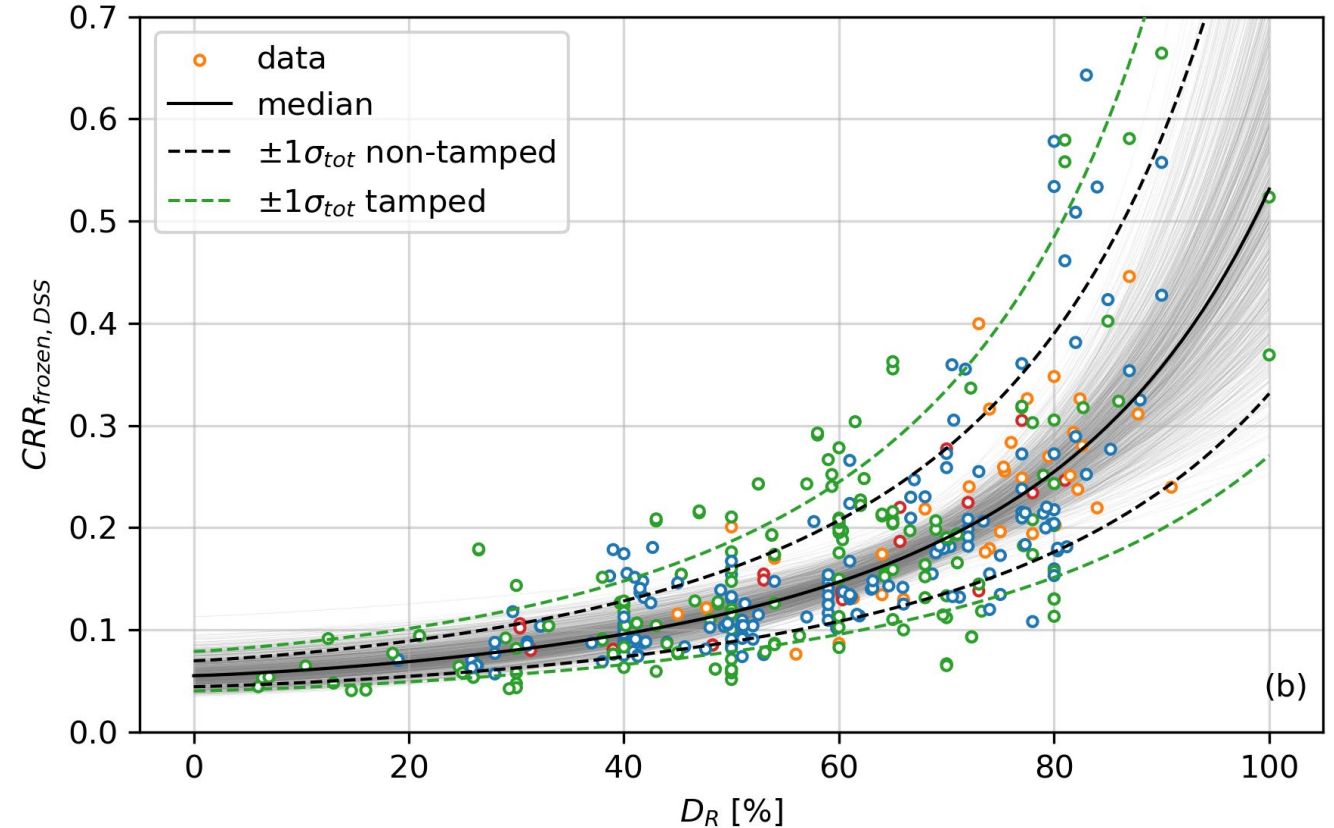
Manifestation models derived from case histories

Updated  $P(T|S)$  model

# Triggering prior

Derived from  
laboratory cyclic tests

Model developed for  
equivalent condition  
of intact sample &  
direct simple shear  
testing



# Modelling approach

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Bayesian approach

Triggering “prior”  $P(T|S)$

**Manifestation models derived from case histories**

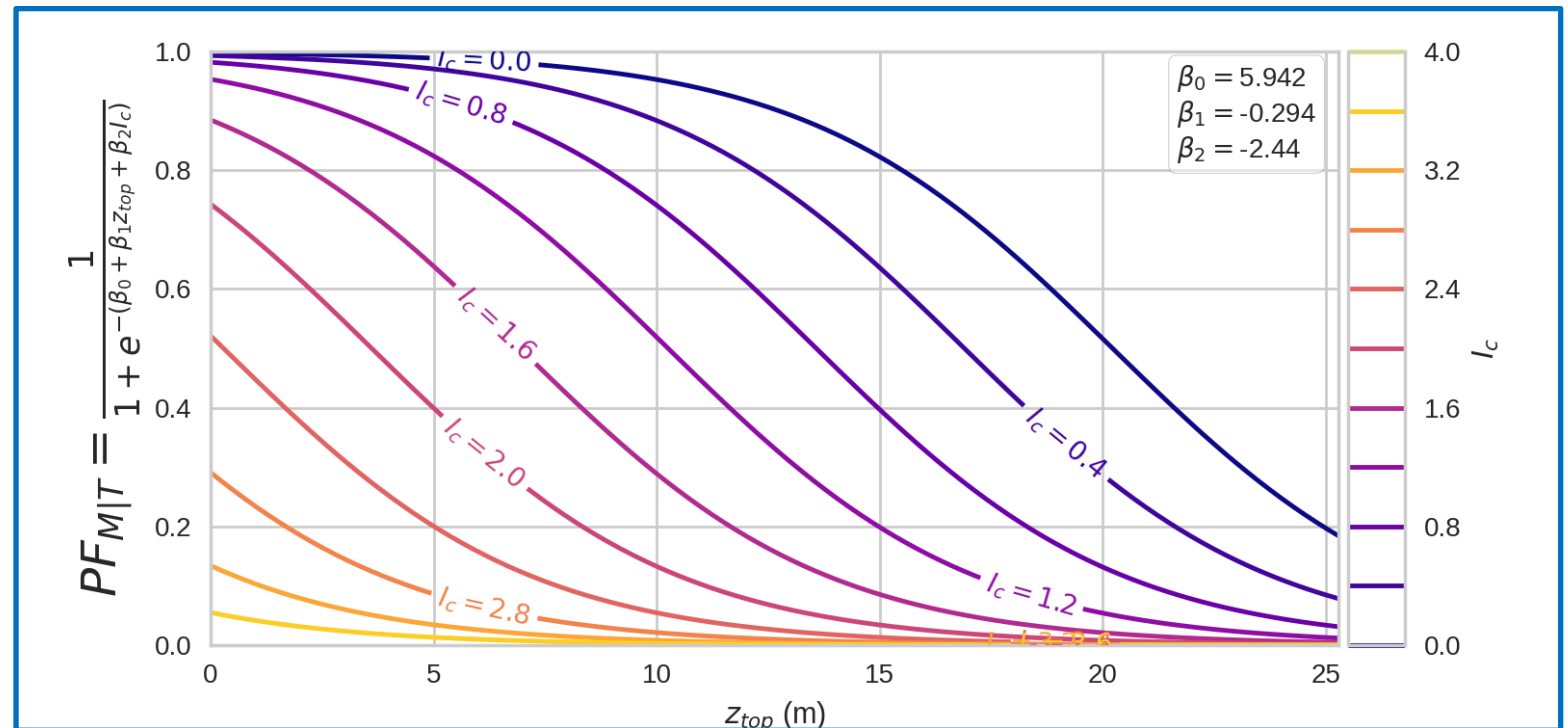
Updated  $P(T|S)$  model



# Probabilistic manifestation models

Derived from case history data  
using Bayesian updating

*Layer Manifestation Model*

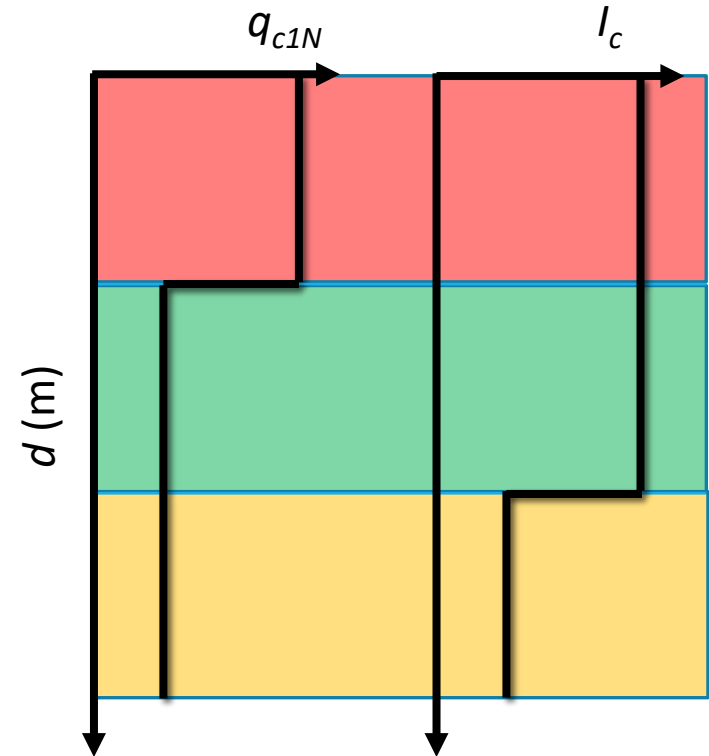


# Probabilistic manifestation models

## Model application

- Individual layers

### Three Layer Profile

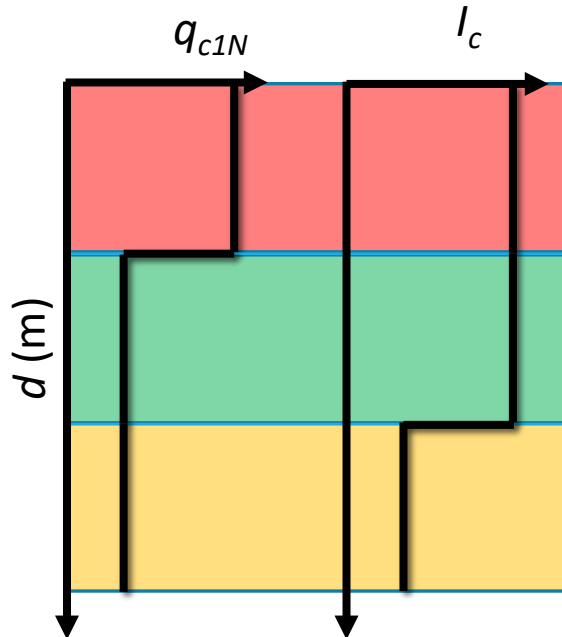


# Probabilistic manifestation models

## Model application

- Individual layers

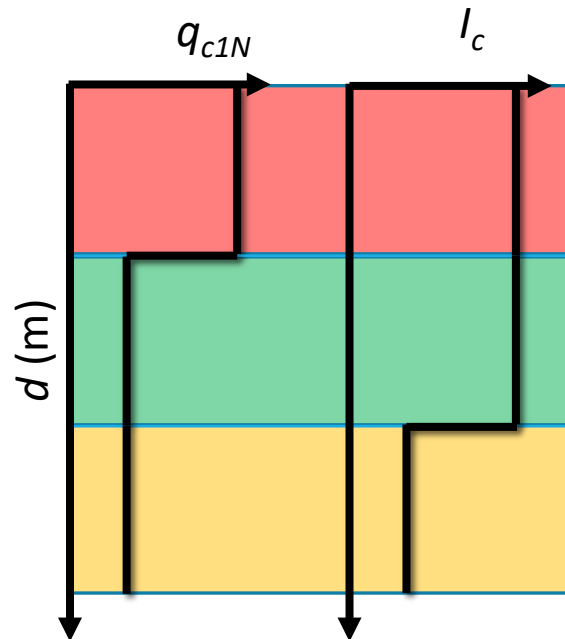
$$P[M_{j=1}^L | T_1^L, z_1, I_{c,1}]$$



# Probabilistic manifestation models

## Model application

- Individual layers



$$P[M_{j=1}^L | T_1^L, z_1, l_{c,1}]$$

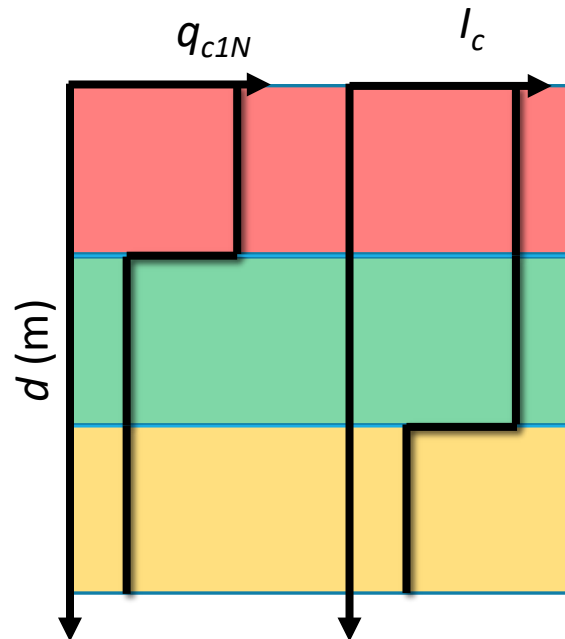
Depth:  $P[M_{j=1}^L | T_1^L, z_1, \dots] \sim \text{high}$  Shallow

$$P[M_{j=1,k}^L | T_{j=1,k}^L, x_{i=3,j=1,k}] \sim 0.2$$

# Probabilistic manifestation models

## Model application

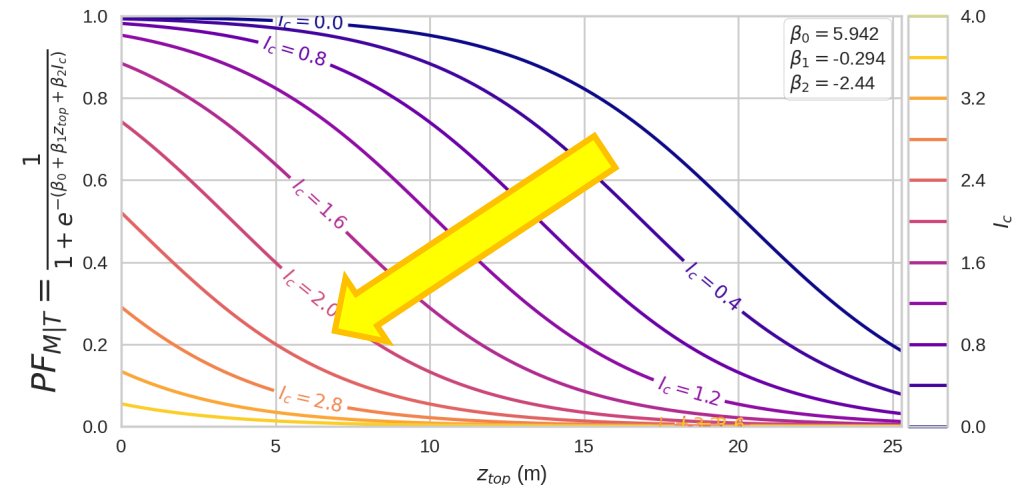
- Individual layers



$$P[M_{j=1}^L | T_1^L, z_1, I_{c,1}]$$

**Depth:**  $P[M_{j=1}^L | T_1^L, z_1, \dots] \sim \text{high}$  **Shallow**

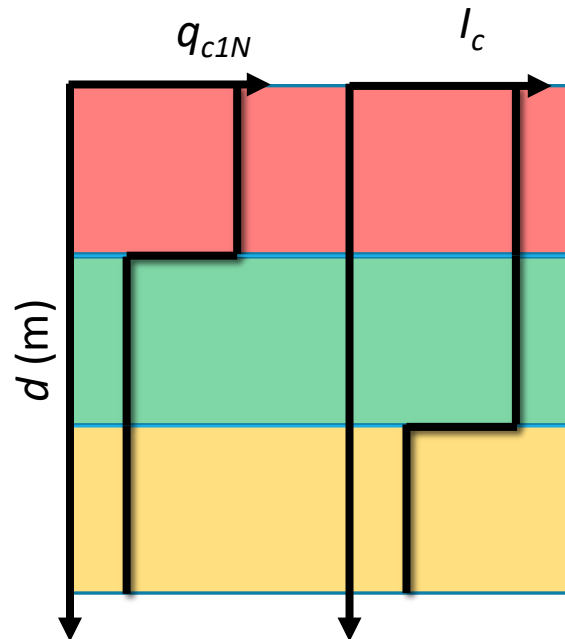
**$I_c$ :**  $P[M_{j=1}^L | T_1^L, \dots, I_{c,1}] \sim \text{low}$  **High**



# Probabilistic manifestation models

## Model application

- Individual layers

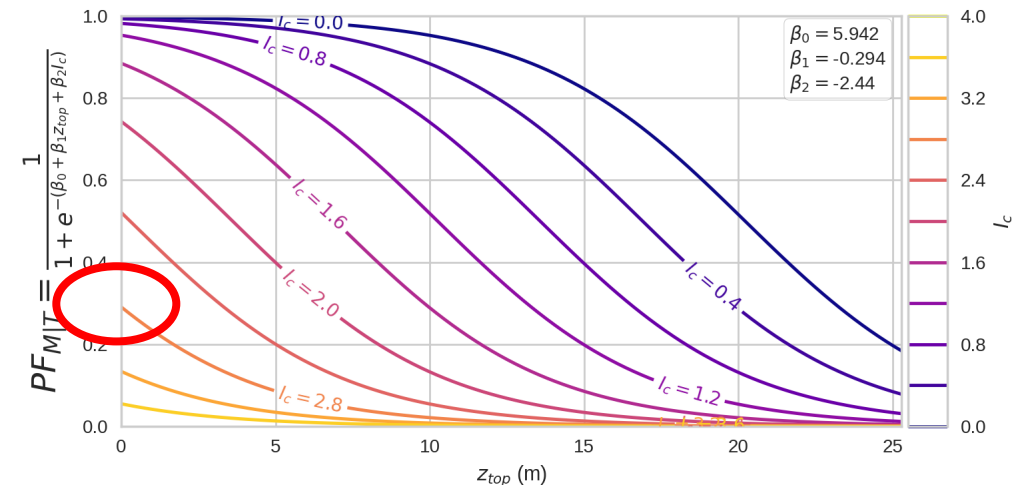


$$P[M_{j=1}^L | T_1^L, z_1, I_{c,1}]$$

**Depth:**  $P[M_{j=1}^L | T_1^L, z_1, \dots] \sim \text{high}$  **Shallow**

**$I_c$ :**  $P[M_{j=1}^L | T_1^L, \dots, I_{c,1}] \sim \text{low}$  **High**

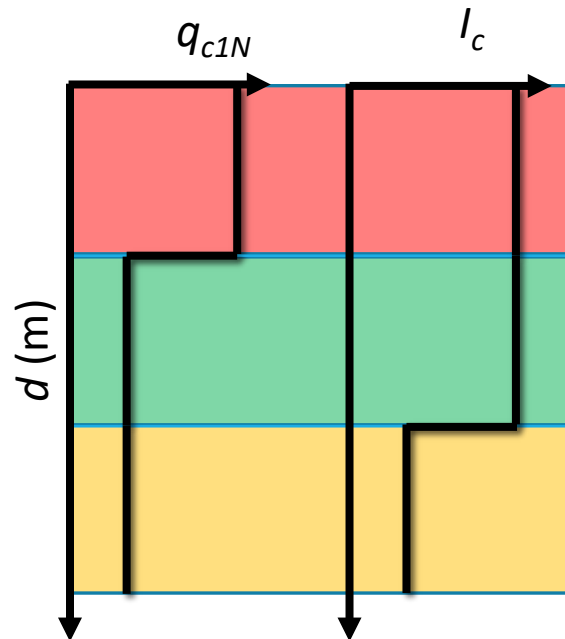
$$P[M_{j=1}^L | T_1^L, \dots] = 0.3$$



# Probabilistic manifestation models

## Model application

- Individual layers



$$P[M_{j=1}^L | T_1^L, z_1, I_{c,1}]$$

**Depth:**  $P[M_{j=1}^L | T_1^L, z_1, \dots] \sim \text{high}$  **Shallow**

**$I_c$ :**  $P[M_{j=1}^L | T_1^L, \dots, I_{c,1}] \sim \text{low}$  **High**

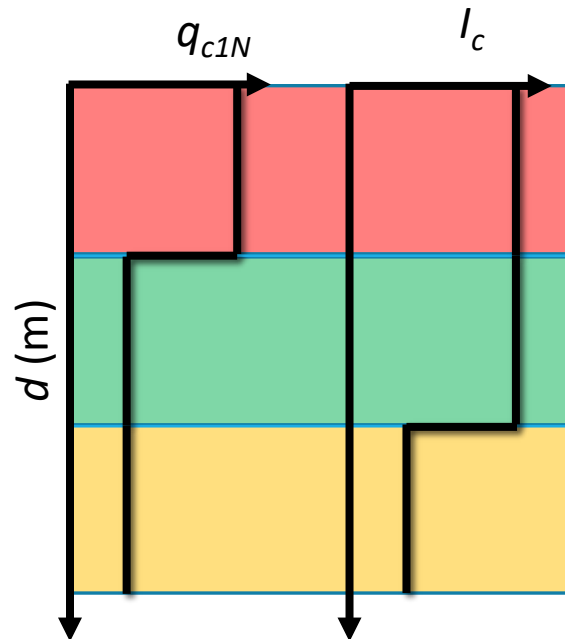
$$P[M_{j=1}^L | T_1^L, \dots] = 0.3$$

$$P[T_1^L] \sim 0.2 \therefore P[M_1^L] = 0.06$$

# Probabilistic manifestation models

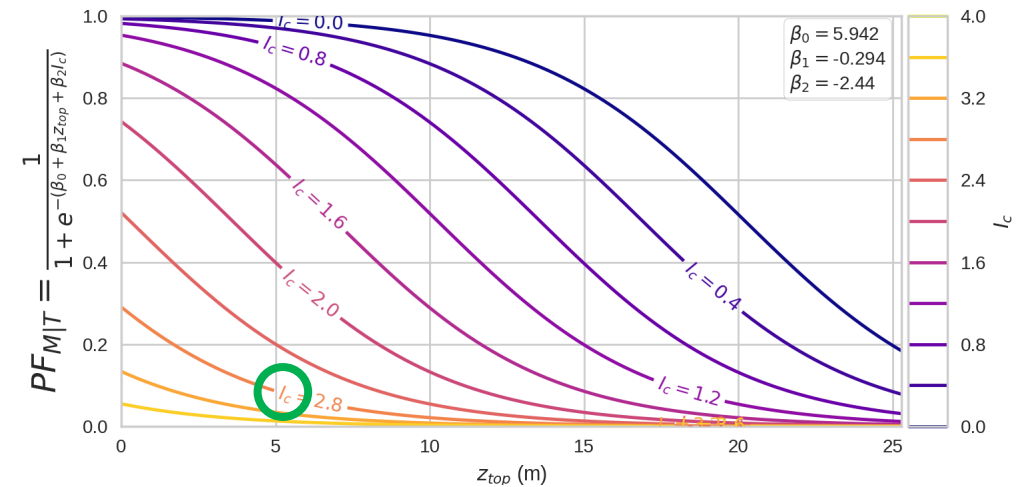
## Model application

- Individual layers



$$P[M_{j=2}^L | T_2^L, z_2, I_{c,2}] = 0.1$$

$$P[T_2^L] \sim 0.4 \therefore P[M_2^L] = 0.04$$

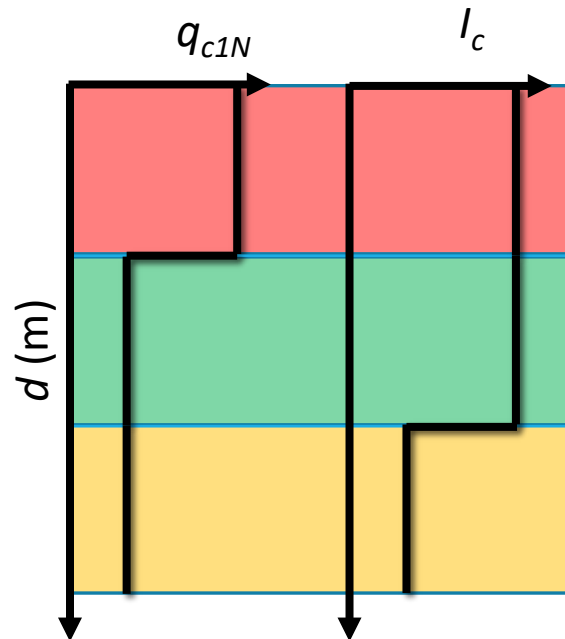




# Probabilistic manifestation models

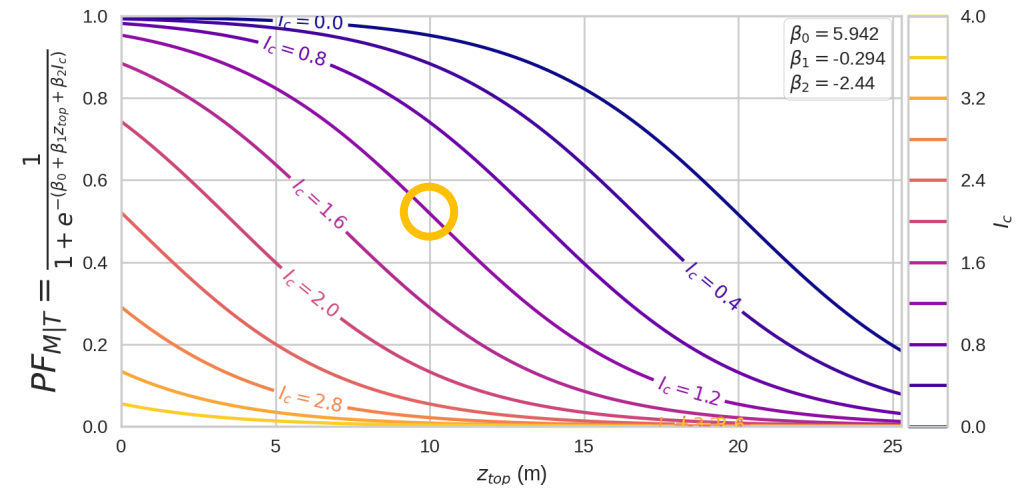
## Model application

- Individual layers



$$P[M_{j=3}^L | T_3^L, z_3, I_{c,3}] = 0.5$$

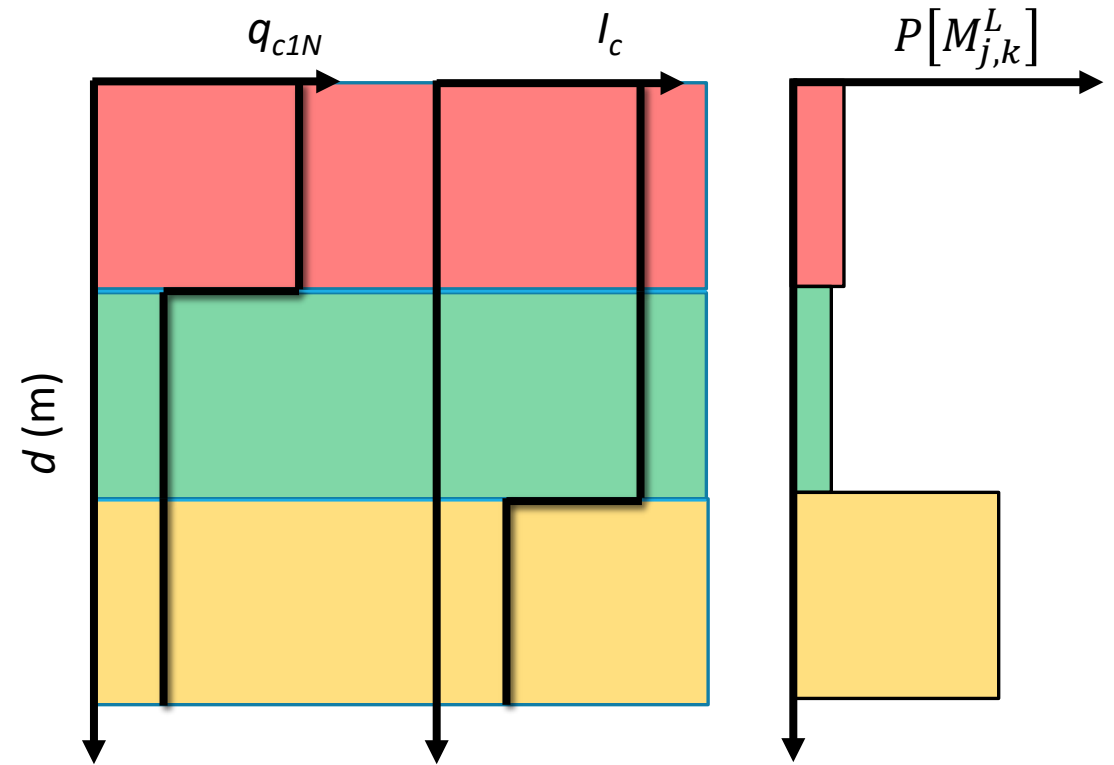
$$P[T_3^L] \sim 0.8 \therefore P[M_3^L] = 0.4$$



# Manifestation models

## Model application

- Individual layers
- Profile



$$P[M^P] = 1 - \prod_{j=1}^{N_L} (1 - P[M_j^L])$$

$$P[M^P] = 1 - (1 - 0.06) \cdot (1 - 0.04) \cdot (1 - 0.4)$$

$$P[M^P] = \mathbf{0.46}$$

# Manifestation models

## Model application

- Individual layers
- Profile

Characterizes field performance more accurately than legacy models (in particular, fewer FPs)

# Modelling approach

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Bayesian approach

Triggering “prior”  $P(T|S)$

Manifestation models derived from case histories

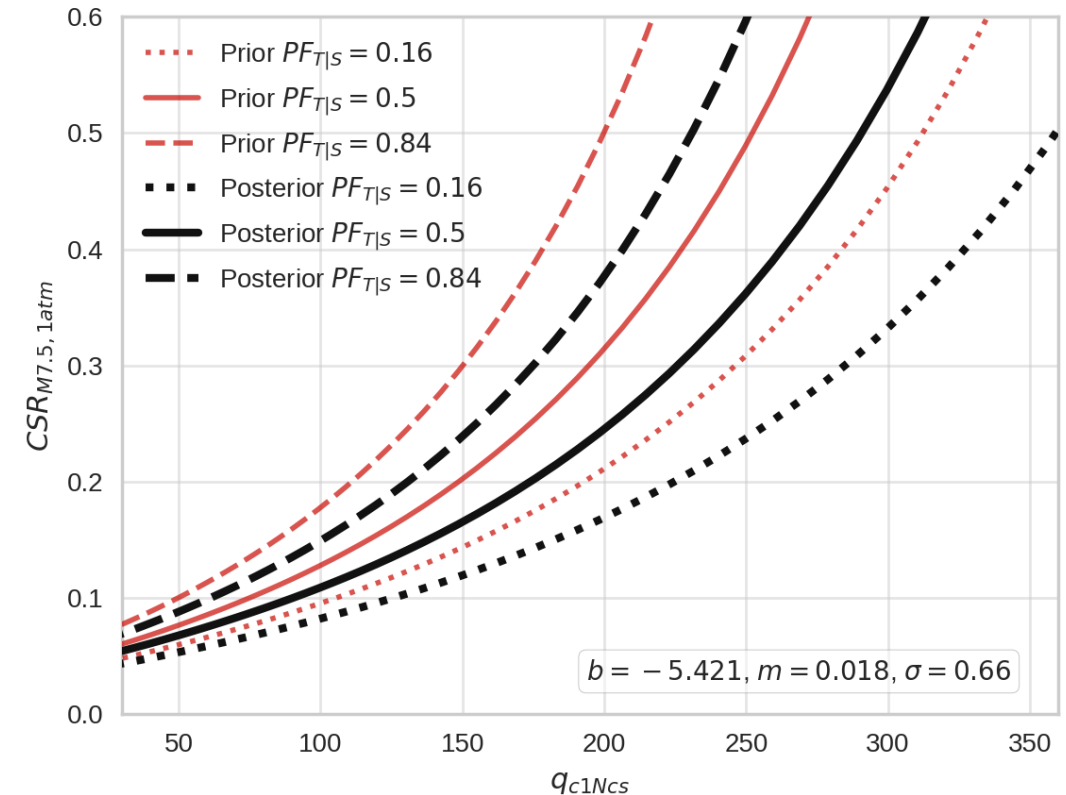
**Updated  $P(T|S)$  model**

# Updated triggering prior

Outcome of Bayesian updating

Slight downward shift, but difference from prior is not statistically significant

Influenced by assumed model components, especially fines correction



# Conclusions

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- Modeling approach unpacks triggering from manifestation
- Ongoing work revising susceptibility model and fines corrections – may shift triggering and manifestation models due to coupling
- Advantages of framework: (1) defined uncertainties; (2) alignment with field performance; (3) well suited for liquefaction effects analysis

# References

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## Databases, web tools:

Next Generation Liquefaction (NGL). <https://nextgenerationliquefaction.org>

NGL tools: DOI: 10.5281/zenodo.14004847

Upcoming workshop: EERI, May 17 2025, 1-5 pm, Oakland, CA. [Link](#)



***NGL Database***

Cubrinovski, M, A Rhodes, N Ntritsos, S Van Ballegooy (2019). System response of liquefiable deposits. *Soil Dynamics and Earthquake Engineering*, 124, 212-229.

Hudson, KS, KJ Ulmer, P Zimmaro, SL Kramer, JP Stewart, SJ Brandenberg (2023). Unsupervised machine learning for detecting soil layer boundaries from cone penetration test data, *Earthquake Engineering and Structural Dynamics*, 52(11),3201-3215.

Ulmer, KJ, KS Hudson, SJ Brandenberg, P Zimmaro, R Pretell, B Carlton, SL Kramer, and JP Stewart (2024). [Next Generation Liquefaction models for susceptibility, triggering, and manifestation, Rev 1](#). U.S. Nuclear Regulatory Commission, *RIL 2024-13*. ML24268A229