

Uncertainty Propagation in the Seismic Collapse Risk for Single-Family Wood-frame Residences

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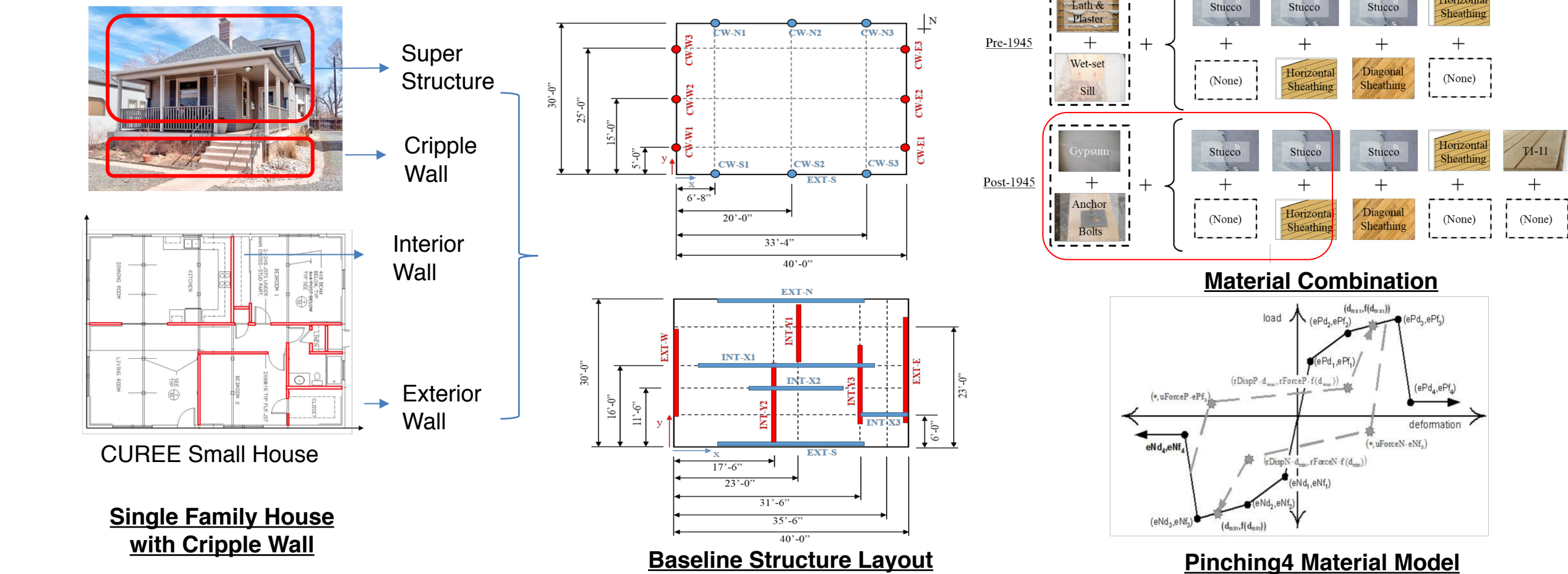
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1. Motivation & Introduction

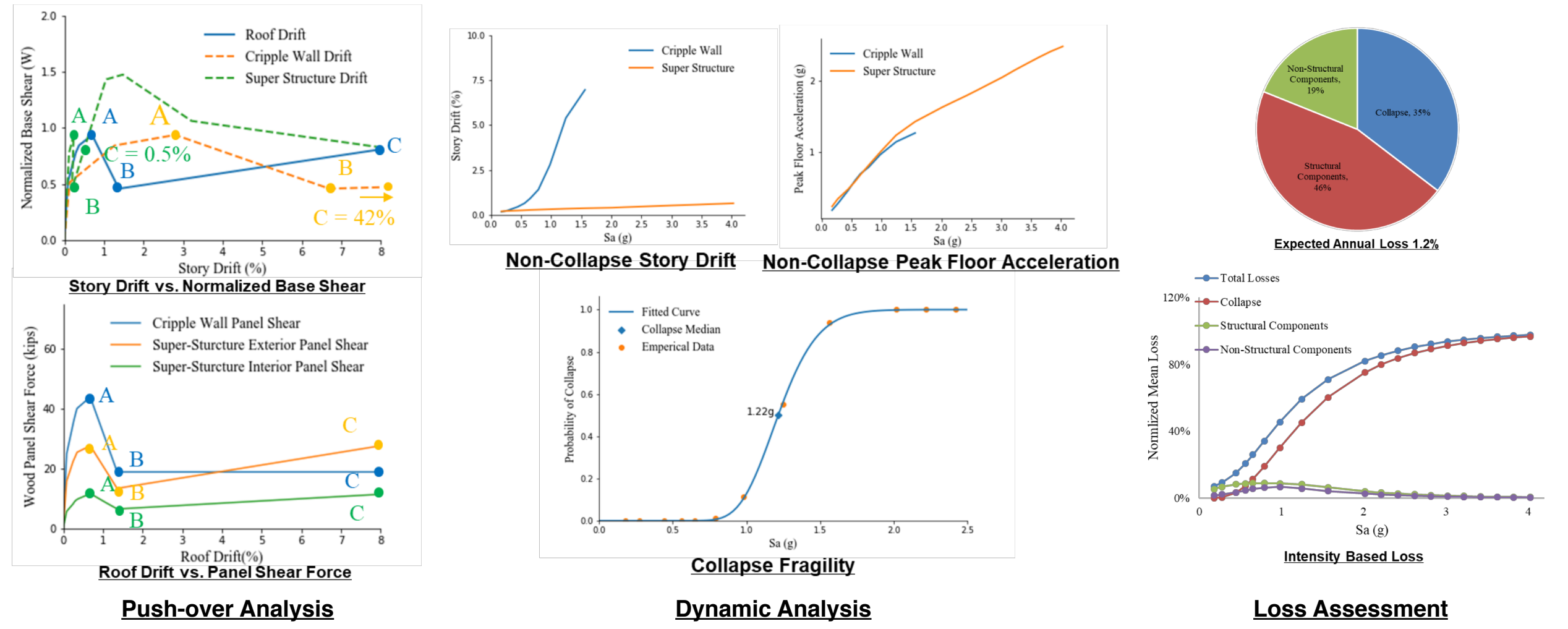
- Buildings constructed with adjacent stories having large differences in strength and stiffness can lead to the formation of a single-story mechanism during earthquake shaking. This type of behavior is undesirable because inelastic deformation is concentrated in a few non-ductile components of a single story instead of being distributed along the height of the building, which can lead to sideways collapse.
- Policy actions are often implemented to mitigate the effects soft-story vulnerabilities. A major challenge with developing such guidelines is being able to adequately capture the variations in structural configurations and material properties of the affected structures. Furthermore, multiple sources of uncertainties (i.e. structure dimensions, construction quality) must be addressed when developing retrofit techniques than can be generalized for a given portfolio. Furthermore, the tools, methods and guidelines that are currently available primarily designing retrofits to provide adequate strength and inelastic deformation capacities. However, within the framework of performance-based seismic design (PBSD) (Moehle & Deierlein, 2004), little or no consideration is given to earthquake-induced economic losses.

2. Building Prototype and Sample Analysis

OpenSees Model Summary



Analysis Results Summary



Parameter Variations

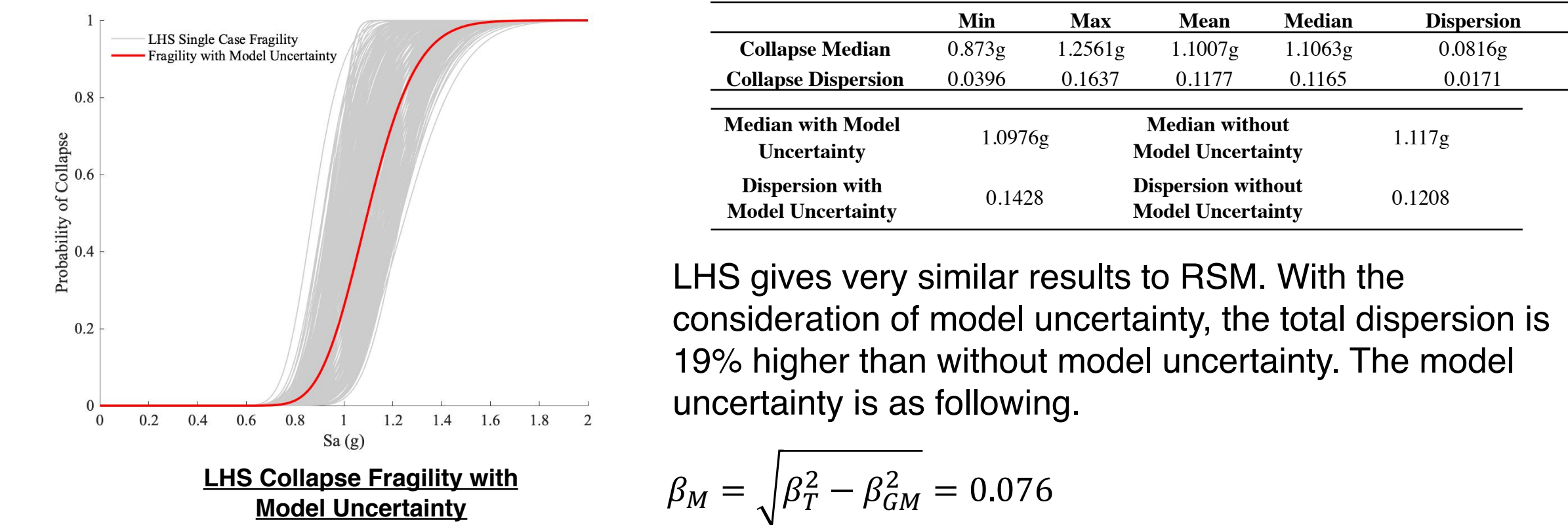
To propagate the model uncertainty, the above building prototype is used. Parameter variations are shown in the right table.

Parameter Name	Distribution	Range
Cripple Wall Height	Uniform	[2ft, 7ft]
Gypsum Deformation Shift	Normal	
Gypsum Force Amplification	Normal	
Gypsum-stucco Deformation Shift	Normal	
Gypsum-stucco Force Amplification	Normal	
Stucco Deformation Shift	Normal	
Stucco Force Amplification	Normal	
Roof Weight	Uniform	[13psf, 20psf]

4. Uncertainty Propagation: Latin Hypercube Sampling (LHS)

Latin Hypercube Sampling Uncertainty Propagation

As an improvement to traditional Monte Carlo method, Latin Hypercube Sampling (LHS) can control the random samples distributed more evenly so that the effective sample size can be reduced. Considering the same parameter variations as RSM, for each parameter, using LHS to generate 500 samples. Then randomly group all the parameters to generate 500 different building models. Through performing nonlinear response history analysis (NRHA), the number of collapse cases are collected at each intensity level. By accumulate all the collapse cases from all 500 cases, a collapse fragility with model uncertainty can be fitted and the total uncertainty is the fragility dispersion.

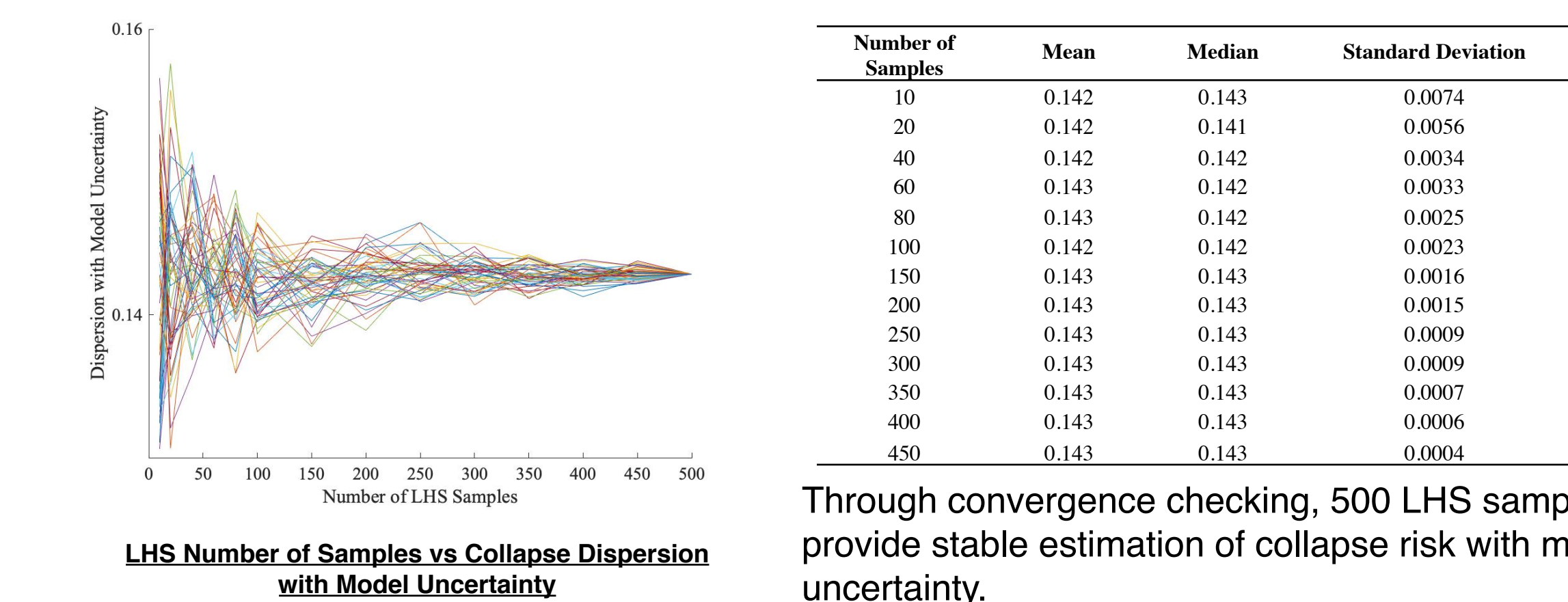


LHS gives very similar results to RSM. With the consideration of model uncertainty, the total dispersion is 19% higher than without model uncertainty. The model uncertainty is as following.

$$\beta_M = \sqrt{\beta_T^2 - \beta_{CM}^2} = 0.076$$

Latin Hypercube Sampling Convergence Check

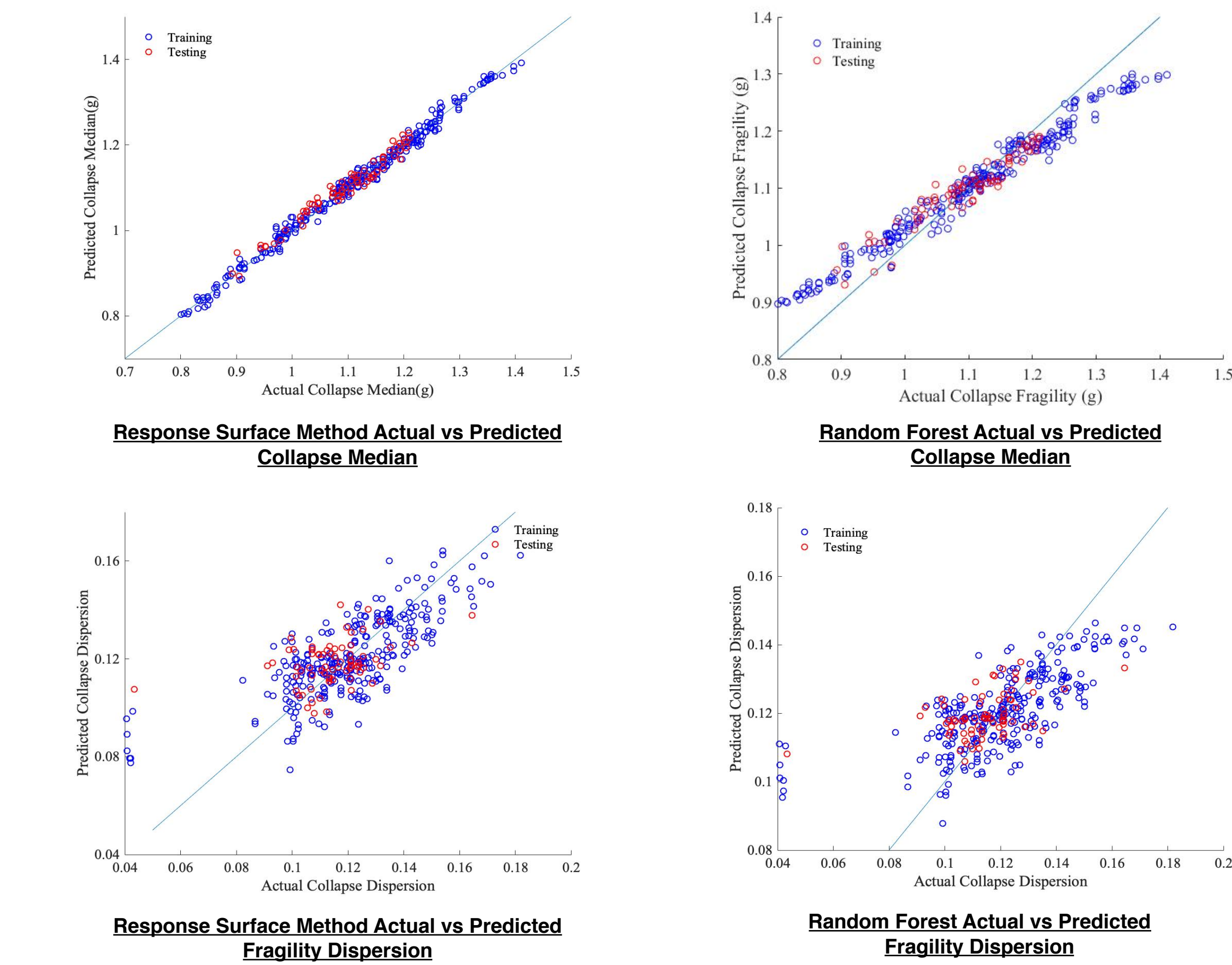
LHS provides with a way to propagate uncertainties, but the number of required samples cannot be estimated before the analysis. Large number of samples should be first tried and convergence is checked.



3. Uncertainty Propagation: Surrogate Models

Development and Verification Surrogate Models

Response Surface Methodology and Random Forest are investigated to model the relationships between building parameters and structure seismic collapse risk. To reduce computational expense and meanwhile develop reliable statistical models, Central Composite Design (CCD) is adopted. Variations in 8 building collapse performance critical parameters are considered, including cripple wall height, roof weight, material force and displacement parameters. The primary focused response parameters are collapse median intensity and dispersion. Besides 289 training set generated using CCD, another separated 70 cases are developed to verify the statistical models.



Using Surrogate Model to Perform Uncertainty Propagation

Through comparing Response Surface Method (RSM) with Random Forest (RF), RSM can provide with unbiased and more reliable predictions. Consequently, RSM is selected to perform uncertainty propagation. Monte Carlo method is adopted, 500 random samples are generated and the corresponding collapse medians and dispersions are computed. At each intensity level, collapse or non-collapse are decided based on the probability of collapse, then accumulate all 500 cases to develop collapse fragility with model uncertainty.

	Min	Max	Mean	Median	Dispersion
Collapse Median	0.8424g	1.3156g	1.1058g	1.1095g	0.0859g
Collapse Dispersion	0.0852	0.1703	0.1209	0.1208	0.0113

Median with Model Uncertainty	1.1027g	Median without Model Uncertainty	1.117g
Dispersion with Model Uncertainty	0.1440	Dispersion without Model Uncertainty	0.1208

With the consideration of model uncertainty, the dispersion is about 20% higher than the dispersion without model uncertainty, which is a dramatic difference in terms of collapse risk. Using the dispersion with and without model uncertainty, model uncertainty can be computed by subtract the ground motion uncertainty.

$$\beta_M = \sqrt{\beta_T^2 - \beta_{CM}^2} = 0.079$$

5. Conclusion

- Statistical models and Latin Hypercube Sampling can be used to quantify the model uncertainties in wood-frame building single family residence collapse performance. Both method can reach an agreement to the propagated uncertainty.
- For the current building prototype, with the consideration of model uncertainty, the total dispersion would increase about 20%, which makes a difference in building seismic performance.
- For statistical models, Response Surface Method is more robust than Random Forest, because it gives unbiased predictions.
- For the purpose of uncertainty quantification, Response Surface Method is computationally less intensive than Latin Hypercube Sampling Method, because it requires about 40% less nonlinear history analysis than LHS.

