

# PACIFIC EARTHQUAKE ENGINEERING RESEARCH CENTER

## Verification of Probabilistic Seismic Hazard Analysis Computer Programs

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### ABSTRACT

Probabilistic seismic hazard analysis (PSHA) has become a fundamental tool in assessing seismic hazards and for estimating seismic design and seismic safety evaluation of ground motions. It is used both on a site-specific basis for important and critical facilities and on a national scale for building codes. This report describes a project to test and verify the numerical approaches and software used in PSHA. The project was sponsored by the Pacific Earthquake Engineering Research (PEER) Center's Lifelines Program. A Working Group was organized and members tested their own computer codes in two sets of tests. Through several iterations, codes were tested and acceptable answers were established either through analytical solutions or as the consensus answer from the test case results. The verification tests are available to any PSHA code developer/user worldwide through this publication and the PEER website. The test cases will be used as a standard verification for all PSHA codes to be used in projects for the PEER Lifelines Program sponsors, which include the California Department of Transportation (Caltrans), the Pacific Gas & Electric Company (PG&E), and the California Energy Commission (CEC).

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### CONTENTS

ABS	STRA	АСТ	iii
AC	KNO	WLEDGMENTS	iv
TA	BLE	OF CONTENTS	V
LIS	T OF	F FIGURES	vii
LIS	T OF	F TABLES	xi
1	INT	<b>FRODUCTION</b>	1
2 APPROACH			
	2.1	Verification Process	7
	2.2	General PSHA Theory	8
3	TES	ST CASES AND RESULTS	11
	3.1	Test Case Set 1	11
	3.2	Test Case Set 2	21
4	CO	NCLUSIONS	25
RE	FERI	ENCES	27
API	PENI	DIX A	

### LIST OF FIGURES

Figure 3.1	Fault and Site Geometry for Test Case Set 1	A-17
Figure 3.2	Test Set 1, Case 1, Site 1	A-18
Figure 3.3	Test Set 1, Case 1, Site 2	A-19
Figure 3.4	Test Set 1, Case 1, Site 3	
Figure 3.5	Test Set 1, Case 1, Site 4	A-21
Figure 3.6	Test Set 1, Case 1, Site 5	A-22
Figure 3.7	Test Set 1, Case 1, Site 6	
Figure 3.8	Test Set 1, Case 1, Site 7	A-24
Figure 3.9	Test Set 1, Case 1, Site 1, Early Results	A-25
Figure 3.10	Test Set 1, Case 2, Site 1	A-26
Figure 3.11	Test Set 1, Case 2, Site 2	A-27
Figure 3.12	Test Set 1, Case 2, Site 3	A-28
Figure 3.13	Test Set 1, Case 2, Site 4	A-29
Figure 3.14	Test Set 1, Case 2, Site 5	A-30
Figure 3.15	Test Set 1, Case 2, Site 6	A-31
Figure 3.16	Test Set 1, Case 2, Site 7	A-32
Figure 3.17	Test Set 1, Case 3, Site 1	A-33
Figure 3.18	Test Set 1, Case 3, Site 2	A-34
Figure 3.19	Test Set 1, Case 3, Site 3	A-35
Figure 3.20	Test Set 1, Case 3, Site 4	A-36
Figure 3.21	Test Set 1, Case 3, Site 5	A-37
Figure 3.22	Test Set 1, Case 3, Site 6	A-38
Figure 3.23	Test Set 1, Case 3, Site 7	A-39
Figure 3.24	Test Set 1, Case 4, Site 4, Early Results	A-40
Figure 3.25	Test Set 1, Case 4, Site 6, Early Results	A-41
Figure 3.26	Test Set 1, Case 4, Site 1	A-42
Figure 3.27	Test Set 1, Case 4, Site 2	A-43
Figure 3.28	Test Set 1, Case 4, Site 3	A-44
Figure 3.29	Test Set 1, Case 4, Site 4	A-45
Figure 3.30	Test Set 1, Case 4, Site 5	A-46

Figure 3.31	Test Set 1, Case 4, Site 6	
Figure 3.32	Test Set 1, Case 4, Site 7	
Figure 3.33	Test Set 1, Case 5, Site 4, Early Re	sultsA-49
Figure 3.34	Test Set 1, Case 5, Site 1	
Figure 3.35	Test Set 1, Case 5, Site 2	
Figure 3.36	Test Set 1, Case 5, Site 3	
Figure 3.37	Test Set 1, Case 5, Site 4	
Figure 3.38	Test Set 1, Case 5, Site 5	
Figure 3.39	Test Set 1, Case 5, Site 6	
Figure 3.40	Test Set 1, Case 5, Site 7	
Figure 3.41	Test Set 1, Case 6, Site 1	
Figure 3.42	Test Set 1, Case 6, Site 2	
Figure 3.43	Test Set 1, Case 6, Site 3	
Figure 3.44	Test Set 1, Case 6, Site 4	
Figure 3.45	Test Set 1, Case 6, Site 5	
Figure 3.46	Test Set 1, Case 6, Site 6	
Figure 3.47	Test Set 1, Case 6, Site 7	
Figure 3.48	Test Set 1, Case 7, Site 6, Early Re	sultsA-64
Figure 3.49	Test Set 1, Case 7, Site 1	
Figure 3.50	Test Set 1, Case 7, Site 2	
Figure 3.51	Test Set 1, Case 7, Site 3	
Figure 3.52	Test Set 1, Case 7, Site 4	
Figure 3.53	Test Set 1, Case 7, Site 5	
Figure 3.54	Test Set 1, Case 7, Site 6	
Figure 3.55	Test Set 1, Case 7, Site 7	
Figure 3.56	Test Set 1, Case 8a, Site 1	
Figure 3.57	Test Set 1, Case 8a, Site 2	
Figure 3.58	Test Set 1, Case 8a, Site 3	
Figure 3.59	Test Set 1, Case 8a, Site 4	
Figure 3.60	Test Set 1, Case 8a, Site 5	
Figure 3.61	Test Set 1, Case 8a, Site 6	
Figure 3.62	Test Set 1, Case 8a, Site 7	

Figure 3.63	Test Set 1, Case 8b, Site 1	A-79
Figure 3.64	Test Set 1, Case 8b, Site 2	2
Figure 3.65	Test Set 1, Case 8b, Site 3	3
Figure 3.66	Test Set 1, Case 8b, Site 4	4
Figure 3.67	Test Set 1, Case 8b, Site 5	5
Figure 3.68	Test Set 1, Case 8b, Site 6	бА-84
Figure 3.69	Test Set 1, Case 8b, Site 7	7
Figure 3.70	Test Set 1, Case 8c, Site 1	
Figure 3.71	Test Set 1, Case 8c, Site 2	2
Figure 3.72	Test Set 1, Case 8c, Site 3	3 A-88
Figure 3.73	Test Set 1, Case 8c, Site 4	4
Figure 3.74	Test Set 1, Case 8c, Site 5	5 A-90
Figure 3.75	Test Set 1, Case 8c, Site 6	5
Figure 3.76	Test Set 1, Case 8c, Site 7	7
Figure 3.77	Test Set 1, Case 9a, Site 1	A-93
Figure 3.78	Test Set 1, Case 9a, Site 2	2
Figure 3.79	Test Set 1, Case 9a, Site 3	3 A-95
Figure 3.80	Test Set 1, Case 9a, Site 4	۲-96 A-96
Figure 3.81	Test Set 1, Case 9a, Site 5	5 A-97
Figure 3.82	Test Set 1, Case 9a, Site 6	5
Figure 3.83	Test Set 1, Case 9a, Site 7	7
Figure 3.84	Test Set 1, Case 9b, Site 1	A-100
Figure 3.85	Test Set 1, Case 9b, Site 2	2
Figure 3.86	Test Set 1, Case 9b, Site 3	3
Figure 3.87	Test Set 1, Case 9b, Site 4	4A-103
Figure 3.88	Test Set 1, Case 9b, Site 5	5
Figure 3.89	Test Set 1, Case 9b, Site 6	5
Figure 3.90	Test Set 1, Case 9b, Site 7	7 A-106
Figure 3.91	Test Set 1, Case 9c, Site 1	A-107
Figure 3.92	Test Set 1, Case 9c, Site 2	2
Figure 3.93	Test Set 1, Case 9c, Site 3	6
Figure 3.94	Test Set 1, Case 9c, Site 4	A-110

Figure 3.95	Test Set 1, Case 9c, Site 5	A-111
Figure 3.96	Test Set 1, Case 9c, Site 6	A-112
Figure 3.97	Test Set 1, Case 9c, Site 7	A-113
Figure 3.98	Test Set 1, Case 10, Site 1	A-114
Figure 3.99	Test Set 1, Case 10, Site 2	A-115
Figure 3.100	Test Set 1, Case 10, Site 3	A-116
Figure 3.101	Test Set 1, Case 10, Site 4	A-117
Figure 3.102	Test Set 1, Case 11, Site 1	A-118
Figure 3.103	Test Set 1, Case 11, Site 2	A-119
Figure 3.104	Test Set 1, Case 11, Site 3	A-120
Figure 3.105	Test Set 1, Case 11, Site 4	A-121
Figure 3.106	Fault and Site Geometry for Cases 1 and 5	A-122
Figure 3.107	Test Set 2, Case 1, Site 1, Early Results	A-123
Figure 3.108	Fault and Site Coordinates for Case 2	A-124
Figure 3.109	Test Set 2, Case 2, Site 1, Early Results	A-125
Figure 3.110	Fault and Site Geometry for Cases 3 and 4	A-126
Figure 3.111	Test Set 2, Case 3, Site 1, Early Results	A-127
Figure 3.112	Test Set 2, Case 4, Site 1, Early Results	A-128
Figure 3.113	Logic Tree for Case 5	A-129
Figure 3.114	Test Set 2, Case 5, Site 1, Early Results	A-130
Figure 3.115	Fault and Site Geometry for Case 6	A-131
Figure 3.116	Test Set 2, Case 6, Site 1, Early Results	A-132
Figure 3.117	Intraslab Zone and Site Geometry for Case 7	A-133
Figure 3.118	Test Set 2, Case 7, Site 1, Early Results	A-134

### LIST OF TABLES

Table 2.1	PSHA code properties	4
Table 3.1	Test case set 1	13
Table 3.2	Median PGA values at sites 1–7	15

## 1 Introduction

In the past three decades, the approach to estimating earthquake ground shaking hazard, particularly to critical and important facilities, has slowly evolved from the traditional deterministic earthquake scenario analysis to probabilistic seismic hazard analysis (PSHA). A prime example is the very comprehensive PSHA that was performed to evaluate both ground shaking and fault displacement hazards at Yucca Mountain, the site of the nation's first nuclear waste repository (Stepp et al. 2001). The National Seismic Hazard Maps developed by the U.S. Geological Survey (USGS), which form the basis of building codes in the U.S. (e.g., International Building Code) are based on PSHA (Frankel et al. 1996; Petersen et al. 2008). Thus PSHA has become the primary tool in estimating seismic hazards in the U.S. and is gaining widespread use worldwide.

The results from PSHA also form the basis for (1) design ground motions specified in structural codes and standards (e.g., AASHTO for bridges); (2) site-specific design of important and critical facilities such as all U.S. Department of Energy facilities (e.g., national laboratories and Yucca Mountain); (3) site-specific design for nuclear power plants and interim nuclear waste storage sites; (4) safety analysis evaluations of important/critical facilities such as U.S. Bureau of Reclamation dams; (5) loss estimation to establish insurance rates; and many other uses. PSHA is now being used by federal and state agencies, which have traditionally used only a deterministic approach for estimating ground motions. Examples of such agencies are the U.S. Army Corps of Engineers and the California Division of Safety of Dams.

PSHA has its roots in the seminal paper by Cornell (1968). The objective in PSHA is to estimate the probability that a specified level of ground motion will be exceeded or to estimate the level of ground motions that will occur at a specified exceedance probability. PSHA integrates hazard from all significant seismic sources and incorporates the frequency of earthquakes from each seismic source. A significant aspect of PSHA is that it allows for the explicit treatment of uncertainty in the inputs. The uncertainties can be quite large in characterizing seismic sources and ground motion attenuation. For a comprehensive discussion of PSHA, we refer the reader to the EERI monograph *Seismic Hazard and Risk Analysis* by McGuire (2004) or the Senior Seismic Hazard Advisory Committee (1997) report.

Despite the relatively widespread use both nationally and internationally of PSHA, only a few publicly available and proprietary PSHA computer codes have been developed. In large part, this is because PSHA calculations are still being done by a relatively small proportion of the professional community. Because of the importance of PSHA in seismic design, the Pacific Earthquake Engineering Research (PEER) Center's Lifelines Program sponsored a Working Group to verify both the numerical approaches and computer software used in PSHA. To our knowledge, this is the first ever comprehensive, organized, and structured verification of PSHA software. This project is one of several projects sponsored by the PEER Center's Lifelines Program to improve tools in seismic hazard estimation. The goal of the Lifelines Program is to increase the safety and reliability of utility and transportation systems in earthquakes through better characterization of the hazards and improved performance of system components.

The objective of the project was to develop a set of standard exercises that can be used by current and future PSHA software developers to validate their codes. The verification process will also provide the means for the PEER Lifelines Program sponsors (the California Department of Transportation, the Pacific Gas and Electric Company, and the California Energy Commission) to ensure that work done for them by others, including consultants, is done using qualified software.

The following describes the two test case sets developed for verification, the final results for Test Case Set 1, and the sample results for Test Case Set 2.

## 2 Approach

The PSHA Validation Project was managed by Ivan Wong and Patricia Thomas (co-Principal Investigators) with assistance from Norm Abrahamson. Members of the Working Group consisted of prominent code developers from government agencies and engineering and risk analysis and management services firms. The members of the Working Group and their computer programs included:

Member	Affiliation	Program	
Tianqing Cao	California Geological Survey	haz02	
Ned Field	U.S. Geological Survey	OpenSHA	
Steve Harmson	U.S. Geological Survey	hazFX v.3f, hazgridX v 3.f,	
Steve Hamisen	0.5. Geological Sulvey	fltrate.peer.f	
Roland LaForge	U.S. Bureau of Reclamation	faultsource_20, mrs 3.1	
Robin McGuire	Risk Engineering	EZ-FRISK	
Andres Mendez	Impact Forecasting	EQ-Elements	
Badie Rowshandel	California Geological Survey	HAZDIR	
Joon Source	Lawrence Livermore National	ALEAS	
Jean Savy	Laboratory		
Mark Stirling	New Zealand Institute of Geological	NEWHAZ	
Mark Stirling	and Nuclear Sciences		
Phalkun Tan	GeoPentech	GP-Haz	
Gabriel Toro	Risk Engineering	FRISK88M Version 2.05	
Bob Youngs	Geomatrix Consultants	XCD52, HAZ50, TREE50	

The Working Group tested both publicly available codes as well as proprietary codes that have been used extensively in hazard evaluation in the U.S. and worldwide. Basic attributes of the various codes are listed in Table 2.1. Three publicly available codes were tested: EZ-FRISK developed by Risk Engineering, Inc.; HAZ38 developed by Norm Abrahamson; and OpenSHA developed by the U.S. Geological Survey. The former is a widely used code both in the U.S. and internationally. HAZ38 was tested by the PIs. OpenSHA was tested by Ned Field. The basic codes used in the development of the U.S. Geological Survey's National Hazard Maps were

tested by Steve Harmsen. The project began in November 2001. A paper that described the early stages of the project was published in 2004 (Wong et al. 2004).

Code	Numerical Model	Truncation Of Ground Motion	Rupture Plane Modeling	Rupture Length & Width Modeling
FRISK88M Version 2.0 G. Toro	Polynomial (26.2.17 of Abramowitz & Stegun)	# Standard Deviations Max. Ground Motion	Horizontal location & hypocentral depth is uniformly distributed. Rupture confined to fault plane.	User inputs Log L = a+bM and std. dev. User-specified std dev Width = ratio * length User specified ratio Length & width not to exceed fault plane
EZ-FRISK R. McGuire	Polynomial (26.2.17 of Abramowitz & Stegun)	# Standard Deviations Max. Ground Motion	Horizontal location & hypocentral depth is uniformly distributed. Rupture confined to fault plane.	User inputs Log L = a+bM and std. dev. User-specified std. dev. Width = ratio * length. User specified ratio. Length & width not to exceed fault plane.
XDC52, HAZ50, TREE50 B. Youngs	Series expansion	# Standard Deviations	Uniform distribution along length. User specified hypocentral depth distribution. For straight-line fault, analytical distance distribution computed. For segmented fault, numerical distribution using 1 km steps. Rupture confined to fault plane	Rupture area specified by log- linear relationship with magnitude. Aspect ratio defined by log linear relationship, 1:1 for M 4, user specified for M 7. Aleatory variability not modeled.
HazFX v3.f, hazgridX v3.f, filtrate.peer.f A. Frankel S. Harmsen	Call to the error function	# Standard Deviations. For CEUS relations, can also truncate at maximum ground motion.	Rupture floats along strike. Rupture confined to fault plane.	For gridded seismicity code, use W&C Magnitude-Length relations. For fault code, rupture always extends from top to bottom (Mmin=6.5). No variability in rupture length or width.
ALEAS J. Savy	Abramowitz polynomial approximation	# Standard Deviations Max. Ground Motion	Monte-Carlo simulation with model of initiation point based on probability distributions of depth and location along the fault. User notified if rupture extends off fault plane.	Rupture area is simulated from set of weighted area-magnitude relations. Area is positioned using distributions on depth and location of initiation point.
EQ-Elements A. Mendez	Discrete numerical integration of equation	# Standard Deviations Max. Ground Motion (Code uses both at the same time.)	Rupture centroid is uniformly distributed along length. Depth of centroid is a function of the magnitude.	Log10(A)=m-4.2 (USGS 99- 517) Use Abrahamson (written communication 1992) to determine width and length.

 Table 2.1a
 PSHA code properties

Code	Numerical Model	Truncation Of Ground Motion	Rupture Plane Modeling	Rupture Length & Width Modeling
GP-Haz P. Tan	Series approximation	# Standard Deviations	Rupture location is discretized uniformly on fault plane. The distance between 2 discrete points can be specified. Rupture location is truncated such that ½ the dimension of the plane does not extend beyond the ends of the fault.	Rupture area calculated first from W&C. Next, rupture length is calculated from W&C. Width is calculated as the ratio of area to length. No aleatory variability is included.
NEWHAZ M. Stirling	Call to error function (For PC code, this uses polynomial expression 7.1.26 in Abramowitz & Stegun.)	# Standard Deviations	Rupture extends to the ends of the fault segment (characteristic model for all faults). Ruptures can overlap by calculating recurrence parameters so that they balance the slip rate. No rupture extends beyond the ends of the fault.	No aleatory variability in length or width. Epistemic uncertainty by modeling overlapping ruptures (that balance the slip rate).
faultsource-20 mrs 3.1 R. LaForge	Discrete numerical integration directly from the equation	# Standard Deviations	EQs are modeled as square (or any other aspect ratio) rupture areas. As many areas as possible are sequenced on plane starting in one corner. Pattern can be shifted along strike and dip as many times as necessary to achieve stable results	The normal distribution of rupture area as a function of magnitude (W&C) can be incorporated.
OpenSHA N. Field	Gamma Series	# Standard Deviations Maximum ground motion	Rupture floats along or down dip. Rupture constrained to fault plane.	Uses M(A) relationships. Aleatory variability can be accommodated.
HAZDIR B. Rowshandel	Direct numerical integration	Standard Deviations	Rupture is confined to fault surface. Rupture floats along strike and across width. Homogeneous rupture with unidirectional directivity effects. Heterogeneous rupture based on asperity and slip distribution. Single hypocenter and random hypocenter with specified distribution are handled.	Rupture area and length are calculated from magnitude. Rupture width is calculated from magnitude or using aspect ratio. Aleatory variability can be included.

 Table 2.1a—Continued

Code	Magnitude Density Functions	Area Source Modeling
FRISK88M	AREAS: Truncated exponential, modified	Point source is default. Hypocenter depth fixed
Version 2.0	exponential (Youngs et al. 1987).	or random, with user-specified distribution; can
G. Toro	FAULTS: Truncated exponential, modified	also include effect of rupture width on depth
	exponential (Youngs et al. 1987), characteristic	distribution. Effect of rupture length for
	(user-specified width and ratio between exponential	modeled background sources can be by
	and characteristic portion; rate is specified as total	randomizing rupture orientation or calculating
	recurrence rate or slip rate). Can model boxcar	distance to rupture or using analytical
	distribution as a special case of characteristic or	approximation.
	exponential distributions.	
EZ-FRISK	AREAS: Truncated exponential, modified AREAS:	Point source is default. Hypocenter depth fixed
R. McGuire	Truncated exponential, modified exponential	or random, with user-specified distribution; can
	(Youngs et al. 1987).	also include effect of rupture width on depth
	FAULTS: Truncated exponential, modified	distribution. Effect of rupture length for
	exponential (Youngs et al. 1987), characteristic	modeled background sources can be by
	(user-specified width and ratio between exponential	randomizing rupture orientation or calculating
	and characteristic portion; rate is specified as total	distance to rupture or using analytical
	recurrence rate or slip rate). Can model boxcar	approximation.
	distribution as a special case of characteristic or	
	exponential distributions.	
XDC52, HAZ50,	Truncated exponential	Area sources are modeled using closely spaced
TREE50	Modified truncated exponential (Youngs et al. 1987)	faults.
B. Youngs	Characteristic with variable width (Youngs and	
	Coppersmith)	
	Separate exponential characteristic components with	
	user specified rates	
	Discrete frequencies for individual magnitude	
	Increments Real time makehilities for gravified time revied	
HogEV v2 f	For gridded seignicity and use truncated	Ear griddod gaigmiaity goda, ghava M=6.0 yaa
$\Pi dZ \Gamma \Lambda V J.I,$	For gridded seisificity code, use trutcated	For gridded seismicity code, above M-0.0 use
filtrate poor f	Ear fault and also have a maximum magnitude	contored on each grid point with fixed donth
A Frankel	model	For $M \le 6.0$ use point sources
S. Harmsen	model.	For W<0.0 use point sources.
ALEAS	Truncated exponential	Area sources modeled as horizontal planes
I Savy	Characteristic models:	The sources modered as nonzontal planes.
J. Savy	Standard Youngs and Connersmith	
	Segmented model of the types developed by	
	WG99 (Input slip rates probabilities of	
	segmentations segment lengths with uncertainty on	
	their endings & lengths).	
	Completely empirical occurrence curve defined at	
	magnitude points, with uncertainty.	
EQ-Elements	Truncated exponential	Area sources are modeled as faults.
A. Mendez	Characteristic	When a-value, b, & Mmax known over a spatial
		grid, faults are randomly generated over grid.
		When input is "complete" EO catalog, a-value is
		calculated over a spatial grid through the use of
		an elliptical spatial weighting function applied
		to each event. EQ events are generated as in (a).
		When area is polygon, the area is filled with
		faults such that the seismicity follows the input
		distributions. "Hard" (all EQs in polygon) and
		"Soft" (EQs can rupture beyond polygon edge).
		Can enter preferred azimuth.

### Table 2.1b PSHA code properties

Code	Magnitude Density Functions	Area Source Modeling
GP-Haz	Truncated exponential (truncation applied to	Area sources are modeled as line sources
P. Tan	density function).	(multi-linear lines on surface) and multi-planar
	Characteristic (Youngs and Coppersmith)	sources (planar sources defined by 3 multi-
		linear lines).
NEWHAZ	Truncated exponential (truncation applied to	Area sources are modeled as a series of point
M. Stirling	density function).	sources, with the ability to use an adaptation of
	Characteristic (assumes one EQ size that is	the Frankel Gaussian smoothing function.
	proportional to dimensions of the fault).	
faultsource-20	Exponential	Area sources are modeled as point sources with
mrs 3.1	Characteristic	fixed grid spacing. Depths are modeled as a
R. LaForge	Maximum Moment	triangular distribution with peak and maximum
		depth specified, with a near-surface
		modification.
N. Field	Dirac delta.	Area sources are modeled as grid points on a
	Gaussian with optional truncation.	horizontal plane.
	Truncated exponential (truncation on density	
	function).	
HAZDIR	Truncated exponential, Gaussian, characteristic	Area sources are modeled as point sources with
B. Rowshandel	(single magnitude), Characteristic (Youngs and	fixed grid spacing distributed over any shape
	Coppersmith), Characteristic with aleatory	area. Horizontal source with uniform depth and
	uncertainty on M <sub>ch</sub> modeled using normal	dipping source with variable depth. Capable of
	probability density function.	Gaussian smoothing, as used in the USGS
		National Hazard maps.

#### 2.1 VERIFICATION PROCESS

The focus of the project was the numerical verification of the codes, and analysis and comparison of their various features. The verification exercises consisted of two sets of cases that tested fundamental aspects of the codes including how they modeled (1) faults, areal sources, and complex fault geometries, (2) recurrence models and rates, and (3) attenuation relationships and their uncertainties. The test cases ranged from the simplest to more sophisticated. The simplest cases have analytical solutions, but the more complex cases do not. "Acceptable" answers to the test cases were defined either through comparisons with the analytical solutions or the means over all results.

The test case sets were developed by the PIs and were distributed to each member of the Working Group. Each member initially ran the test cases and sent their results back to the PIs. The results were compiled for the whole Working Group and sent back to each participant without identifying the names of the codes except for their own code. This initial feedback allowed for each code developer to identify numerical errors, errors in interpretations, or

limitations in their codes and the opportunity to correct them. In some cases, this resulted in modifications of the codes. For each test case set, the above steps were followed and a workshop was held to discuss the group results, to identify discrepancies and the reasons for them, particularly if differences were due to differences in assumptions, numerical solutions, and hence features of the codes. Recommendations of minimum standards for meeting the benchmark results (e.g., 10% in probability level) were also defined to qualify the hazard codes.

A total of five workshops were held by the Working Group to discuss and evaluate the results of the two test case sets. Several iterations of running the test cases were required by the Working Group members. In some cases, test cases required re-running because of misinterpretations of the tests as well as software errors. Because of the extended duration of the project, schedule conflicts and change in affiliations prevented some of the Working Group members (Cao, Harmsen, Savy, and Stirling) from completing the test cases.

The major differences between the individual results, however, were due to differences in numerical approaches in the codes. For example, possibly the most significant difference among the Working Group members was the approach in modeling rupture areas for events smaller than the total fault area. In particular, the way the rupture area is moved along the length and width of a fault led to significant differences in the PSHA results. Some developers allowed the rupture area to extend beyond the fault. Some pushed the rupture area back onto the fault, while others tapered the slip at the edges. Some of the large differences were found to be an initial lack of clearly defined test cases (i.e., artificially set sigma to zero, not truncate sigma at zero). Other issues encountered in the test cases were the implementation of hanging wall/footwall factor in the Abrahamson and Silva (1997) attenuation relationship, the modeling of nonplanar faults with depth, and the lower limit of integration of the hazard (e.g., Mmin or negative infinity). The magnitude step size used in the test cases also led to differences in the test cases.

#### 2.2 GENERAL PSHA THEORY

The standard PSHA approach is based on the model developed principally by Cornell (1968). The occurrence of earthquakes on a fault is assumed to be a Poisson process. The Poisson model is widely used and is a reasonable assumption in regions where data are sufficient to provide only an estimate of average recurrence rate (Cornell 1968). When there are sufficient data to permit a real-time estimate of the occurrence of earthquakes, the probability of exceeding a given

value can be modeled as an equivalent Poisson process in which a variable average recurrence rate is assumed. The occurrence of ground motions at the site in excess of a specified level is also a Poisson process if (1) the occurrence of earthquakes is a Poisson process and (2) the probability that any one event will result in ground motions at the site in excess of a specified level is independent of the occurrence of other events.

The probability that a ground motion parameter "Z" exceeds a specified value "z" in a time period "t" is given by:

$$\mathbf{p}(Z > z) = 1 - \mathrm{e}^{-\mathbf{v}(z) \cdot \mathbf{t}} \tag{2.1}$$

where v(z) is the annual mean number (or rate) of events in which Z exceeds z. It should be noted that the assumption of a Poisson process for the number of events is not critical. This is because the mean number of events in time t,  $v(z) \bullet t$ , can be shown to be a close upper bound on the probability p(Z > z) for small probabilities (less than 0.10) that generally are of interest for engineering applications. The annual mean number of events is obtained by summing the contributions from all sources, that is:

$$\mathbf{v}(z) = \sum_{n} \mathbf{v}_{n}(z) \tag{2.2}$$

where  $v_n(z)$  is the annual mean number (or rate) of events on source n for which *Z* exceeds *z* at the site. The parameter  $v_n(z)$  is given by the expression:

$$\mathbf{v}_{\mathbf{n}}(z) = \sum_{i} \sum_{j} \beta_{\mathbf{n}}(\mathbf{m}_{i}) \bullet \mathbf{p}(\mathbf{R} = \mathbf{r}_{j} | \mathbf{m}_{i}) \bullet \mathbf{p}(Z > z | \mathbf{m}_{i}, \mathbf{r}_{j})$$
(2.3)

where:

- $\beta_n(m_i)$  = annual mean rate of recurrence of earthquakes of magnitude increment  $m_i$  on source n;
- $p(R=r_j|m_i) = probability that given the occurrence of an earthquake of magnitude$  $m_i on source n, r_j is the closest distance increment from the rupture$ surface to the site;
- $p(Z > z | m_i, r_j) =$  probability that given an earthquake of magnitude  $m_i$  at a distance of  $r_i$ , the ground motion exceeds the specified level z.

## 3 Test Cases and Results

Two sets of test cases were developed to evaluate elements of the PSHA codes. The objective of Test Case Set 1 was to test some basic elements of the codes, including how rupture areas were modeled on a fault plane, how recurrence models were used, how area sources were modeled, and how the standard deviations (sigma) in attenuation relationships were incorporated into the hazard calculations.

The purpose of Test Case Set 2 was to test more sophisticated elements of the codes such as the modeling of non-planar faults, listric faults, and the intraslab regions of subduction zones (Wadati-Benioff zones), multiple seismic sources, recurrence intervals as implemented with recurrence models, use of logic trees, computation of fractiles, and deaggregation.

The solutions to Test Case Set 1 are shown in the Appendix. The solutions to test Case Set 2 are not provided because consensus results were not reached due to schedule constraints (Section 3.2).

#### **3.1 TEST CASE SET 1**

Test Case 1 underwent three revisions due to not readily explainable differences in results in the first two versions. This third version was chosen to focus on the simple test cases of Set 1. The solutions have been calculated by hand and with Microsoft Excel for some of the test cases. To aid in the process, magnitude probability functions and distance probability functions have been provided for many of the cases and sites. Figure 3.1 illustrates the fault and site geometry. Site and source coordinates are provided in Appendix A.

The following were the instructions to the Working Group Members: Please provide mean hazard results (probability of exceedance) for peak horizontal acceleration (PGA) defined at 0.001, 0.01, 0.05, 0.1, 0.15, 0.2, 0.25, 0.3, 0.35, 0.4, 0.45, 0.5, 0.55, 0.6, 0.7, 0.8, 0.9, and 1.0 g. Assume a Poisson model when converting rates to annual probabilities of exceedance. Hand-calculated solutions are provided in Appendix A for the following test cases: 1, 2, 4, 5, 6, 7, and 9b. For tests cases and sites without hand-calculated solutions, mean results from the group of participants is provided in Appendix A.

Use 16.05 (not 16.1) in the equation  $\log M_0 = 16.05 + 1.5 M$ 

Use 3x10<sup>11</sup> dyne/cm<sup>2</sup>

Use a magnitude integration step size small enough to define the specified magnitude density function. The bin size for magnitude integration should be defined such that the  $M_{min}$  is at the lower edge of a bin, not in the center (i.e., If your magnitude step size is 0.01, one magnitude bin should be from **M** 5.0 to 5.01)

When integrating over the magnitude density function, integrate from zero (not M<sub>min</sub>)

Use uniform slip with tapered edges. Downdip and along-strike integration step size should be small enough to produce uniform rupture location. Do not allow rupture off the ends of fault.

Maintain the aspect ratio defined until maximum width is reached, then increase length (conservation of area at the expense of aspect ratio)

Sigma = 0 for the attenuation relationship implies that the sigma in the relationship is artificially set to zero, not that the sigma is truncated.

Note that equation for ln(y) in Table 3.1 of Sadigh *et al.* (1997) has a typo in the third term. It should read C3\*(8.5-M)^2.5 to match equation 2.2.

Rupture dimension relationships:

Log (A) = M - 4  $\sigma_A = 0.25$ 

 $Log (W) = 0.5*M - 2.15 \sigma_W = 0.15$ 

 $Log (L) = 0.5*M - 1.85 \sigma_L = 0.20$ 

Aspect Ratio = 2

Note: Sigma for all rupture dimension relationships should be set to zero for all cases except 3a–g.

For all faults, the slip rate is 2 mm/year, b-value = 0.9

For the area source, number of events per year of  $M_{min}$  and greater ( $M \ge 5$ ) is 0.0395 for the whole area, b-value =0.9, and  $M_{max} = 6^{1/2}$ .

The following test cases are also summarized in Table 3.1.

Name	Description	Source	Magnitude- Density Function <sup>1,2</sup>	Attenuation Relation	Rupture Dimension Relationships <sup>3,4,5,6</sup>
Set 1 Case 1	Single rupture of entire fault plane. Tests distance, rate, and attenuation calculations.	Fault 1 (vertical SS) b-value=0.9 slip rate=2mm/yr	Delta Function at M 6.5	Sadigh <i>et</i> <i>al.</i> (1997), rock $\sigma = 0$	$\begin{array}{l} \text{Log (A)=M-4; } \sigma_{\text{A}}=0 \\ \text{Log (W)=0.5*M-2.15;} \\ \sigma_{\text{W}}=0 \\ \text{Log (L)=0.5*M-1.85; } \sigma_{\text{L}} \\ =0 \end{array}$
Set 1 Case 2	Single rupture smaller than fault plane. Tests uniform slip and edge effects.	Fault 1(vertical SS) b-value=0.9 slip rate=2mm/yr	Delta Function at M 6.0	Sadigh <i>et</i> al.(1997), rock $\sigma = 0$	$\begin{array}{l} \text{Log (A)=M-4; } \sigma_{\text{A}}=0 \\ \text{Log (W)=0.5*M-2.15;} \\ \sigma_{\text{W}}=0 \\ \text{Log (L)=0.5*M-1.85; } \sigma_{\text{L}} \\ =0 \end{array}$
Set 1 Case 3	Single rupture smaller than fault plane, including variation of rupture plane dimensions. Tests uniform slip and edge effects, variability of rupture areas.	Fault 1(vertical SS) b-value=0.9 slip rate=2mm/yr	Delta Function at M 6.0	Sadigh <i>et</i> <i>al.</i> (1997), rock $\sigma = 0$	$\begin{array}{l} \text{Log} (A) = \text{M-4}; \ \sigma_{A} = 0.25 \\ \text{Log} (W) = 0.5*\text{M-2.15}; \\ \sigma_{W} = 0.15 \\ \text{Log} (L) = 0.5*\text{M-1.85}; \ \sigma_{L} \\ = 0.20 \end{array}$
Set 1 Case 4	Single rupture smaller than fault plane on dipping fault.	Fault 2(reverse 60°) b-value=0.9 slip rate=2mm/yr	Delta Function at M 6.0	Sadigh <i>et</i> <i>al.</i> (1997), rock $\sigma = 0$	Log (A)=M-4; $\sigma_A = 0$ Log (W)=0.5*M-2.15; $\sigma_W = 0$ Log (L)=0.5*M-1.85; $\sigma_L$ = 0
Set 1 Case 5	Truncated exponential model.	Fault 1(vertical SS) b-value=0.9 slip rate=2mm/yr	Truncated exponential model, $M_{max} =$ 6.5 $M_{min} =$ 5	Sadigh <i>et</i> <i>al.</i> (1997), rock $\sigma = 0$	Log (A)=M-4; $\sigma_A = 0$ Log (W)=0.5*M-2.15; $\sigma_W = 0$ Log (L)=0.5*M-1.85; $\sigma_L = 0$
Set 1 Case 6	Truncated normal model.	Fault 1(vertical SS) b-value=0.9 slip rate=2mm/yr	Truncated normal model, $M_{char} = 6.2$ , $M_{max} = 6.5$ , sigma=.25 $M_{min}=5$	Sadigh <i>et</i> <i>al.</i> (1997), rock $\sigma = 0$	$\begin{array}{l} \text{Log (A)=M-4; } \sigma_{A}=0 \\ \text{Log (W)=0.5*M-2.15;} \\ \sigma_{W}=0 \\ \text{Log (L)=0.5*M-1.85; } \sigma_{L} \\ =0 \end{array}$
Set 1 Case 7	Characteristic model (Youngs & Coppersmith 1985)	Fault 1(vertical SS) b-value=0.9 slip rate=2mm/yr	Characteristic model, $M_{char} =$ 6.2, $M_{max} =$ 6.45 $M_{min}=5$	Sadigh <i>et</i> al.(1997), rock $\sigma = 0$	$\begin{array}{l} \mbox{Log} (A) = M-4; \ \sigma_{A} = 0 \\ \mbox{Log} (W) = 0.5*M-2.15; \\ \ \sigma_{W} = 0 \\ \ \mbox{Log} (L) = 0.5*M-1.85; \ \sigma_{L} \\ = 0 \end{array}$
Set 1 Case 8a	Single rupture smaller than fault plane. (Repeat of case 2 with gm variability untruncated).	Fault 1(vertical SS) b-value=0.9 slip rate=2mm/yr	Delta Function at M 6.0	Sadigh <i>et</i> <i>al.</i> (1997), rock Do not truncate sigma	Log (A)=M- $\overline{4}$ ; $\sigma_{A} = 0$ Log (W)=0.5*M-2.15; $\sigma_{W} = 0$ Log (L)=0.5*M-1.85; $\sigma_{L}$ = 0

### Table 3.1 Test cases set 1

Name	Description	Source	Magnitude- Density Function <sup>1,2</sup>	Attenuation Relation	Rupture Dimension Relationships <sup>3,4,5,6</sup>
Set 1 Case 8b	Single rupture smaller than fault plane. (Repeat of case 2 with gm variability truncated at 2 std. dev.).	Fault 1(vertical SS) b-value=0.9 slip rate=2mm/yr	Delta Function at M 6.0	Sadigh <i>et</i> <i>al.</i> (1997), rock Truncate sigma at 2 std.dev.	Log (A)=M-4; $\sigma_A = 0$ Log (W)=0.5*M-2.15; $\sigma_W = 0$ Log (L)=0.5*M-1.85; $\sigma_L = 0$
Set 1 Case 8c	Single rupture smaller than fault plane. (Repeat of case 2 with gm variability truncated at 3 std.dev.)	Fault 1(vertical SS) b-value=0.9 slip rate=2mm/yr	Delta Function at M 6.0	Sadigh <i>et al.</i> (1997), rock Truncate sigma at 3 std.dev.	Log (A)=M-4; $\sigma_A = 0$ Log (W)=0.5*M-2.15; $\sigma_W = 0$ Log (L)=0.5*M-1.85; $\sigma_L = 0$
Set 1 Case 9a	Single rupture smaller than fault plane on dipping fault with gm truncated at 3 std. dev.	Fault 2(reverse 60°) b-value=0.9 slip rate=2mm/yr	Delta Function at M 6.0	Sadigh <i>et</i> <i>al.</i> (1997), rock Truncate sigma at 3 std.dev.	Log (A)=M-4; $\sigma_A = 0$ Log (W)=0.5*M-2.15; $\sigma_W = 0$ Log (L)=0.5*M-1.85; $\sigma_L = 0$
Set 1 Case 9b	Single rupture smaller than fault plane on dipping fault using AS 97 gm, no gm variability.	Fault 2(reverse 60°) b-value=0.9 slip rate=2mm/yr	Delta Function at M 6.0	Abrahamson & Silva (1997), rock $\sigma = 0$	Log (A)=M-4; $\sigma_A = 0$ Log (W)=0.5*M-2.15; $\sigma_W = 0$ Log (L)=0.5*M-1.85; $\sigma_L = 0$
Set 1 Case 9c	Single rupture smaller than fault plane on dipping fault using Campbell 1997 and gm truncated at 3 std. dev.	Fault 2(reverse 60°) b-value=0.9 slip rate=2mm/yr	Delta Function at M 6.0	Campbell (1997), soft rock, depth to basement rock = 2km, depth to seismogenic zone=3km Truncate sigma at 3 std.dev., use amplitude dependent sigma	Log (A)=M-4; $\sigma_A = 0$ Log (W)=0.5*M-2.15; $\sigma_W = 0$ Log (L)=0.5*M-1.85; $\sigma_L = 0$
Set 1 Case 10	Area Source with fixed depth of 5 km.	Area 1 $M_w \ge 0.0395$ b-value=0.9	Truncated Exponential, M <sub>max</sub> =6.5 M <sub>min</sub> =5	Sadigh <i>et al.</i> (1997), rock $\sigma = 0$	Use 1 km grid spacing of point sources or small faults to simulate uniform distribution.
Set 1 Case 11	Volume Source with depth of 5 km to 10 km.	Area 1 $M_w \ge = 0.0395$ b-value=0.9	Truncated Exponential, M <sub>max</sub> =6.5 M <sub>min</sub> =5	Sadigh <i>et</i> <i>al.</i> (1997), rock $\sigma = 0$	Use 1 km grid spacing of point sources or small faults to simulate uniform distribution.
Set 1 Case 12	Single rupture of entire fault plane. Adding ground motion variability to Case 1.	Fault 1 (vertical SS) b-value=0.9 slip rate=2mm/yr	Delta Function at M 6.5	Sadigh <i>et</i> <i>al.</i> (1997), rock Truncate sigma at 3 std.dev	Log (A)=M- $\overline{4}$ ; $\sigma_{A} = 0$ Log (W)=0.5*M-2.15; $\sigma_{W} = 0$ Log (L)=0.5*M-1.85; $\sigma_{L}$ = 0

Table 3.1—*Continued* 

Integration over magnitude zero. Use magnitude integration step size as small as necessary to model magnitude density function. For all cases, uniform slip with tapered slip at edges (see Fig. 3.2). No ruptures are to extend beyond the edge of the fault plane. 

Aspect Ratio to be maintained until maximum width is reached, then increase length (conserve area at the expense of aspect ratio). 

Downdip and along strike integration step size should be as small as necessary for uniform rupture location.

#### Case 1

Purpose: A single rupture of the entire fault plane will test the code calculation of distance, fault activity rate, and attenuation relation without variability.

Single-magnitude event (M 6.5) on Fault 1 that ruptures entire fault plane. Use Sadigh *et al.* (1997), rock, sigma = 0. Calculate the hazard for the seven sites shown in Figure 3.1.

#### Results

Test Case 1 is designed to test the code computation of fault distance, fault activity rate, and median ground motion predicted by the Sadigh *et al.* (1997), rock, for a given magnitude and distance. With a single-magnitude event (delta function of **M** 6.5) that ruptures the entire fault, the fault activity rate of 2.853E-3 is easily computed using the slip rate (2 mm/year) and fault area (300 km<sup>2</sup>). Due to the lack of variability in the ground motion and in the distance to the rupture plane for each site, the resulting hazard curve is a horizontal line at the fault activity rate extending to the ground motion value predicted for the magnitude and distance. Table 3.2 provides the median ground motion for each site. The results from all codes tested matched the analytical solution (Figs. 3.2–3.8).

Site	Distance (km)	PGA for M 6.5 (g)
1	0	0.7717
2	10	0.3123
3	50	0.0497
4	0	0.7717
5	10	0.3123
6	0	0.7717
7	10	0.3123

Table 3.2 Median PGA values at sites 1–7

#### Case 2

Purpose: A single rupture smaller than the fault plane tests uniform slip and edge effects.

Single-magnitude event (**M** 6.0) on Fault 1 with one size rupture plane (smaller than total fault plane area) as defined using the rupture area (RA), rupture width (RW), rupture length (RL) and/or aspect ratio relationships given below ( $\sigma_{RA} = \sigma_{RL} = \sigma_{RW} = 0$ ). Use Sadigh *et al.* (1997), rock, sigma = 0. Calculate the hazard for the seven sites shown in Figure 3.1.

#### Results

Test Case 2 is designed to test a code's computation of rupture area, distribution of slip, and distance to rupture. Variability of RA dimensions and ground motion was set to zero to simplify the test case. The initial results from the codes tested showed significant differences. Figure 3.9 shows an early set of results for Site 1, which is located on the trace of the fault at the midpoint along the strike. Some codes initially provided different results for Sites 4 and 6, which are located at the ends of the fault. An examination of the results and discussion among participants determined that modeling of the rupture on the fault plane, especially near the fault edges, differed among code developers. These differences in approach led to significant differences in hazard for this simple test case. The Working Group decided to adopt a recommended approach for the rupture model: uniform slip which tapers at the fault to the other end both along the strike and the down-dip width. No ruptures are allowed to extend beyond the edges of the fault. Hazard near the ends is sensitive to the step-size used to move the rupture. With the recommended approach, the codes tested were able to approximate the analytical solution closely. Figures 3.10 to 3.16 show the results for the seven sites.

#### Case 3

Purpose: A single rupture smaller than the fault plane with variability in the rupture dimension relationships included tests of the uniform slip and edge effects with variability of the rupture area, the width and the length.

Single-magnitude event (**M** 6.0) on Fault 1 with rupture planes as defined using the RA, RW, RL and/or aspect ratio relationships given below (include sigma in these relationships). Maintain the aspect ratio defined until maximum width is reached, then increase length (conservation of area at the expense of aspect ratio.) Use Sadigh *et al.* (1997), rock, sigma = 0. Calculate the hazard for the seven sites shown in Figure 3.1.

#### Results

Test Case 3 builds directly on Case 2. The only change is the inclusion of variability in the rupture dimension relations. The rupture dimension equations were chosen such that the median rupture length and width would not be sensitive to the computation approach. Some of the codes compute RA based on magnitude then maintain a constant aspect ratio. Other codes compute RA and width based on magnitude and back out the rupture length. However, the different approaches to incorporating the variability and computing the rupture dimensions will provide

different hazard results. The variation of hazard results provides an example of the sensitivity to this parameter. Note that the variability in the rupture dimension equations is not always incorporated in standard PSHAs. The results for all sites are shown in Figures 3.17–3.23.

#### Case 4

Purpose: This case is a repeat of Case 2 using a dipping fault (Fault 2). It tests the calculation of distance to a dipping fault.

Single-magnitude event (**M** 6.0) on Fault 2 with one size rupture plane (smaller than total fault plane area) as defined using the RA, RW, RL and/or aspect ratio relationships given above ( $\sigma_{RA} = \sigma_{RL} = \sigma_{RW} = 0$ ). Use Sadigh *et al.* (1997), rock, sigma = 0. Calculate the hazard for the seven sites shown in Figure 3.1.

#### Results

Test Case 4 is intended to further test the geometric modeling of faults. It is a slight variation of Test Case 2. In this case, a single size rupture smaller than the full fault plane occurs on a buried dipping fault. With variability in ground motion and rupture dimensions set to zero, the hazard is a function only of the fault activity rate (calculated from the magnitude, slip rate and fault area) and distance to the rupture. The solutions computed by hand and Microsoft Excel are compared to the results for Sites 1, 2, and 7. As with Test Case 2, initial results showed large variation due to variation in approaches for distribution of rupture plane on the fault plane, especially near the edges. Figures 3.24 and 3.25 are the initial results for sites on the ends of the fault (Sites 4 and 6, respectively.) After modifications to model slip that tapers at the edges, all results compare well with the hand solutions, with the exception of one code for Site 7, which is on the footwall (Figs. 3.26–3.32). In addition, results from these codes are all tightly grouped. These results indicate that the geometric modeling of dipping faults and movement of ruptures on the fault plane are consistent among the codes.

#### Case 5

Purpose: Tests calculation of the truncated exponential model.

Calculate the hazard for all seven sites due to rupture of Fault 1 using the truncated exponential model ( $M_{max}$  6.5 and  $M_{min}$  5.0) and Sadigh *et al.* (1997), rock, sigma = 0. Use the RA, RW, and RL relationships (with  $\sigma_{RA} = \sigma_{RL} = \sigma_{RW} = 0$ ) to define the dimensions of the rupture planes.

#### Results

Test Case 5 is intended to test one magnitude-frequency distribution, specifically the truncated exponential model. This model is used extensively in realistic hazard analyses. The initial results pointed toward a difference in approach for calculating the fault activity rate using the truncated exponential magnitude distribution model. As seen in Figure 3.33, the initial hazard results could be grouped into two sets. The difference is due to whether the integration over magnitude is done from the minimum magnitude or zero. Participants were then asked to modify their codes to integrate from zero. The results for all sites are shown in Figures 3.34–3.40. The solutions were computed by hand with the assistance of Microsoft Excel for Sites 4, 5, and 6, for which the geometries provide simple distance to rupture distributions. Hazard results from all codes compare well with the hand solutions, and are tightly grouped for the sites without hand solutions.

#### <u>Case 6</u>

Purpose: Tests the truncated normal model.

Calculate the hazard for all 7 sites due to the rupture of Fault 1 using the truncated normal model (M<sub>char</sub> 6.2, M<sub>max</sub> 6.5, sigma 0.25 and M<sub>min</sub> 5.0) and Sadigh *et al.* (1997), rock, sigma 0. Use the RA, RW, and RL relationships (with  $\sigma_{RA} = \sigma_{RL} = \sigma_{RW} = 0$ ) to define the dimensions of the rupture planes.

#### Results

Test Case 6 is intended to test the truncated normal magnitude distribution model. Figures 3.41 to 3.47 show the results for all sites. As with Test Case 5, the results from all codes compare well with the hand solutions, and are tightly grouped for the sites without hand solutions.

#### <u>Case 7</u>

Purpose: Tests the characteristic model.

Calculate the hazard for all 7 sites due to the rupture of Fault 1 using the characteristic model (Youngs and Coppersmith [1985]  $M_{char}$  6.2,  $M_{max}$  6.45, and  $M_{min}$  5.0) and Sadigh *et al.* (1997), rock, sigma 0. Use the RA, RW, and RL relationships (with  $\sigma_{RA} = \sigma_{RL} = \sigma_{RW} = 0$ ) to define the dimensions of rupture planes.

#### Results

Test Case 7 is intended to test the characteristic magnitude frequency distribution, which is used extensively in modern PSHAs. Similar to Test Case 5, which tests the exponential model, early results showed differences in calculating the fault activity rate. The initial results for Site 6 are shown in Figure 3.48. Note the spread in hazard at very low ground motions. The final results show consistency between all codes (Figs. 3.49–3.55).

#### <u>Case 8</u>

Purpose: This is a repeat of Case 2 with ground motion variability included as defined by the attenuation relationship. The case is run with ground motion variability untruncated, truncated at 2 standard deviations, and truncated at 3 standard deviations.

Calculate the hazard for all seven sites due to a single-magnitude event (**M** 6.0) on Fault 1 using Sadigh *et al.* (1997), rock, sigma untruncated, and truncated at two and three standard deviations. Use the RA, RW, and RL relationships (with  $\sigma_{RA} = \sigma_{RL} = \sigma_{RW} = 0$ ) to define the dimensions of the rupture planes.

#### Results

Test Case 8 is an extension of Case 2 in order to test the addition of aleatory variability in the ground motion prediction equation. The case was analyzed using untruncated variability and variability truncated at two and three standard deviations. The hazard results from all codes are tightly grouped. Figures 3.56 to 3.62 show the results for untruncated ground motion variability. The hazard results for cases with ground motion variability truncated at two and three standard deviations are shown in Figures 3.63–3.69 and Figures 3.70–3.76, respectively.

#### Case 9

Purpose: A single rupture smaller than the fault plane on a dipping fault testing three common attenuation relationships.

Calculate the hazard for all seven sites due to a single-magnitude event (**M** 6.0) on Fault 2 using the following three attenuation relationships

- (9a) Sadigh et al. (1997), rock, sigma truncated at 3 standard deviations
- (9b) Abrahamson and Silva (1997), rock, sigma = 0
- (9c) Campbell (1997), soft rock, depth to basement rock = 2 km, depth to seismogenic zone = 3 km, sigma truncated at 3 standard deviations

Compute the results for the attenuation relationships individually. Use the RA, RW, and RL relationships (with  $\sigma_{RA} = \sigma_{RL} = \sigma_{RW} = 0$ ) to define the dimensions of the rupture planes.

Note for Abrahamson and Silva (1997), include the style of faulting factor (F=1 for reverse fault) and the hanging wall factor. As defined, the hanging wall factor applies to only Site 2. HW = 1 for Sites 1, 2, 3, 4, and 6. However, fHW(Rrup) = 0 for Sites 1, 4, and 6 (Rrup < 4) as well as Site 3 (Rrup > 25). HW = 0 for Site 5 (off edge) and Site 7 (on footwall).

Also note that the Abrahamson and Silva (1997) formula for  $f_3(M)$ , Eq. 6, p.106 contains an error. For **M** between 5.8 and c1, the fraction  $[(a_6-a_5)/(c_1-5.8)]$  should be multiplied by (**M**-5.8).

#### Results

Test Case 9a is an extension of Test Case 4. The variability in the ground motion attenuation relation is included and truncated at three sigma. The hazard results are shown in Figures 3.77–3.83. Hand solutions were not computed; however, there is consistency in the results from all codes.

Test Case 9b uses an attenuation relation that includes hanging wall effects. The variability in the ground motion is not included so as to allow for easier hand solution. The solutions are provided for Sites 1, 2, and 7. The hazard results for all sites are shown in Figures 3.84–3.90. For sites on the ends of the surface projection of the fault, Sites 4 and 6, there is one outlier (Figs. 3.87 and 3.89). The results from Site 1 also show some variation among codes, the source of which has not been determined.

Test Case 9c tests the implementation of the Campbell (1997) attenuation relation for soft rock. The results are presented in Figures 3.91–3.97. The hazard results are clustered into two groups. This is due to the use of different estimates of variability in the ground motion attenuation relation. Campbell (1997) provides two estimates of variability, one as a function of magnitude and one as a function of amplitude, or PGA. To confirm, Haz38 was run for Sites 2, 3, and 5 using both relations (Figs. 3.92, 3.93, and 3.95, respectively).

#### <u>Case 10</u>

Purpose: Area source with fixed depth of 5 km

Calculate the hazard at four sites for the area source defined in Figure 3.1. Use the truncated exponential model with  $M_{max} = 6.5$  and  $M_{min}=5.0$ . Source should be uniformly

distributed point sources (or approximations to point source) across the area (1 km grid spacing) at a fixed depth of 5 km. The attenuation relationship is Sadigh *et al.* (1997), rock, sigma = 0.

#### Results

Test Case 10 tests the computation of hazard from an area source. The case was defined as having uniformly distributed point sources throughout the area at a fixed depth. However, some of the codes tested do not implement point sources. These codes used an area source defined with uniformly distributed small faults that were set to be 1 square km in size. Even with these differences, results from all codes are consistent, as shown in Figures 3.98–3.101.

#### Case 11

Purpose: Volume source with fixed depth of 5–10 km

Calculate the hazard at four sites for area source defined in Figure 3.1. Use the truncated exponential model with  $M_{max} = 6.5$  and  $M_{min}=5.0$ . The source should be uniformly distributed point sources (or approximation to point sources) throughout the volume (1 km grid spacing) defined by the area and a depth range of 5–10 km. The attenuation relationship is Sadigh *et al.* (1997), rock, sigma = 0.

#### Results

Test Case 11 extends the area source to a volume with point sources distributed over a depth range. The hazard results are shown in Figures 3.102–3.105. As with Test Case 10, the results from all codes are consistent with each other.

#### 3.2 TEST CASE SET 2

The following describes the second set of test cases. Mean hazard results (probability of exceedance) for PGA defined at 0.001, 0.01, 0.05, 0.1, 0.2, 0.3, 0.4, 0.5, 0.75, 1.0, 1.25, and 1.5 g were calculated. A Poisson model was assumed when converting rates to probabilities.

The second set of test cases is designed to test more complicated source geometry, multiple sources, and the implementation of logic trees. The participants provided the hazard results. However, due to schedule constraints, the results were not revised after all code issues related to Test Case 1 were resolved. The consensus results are not provided for Test Case 2.

#### For All Cases:

Use  $M_{min} = 5.0$  with an integration step size small enough to adequately model the Magnitude density function

Fault rupture dimension relationships:

Log (A) = M-4  $\sigma_A=0$ Log (W) = 0.5\*M-2.15  $\sigma_W=0$ Log (L) = 0.5\*M-1.85  $\sigma_L=0$ Aspect Ratio = 2

#### Case 1a-f (Non-Planar Fault)

Calculate the hazard at the three sites shown in Figure 3.106 due to the rupture of Fault A (unsegmented rupture only) using the truncated exponential model ( $M_{max} = 7.0$ ), slip rate = 2 mm/yr, b-value = 0.9, and the Sadigh *et al.* (1997) attenuation relationship, rock, sigma = 0. Use the RA, RW, and RL relationships given below (with  $\sigma_{RA} = \sigma_{RL} = \sigma_{RW} = 0$ ) to define the dimensions of the rupture planes. For cases 1a, 1b, and 1c use a dip of 60 degrees to the east. For cases 1d, 1e, and 1f use a dip of 60 degrees to the west.

The initial results for Site 1 are provided in Figure 3.107. This test case is designed to test how the geometry of non-straight-line faults are handled across available codes. Most codes to date model faults with planes. For a fault that bends along strike and dips other than 90 degrees, this creates gaps or overlaps of the planes at the bend along strike. Modeling approaches to address these gaps or overlaps range from ignoring the gap and combining planes at the intersection, to using the average strike to project the fault bottom points and connect (which changes the dip), to using conical surfaces to fill the gaps. This issue becomes more important when hanging wall factors are considered. Determination of whether a site is on the hanging wall or not may be sensitive to gaps. In addition, the Rx parameter in the Next Generation of Attenuation (NGA) ground motion relations can be sensitive to the correct geometric modeling of the fault.

#### Cases 2a-c (Multiple Sources, Deaggregation)

Calculate the hazard at the three sites shown in Figure 3.108 due to the area source, Fault B, and Fault C. For the area source, use the truncated exponential model ( $M_{max}$ =6.5) and the cumulative number of events with  $M \ge 5.0 = 0.0395$ . For Fault B (L=75 km), use the characteristic model

(Youngs and Coppersmith [1985],  $M_{char} = 7.0$ ,  $M_{max} = 7.25$ ), and slip rate = 2 mm/yr. For Fault C (L=25 km), use the characteristic model (Youngs and Coppersmith [1985],  $M_{char} = 6.5$ ,  $M_{max} = 6.75$ ), and slip rate = 1 mm/yr. For all sources, use the Sadigh *et al.* (1997) attenuation relationship, rock, sigma truncated at 3 standard deviations, b-value = 0.9, a  $M_{min} = 5.0$ . For the faults, use the RA, RW, and RL relationships given below (with  $\sigma_{RA} = \sigma_{RL} = \sigma_{RW} = 0$ ) to define the dimensions of the rupture planes.

Provide the following deaggregation results for peak ground acceleration at Sites 1 and 3 corresponding to the annual exceedance probabilities of 0.01 and 0.0001:

Modal values M\*, D\*,  $\epsilon^*$ 

Mean values M-bar, D-bar, ɛ-bar

Test Case 2 was designed to look at multiple sources and deaggregation. An example of early hazard results is shown in Figure 3.109. With perhaps two outliers, the results are fairly closely grouped.

#### <u>Cases 3a-c (Recurrence Interval, Characteristic Model)</u>

Calculate the hazard for all three sites due to the rupture of Fault D (Fig. 3.110) using the characteristic model (Youngs and Coppersmith [1985],  $M_{char} = 6.2$ ,  $M_{max} = 6.45$ ), recurrence interval = 1000 years, and the Sadigh *et al.* (1997) attenuation relationship, rock, sigma = 0. Use the RA, RW, and RL relationships (with  $\sigma_{RA} = \sigma_{RL} = \sigma_{RW} = 0$ ) to define the dimensions of the rupture planes.

Test Case 3 is an extension of Test Case 7 from Set 1. It is intended to test the use of the recurrence interval using the characteristic model of earthquake magnitude distribution. Early results are shown in Figure 3.111 for Site 1.

#### <u>Cases 4a–c (Recurrence Interval, Truncated Normal Model)</u>

Calculate the hazard for all three sites due to the rupture of Fault D (Fig. 3.110) using the truncated normal model ( $M_{char} = 6.2$ ,  $M_{max} = 6.5$ , sigma = 0.25), recurrence interval = 1000 years, and the Sadigh *et al.* (1997) attenuation relationship, rock, sigma = 0. Use the RA, RW, and RL relationships (with  $\sigma_{RA} = \sigma_{RL} = \sigma_{RW} = 0$ ) to define the dimensions of the rupture planes.

Test Case 4 is intended to test the use of the recurrence interval with the truncated normal distribution of earthquake magnitude. Early results are shown in Figure 3.112 for Site 1.

#### Cases 5a-c (Logic Tree, Fractiles)

Calculate the hazard for all three sites due to the rupture of Fault A (Fig. 3.106) as shown in the logic tree in Figure 3.113. Provide the mean hazard along with the 5<sup>th</sup> and 95<sup>th</sup> percentile fractiles. Use the Sadigh *et al.* (1997) attenuation relationship, rock, truncate sigma at three standard deviations. Use the RA, RW, and RL relationships (with  $\sigma_{RA} = \sigma_{RL} = \sigma_{RW} = 0$ ) to define dimensions of rupture planes.

The initial results for Test Case 5 for Site 1 is shown in Figure 3.114. Due to a lack of discussion and revision, it is unknown if the wide range of results is a result of different interpretation of the logic tree or input errors.

#### Cases 6a-c (Listric Fault)

Calculate the hazard for all three sites due to the rupture of Fault E (Fig. 3.115) using the truncated exponential model ( $M_{max} = 6.5$ ) and the Sadigh *et al.* (1997) attenuation relationship, rock, sigma = 0. Assume that the fault is strike-slip for the attenuation relationship. Slip-rate = 2 mm/yr. Use the RA, RW, and RL relationships (with  $\sigma_{RA} = \sigma_{RL} = \sigma_{RW} = 0$ ) to define the dimensions of the rupture planes.

Test Case 6 is intended to examine the various modeling approaches for a listric fault and its effect on hazard. The initial results are shown in Figure 3.116. Differences in rate could be a result of different fault areas due to the different fault geometries, but also could be due to the integration issues discovered in Test Case 1.

#### Cases 7a-c (Intraslab Zone)

Calculate the hazard for all three sites due to rupture of the intraslab zone with uniform thickness of 10 km (Fig. 3.117) using the truncated exponential model ( $M_{max} = 7.5$ ) and the Youngs *et al.* (1997) attenuation relationship, with sigma truncated at three standard deviations. The *b*-value is 0.9. The rate for events greater and equal to 5 is 0.005644.

Test Case 7 is intended to test the modeling of an intraslab zone. The slab was defined as a dipping volume. The modeling approaches for this varied among codes. Most used a series of horizontal volumes that stairstep down from the shallow end to the deeper end of the slab. Figure 3.118 shows the initial results for Site 1.

## 4 Conclusions

This report describes a project to test and verify the numerical approaches and software used in PSHA. A Working Group was organized and each member tested their own computer code in two sets of tests. Through several iterations, codes were tested and acceptable answers were established either through analytical solutions or as the consensus answer from the test case results. Given the significant experience of the Working Group members, it was somewhat surprising to find major differences in the initial code verification results. However, more often than not, the differences were due to the differences in the numerical approaches used to solve a particular mathematical problem. Once an agreed-upon solution was adopted and the source characterization clearly defined, the results generally converged.

The verification tests are available to any PSHA code developer/user worldwide through this publication and the PEER website. The test cases will be used as a standard verification for all PSHA codes to be used in projects for the PEER Lifelines Program sponsors, which include the California Department of Transportation (Caltrans), the Pacific Gas & Electric Company (PG&E), and the California Energy Commission (CEC).

### REFERENCES

- Abrahamson, N., 2000, Effects of rupture directivity on probabilistic seismic hazard analysis: Sixth International Conference on Seismic Zonation, v. I, p. 151-156.
- Abrahamson, N.A. and Silva, W.J., 1997, Empirical response spectral attenuation relations for shallow crustal earthquakes: Seismological Research Letters, v. 68, p. 94-127.
- Campbell, K.C., 1997, Empirical near source attenuation relationships for horizontal and vertical components of peak ground acceleration, velocity, and pseudo-absolute acceleration response spectra: Seism. Res. Lett. 68, 154-179.
- Cornell, C. A., 1968, Engineering seismic risk analysis: Bulletin of the Seismological Society of America, v. 58, p. 1583-1606.
- Frankel, A., Mueller, C., Barnard, T., Perkins, D., Leyendecker, E.V., Dickman, N., Hanson, S., and Hopper, M., 1996, National seismic hazard maps; documentation June 1996: U.S. Geological Survey Open-File Report 96-532, 110 p.
- McGuire, R.K., 2004, Seismic hazard and risk analysis: Earthquake Engineering Research Institute, Monograph 10, 221 p.
- Petersen, M.D., Frankel, A.D., Harmsen, S.C., Mueller, C.S., Haller, K.M., Wheeler, R.L., Wesson, R.L., Zeng, Y., Boyd, O.S., Perkins, D.M., Luco, N., Field, E.H., Wills, C.J., and Rukstales, K.S., 2008, Documentation for the 2008 update of the United States National Seismic Hazard Maps: U.S. Geological Survey Open-File Report 2008-1128, 61 p.
- Sadigh, K., C.-Y. Chang, J.A. Egan, F. Makdisi, and R.R. Youngs 1997. Attenuation relationships for shallow crustal earthquakes based on California strong motion data: Seismological Research Letters, 68, 180-189.
- Senior Seismic Hazard Analysis Committee (SSHAC), 1997, Recommendations for probabilistic seismic hazard analysis: Guidance on uncertainty and use of experts: U.S. Nuclear Regulatory Commission (NRC) NUREG/CR-6372, Washington, D.C.
- Stepp, J.C., Wong, I., Whitney, J., Quittmeyer, R., Abrahamson, N., Coppersmith, K., Toro, G., Youngs, R., Savy, J., Sullivan, T., and Yucca Mountain PSHA Project Members, 2001, Probabilistic seismic hazard analyses for ground motions and fault displacement at Yucca Mountain, Nevada: Earthquake Spectra, v. 17, p.113-151.
- Wong, I.G., Thomas, P.A., and Abrahamson, N., 2004, The PEER-Lifelines validation of software used in probabilistic seismic hazard analysis, *in* 2004 Geotechnical Engineering for Transportation Projects, Proceedings, M. Yegian and E. Kavazanjian (eds.), American Society of Civil Engineers, Geotechnical Special Publication No. 126, v. 1, p. 807-815.
- Youngs, R.R. and Coppersmith, K.J., 1985, Implications of fault slip rates and earthquake recurrence models to probabilistic seismic hazard estimates: Bulletin of the Seismological Society of America, v. 75, p. 939-964.
- Youngs, R.R., Swan, F.H., Power, M.S., Schwartz, D.P. and Green, R.K., 1987, Probabilistic analysis of earthquake ground shaking hazard along the Wasatch front, Utah, in P. L. Gori and W.W. Hays (eds.), Assessment of Regional Earthquake Hazards and Risk Along the Wasatch Front, Utah, U. S. Geological Survey Open-File Report 87-585, v. II, p. M1-M110.

Appendix A
# SITE AND SOURCE COORDINATES

Site	Latitude	Longitude	Comment
1	38.113	-122.000	On Fault Midpoint along Strike
2	38.113	-122.114	10km West of fault, at midpoint
3	38.111	-122.570	50km West of fault, at midpoint
4	38.000	-122.000	South end of fault
5	37.910	-122.000	10km south of fault along strike
6	38.225	-122.000	North end of fault
7	38.113	-121.886	10km East of fault, at midpoint

#### Sites for Test Set 1, Cases 1 through 9

## Coordinates for 25 km fault for Test Set 1, Cases 1 through 9

Latitude	Longitude	Comment
38.00000	-122.000	South end of fault
38.22480	-122.000	North end of fault

#### Sites for Test Set 1, Cases 10 and 11

Site	Latitude	Longitude	Comment
1	38.000	-122.000	Center of Area 1
2	37.550	-122.000	50km N of Site 1
3	37.099	-122.000	On Area Boundary
4	36.874	-122.000	25km N of Area Boundary

#### Coordinates for Area Source for Test Set 1, Cases 10 and 11

Latitude	Longitude
38.901	-122.000
38.899	-121.920
38.892	-121.840
38.881	-121.760
38.866	-121.682
38.846	-121.606
38.822	-121.532
38.794	-121.460
38.762	-121.390
38.727	-121.324
38.688	-121.261
38.645	-121.202
38.600	-121.147
38.551	-121.096
38.500	-121.050
38.446	-121.008
38.390	-120.971
38.333	-120.940
38.273	-120.913
38.213	-120.892
38.151	-120.876
38.089	-120.866
38.026	-120.862
37.963	-120.863
37.900	-120.869
37.838	-120.881
37.777	-120.899
37.717	-120.921
37.658	-120.949

Latitude	Longitude
37.601	-120.982
37.545	-121.020
37.492	-121.063
37.442	-121.110
37.394	-121.161
37.349	-121.216
37.308	-121.275
37.269	-121.337
37.234	-121.403
37.203	-121.471
37.176	-121.542
37.153	-121.615
37.133	-121.690
37.118	-121.766
37.108	-121.843
37 101	-121 922
37 099	-122,000
37.101	-122.000
37.101	-122.157
37.118	-122.137
37.133	-122 310
37.153	-122.310
37.135	-122.505
37.203	_122.438
37.205	-122.527
37.254	-122.597
37.209	-122.005
37.308	122.723
37.349	122.764
37.394	-122.839
37.442	-122.890
37.492	-122.937
37.545	122.018
37.601	123.018
27.717	123.070
27.777	-123.079
27.828	-123.101
37.030	-123.119
37.900	-125.151
28 026	-123.137
28,020	-123.136
29 151	-123.134
20 212	-125.124
28 272	-125.106
20 222	-125.067
28 200	-123.000
20 446	-123.029
20 500	-122.772
<u> </u>	-122.930
38.331	-122.904
38.600	-122.853
38.043	-122./98
38.088	-122./39
38.727	-122.070
38.762	-122.610

Latitude	Longitude
38.794	-122.540
38.822	-122.468
38.846	-122.394
38.866	-122.318
38.881	-122.240
38.892	-122.160
38.899	-122.080

## Sites for Test Set 2

Test Case	Site	Latitude	Longitude
1	1	38.1126	-121.886
1	2	38.1800	-121.886
1	3	38.2696	-122.114
2	1	37.5495	-122.000
2	2	37.0990	-122.000
2	3	36.8737	-122.000
3–7	1	38.1126	-121.886
3–7	2	38.2252	-122.000
3-7	3	38.0000	-122.000

## Fault Coordinates for Test Set 2

Test Case	Fault	Latitude	Longitude
1, 5	Fault A - Unsegmented	38.6147	-121.7130
1, 5	Fault A - Unsegmented	38.4200	-121.8569
1, 5	Fault A - Unsegmented	38.2248	-122.0000
1, 5	Fault A - Unsegmented	38.0000	-122.0000
1, 5	Fault A - Unsegmented	37.8049	-121.8581
1, 5	Fault A - Unsegmented	37.6095	-121.7169
1, 5	Fault A - Segment A	38.6147	-121.7130
1, 5	Fault A - Segment A	38.4200	-121.8569
1, 5	Fault A - Segment B	38.4200	-121.8569
1, 5	Fault A - Segment B	38.2248	-122.0000
1, 5	Fault A - Segment C	38.2248	-122.0000
1, 5	Fault A - Segment C	38.0000	-122.0000
1, 5	Fault A - Segment D	38.0000	-122.0000
1, 5	Fault A - Segment D	37.8049	-121.8581
1, 5	Fault A - Segment E	37.8049	-121.8581
1, 5	Fault A - Segment E	37.6095	-121.7169
2	Fault B	38.6749	-121.5691
2	Fault B	38.6749	-122.4309
2	Fault C	37.3242	-121.8590
2	Fault C	37.3242	-122.1410
3, 4	Fault D	38.2248	-122.0000
3, 4	Fault D	38.0000	-122.0000
6	Fault E	38.2248	-122.0000
6	Fault E	38.0000	-122.0000
7	Intraslab	38.4496	-122.0000
7	Intraslab	37.7752	-122.0000

Latitude	Longitude
38.901	-122.000
38.899	-121.920
38.892	-121.840
38.881	-121.760
38.866	-121.682
38.846	-121.606
38.822	-121.532
38.794	-121.460
38.762	-121.390
38.727	-121.324
38,688	-121.261
38.645	-121,202
38 600	-121 147
38 551	-121.096
38 500	-121.050
38.446	-121.008
38 390	-120.971
38 333	-120.971
28 272	120.013
28 212	-120.913
29.151	-120.892
28,080	-120.870
38.089	-120.800
38.026	-120.862
37.963	-120.863
37.900	-120.869
37.838	-120.881
37.777	-120.899
37.717	-120.921
37.658	-120.949
37.601	-120.982
37.545	-121.020
37.492	-121.063
37.442	-121.110
37.394	-121.161
37.349	-121.216
37.308	-121.275
37.269	-121.337
37.234	-121.403
37.203	-121.471
37.176	-121.542
37.153	-121.615
37.133	-121.690
37.118	-121.766
37.108	-121.843
37.101	-121.922
37.099	-122.000
37.101	-122.078
37.108	-122.157
37.118	-122.234
37.133	-122.310
37.153	-122.385
37.176	-122.458
37.203	-122.529

Area Source Coordinates for Test Set 2, Case 2

Latitude	Longitude
37.234	-122.597
37.269	-122.663
37.308	-122.725
37.349	-122.784
37.394	-122.839
37.442	-122.890
37.492	-122.937
37.545	-122.980
37.601	-123.018
37.658	-123.051
37.717	-123.079
37.777	-123.101
37.838	-123.119
37.900	-123.131
37.963	-123.137
38.026	-123.138
38.089	-123.134
38.151	-123.124
38.213	-123.108
38.273	-123.087
38.333	-123.060
38.390	-123.029
38.446	-122.992
38.500	-122.950
38.551	-122.904
38.600	-122.853
38.645	-122.798
38.688	-122.739
38.727	-122.676
38.762	-122.610
38.794	-122.540
38.822	-122.468
38.846	-122.394
38.866	-122.318
38.881	-122.240
38.892	-122.160

Hand Solutions for Set 1, Test Case 2							
Peak Ground	Annual Exceedance Probability						
Acceleration	Site 1	Site 2	Site 3	Site 4	Site 5	Site 6	Site 7
(g)							
0.001	1.59E-02	1.59E-02	1.59E-02	1.59E-02	1.59E-02	1.59E-02	1.59E-02
0.01	1.59E-02	1.59E-02	1.59E-02	1.59E-02	1.59E-02	1.59E-02	1.59E-02
0.05	1.59E-02	1.59E-02	0.00E+00	1.59E-02	1.59E-02	1.59E-02	1.59E-02
0.1	1.59E-02	1.59E-02	0.00E+00	1.59E-02	1.56E-02	1.59E-02	1.59E-02
0.15	1.59E-02	1.59E-02	0.00E+00	1.59E-02	7.69E-03	1.59E-02	1.59E-02
0.2	1.59E-02	1.59E-02	0.00E+00	1.58E-02	1.60E-03	1.58E-02	1.59E-02
0.25	1.59E-02	0.00E+00	0.00E+00	1.20E-02	0.00E+00	1.20E-02	0.00E+00
0.3	1.59E-02	0.00E+00	0.00E+00	8.64E-03	0.00E+00	8.64E-03	0.00E+00
0.35063	1.59E-02	0.00E+00	0.00E+00	5.68E-03	0.00E+00	5.68E-03	0.00E+00
0.4	1.18E-02	0.00E+00	0.00E+00	3.09E-03	0.00E+00	3.09E-03	0.00E+00
0.45	8.23E-03	0.00E+00	0.00E+00	1.51E-03	0.00E+00	1.51E-03	0.00E+00
0.5	5.23E-03	0.00E+00	0.00E+00	6.08E-04	0.00E+00	6.08E-04	0.00E+00
0.55	2.64E-03	0.00E+00	0.00E+00	1.54E-04	0.00E+00	1.54E-04	0.00E+00
0.6	3.63E-04	0.00E+00	0.00E+00	2.92E-06	0.00E+00	2.92E-06	0.00E+00
0.65	0.00E+00	0.00E+00	0.00E+00	0.00E+00	0.00E+00	0.00E+00	0.00E+00

# SOLUTIONS TO SET 1, TEST CASES 2, 4, 5, 6, 7 AND 9b

Hand Solutions for Set 1, Test Case 4						
Peak Ground	Site 1	Site 2	Site 7			
Acceleration (g)						
0.001	1.68E-02	1.68E-02	1.68E-02			
0.01	1.68E-02	1.68E-02	1.68E-02			
0.05	1.68E-02	1.68E-02	1.68E-02			
0.10	1.68E-02	1.68E-02	1.68E-02			
0.15	1.68E-02	1.68E-02	1.68E-02			
0.20	1.68E-02	1.68E-02	1.64E-02			
0.25	1.68E-02	1.68E-02	4.17E-03			
0.30	1.68E-02	0.00E+00	0.00E+00			
0.35	1.68E-02	0.00E+00	0.00E+00			
0.40	1.37E-02	0.00E+00	0.00E+00			
0.45	1.01E-02	0.00E+00	0.00E+00			
0.50	7.03E-03	0.00E+00	0.00E+00			
0.55	4.37E-03	0.00E+00	0.00E+00			
0.60	2.00E-03	0.00E+00	0.00E+00			
0.65	0.00E+00	0.00E+00	0.00E+00			

Hand Solutions for Set 1, Test Case 5							
Peak Ground Acceleration (g)	Site 4	Site 5	Site 6				
0.001	3.99E-02	3.99E-02	3.99E-02				
0.01	3.99E-02	3.99E-02	3.99E-02				
0.05	3.98E-02	3.14E-02	3.98E-02				
0.1	2.99E-02	1.21E-02	2.99E-02				
0.15	2.00E-02	4.41E-03	2.00E-02				
0.2	1.30E-02	1.89E-03	1.30E-02				
0.25	8.58E-03	7.53E-04	8.58E-03				
0.3	5.72E-03	1.25E-04	5.72E-03				
0.35	3.88E-03	0.00E+00	3.88E-03				
0.4	2.69E-03	0.00E+00	2.69E-03				
0.45	1.91E-03	0.00E+00	1.91E-03				
0.5	1.37E-03	0.00E+00	1.37E-03				
0.55	9.74E-04	0.00E+00	9.74E-04				
0.6	6.75E-04	0.00E+00	6.75E-04				
0.7	2.52E-04	0.00E+00	2.52E-04				
0.8	0.00E+00	0.00E+00	0.00E+00				

Hand Solutions for Set 1, Test Case 6						
Peak Ground Acceleration (g)	Site 4	Site 5	Site 6			
0.001	7.75E-03	7.75E-03	7.75E-03			
0.01	7.75E-03	7.75E-03	7.75E-03			
0.05	7.75E-03	7.75E-03	7.75E-03			
0.075	7.75E-03	7.75E-03	7.75E-03			
0.10	7.74E-03	7.37E-03	7.74E-03			
0.15	7.64E-03	5.81E-03	7.64E-03			
0.20	7.31E-03	3.57E-03	7.31E-03			
0.25	6.73E-03	1.52E-03	6.73E-03			
0.30	5.99E-03	2.26E-04	5.99E-03			
0.40	4.27E-03	0.00E+00	4.27E-03			
0.50	2.64E-03	0.00E+00	2.64E-03			
0.60	1.35E-03	0.00E+00	1.35E-03			
0.65	8.63E-04	0.00E+00	8.63E-04			
0.70	4.74E-04	0.00E+00	4.74E-04			
0.80	0.00E+00	0.00E+00	0.00E+00			

# Hand Solutions for Set 1, Test Case 5

nanu Solutions for Set 1, Test Case 7							
Peak Ground Acceleration (g)	Site 4	Site 5	Site 6				
0.001	1.14E-02	1.14E-02	1.14E-02				
0.01	1.14E-02	1.14E-02	1.14E-02				
0.05	1.14E-02	1.03E-02	1.14E-02				
0.1	1.01E-02	7.65E-03	1.01E-02				
0.15	8.72E-03	5.66E-03	8.72E-03				
0.2	7.75E-03	3.50E-03	7.75E-03				
0.25	6.84E-03	1.40E-03	6.84E-03				
0.3	5.95E-03	4.89E-06	5.95E-03				
0.35	5.06E-03	0.00E+00	5.06E-03				
0.4	4.18E-03	0.00E+00	4.18E-03				
0.45	3.34E-03	0.00E+00	3.34E-03				
0.5	2.56E-03	0.00E+00	2.56E-03				
0.55	1.85E-03	0.00E+00	1.85E-03				
0.6	1.20E-03	0.00E+00	1.20E-03				
0.7	1.87E-04	0.00E+00	1.87E-04				
0.80	0.00E+00	0.00E+00	0.00E+00				

Hand Solutions for Set 1, Test Case 9b						
Peak Ground Acceleration	Site 1	Site 2	Site 7			
(g)						
0.001	1.68E-02	1.68E-02	1.68E-02			
0.01	1.68E-02	1.68E-02	1.68E-02			
0.05	1.68E-02	1.68E-02	1.68E-02			
0.1	1.68E-02	1.68E-02	1.68E-02			
0.15	1.68E-02	1.68E-02	1.68E-02			
0.2	1.68E-02	1.68E-02	1.68E-02			
0.25	1.68E-02	1.68E-02	1.68E-02			
0.3	1.68E-02	1.68E-02	8.76E-03			
0.35	1.68E-02	1.68E-02	8.46E-04			
0.4	1.68E-02	1.68E-02	0.00E+00			
0.45	1.68E-02	1.68E-02	0.00E+00			
0.5	1.68E-02	0.00E+00	0.00E+00			
0.55	1.46E-02	0.00E+00	0.00E+00			
0.6	1.22E-02	0.00E+00	0.00E+00			
0.7	7.66E-03	0.00E+00	0.00E+00			
0.8	2.70E-03	0.00E+00	0.00E+00			

## Hand Solutions for Set 1, Test Case 7

## MEAN RESULTS FOR TEST CASES WITHOUT HAND SOLUTIONS

	171	can results set 1, C	азс т	
Peak Ground Acceleration (g)	Site 3	Site 4	Site 5	Site 6
0.001	1.68E-02	1.68E-02	1.68E-02	1.68E-02
0.01	1.68E-02	1.68E-02	1.68E-02	1.68E-02
0.05		1.68E-02	1.68E-02	1.68E-02
0.1		1.68E-02	1.68E-02	1.68E-02
0.15		1.68E-02	1.23E-02	1.68E-02
0.2		1.68E-02	5.22E-03	1.68E-02
0.25		1.57E-02	4.75E-04	1.57E-02
0.3		1.18E-02		1.18E-02
0.35		8.42E-03		8.40E-03
0.4		5.11E-03		5.09E-03
0.45		2.88E-03		2.86E-03
0.5		1.50E-03		
0.55		6.44E-04		
0.6		1.75E-04		

## Mean Results Set 1, Case 4

## Mean Results Set 1, Case 5

Peak Ground Acceleration (g)	Site 1	Site 2	Site 3	Site 7
0.001	4.00E-02	4.00E-02	4.00E-02	4.00E-02
0.01	4.00E-02	4.00E-02	4.00E-02	4.00E-02
0.05	4.00E-02	4.00E-02		4.00E-02
0.1	3.99E-02	3.31E-02		3.31E-02
0.15	3.46E-02	1.22E-02		1.22E-02
0.2	2.57E-02	4.85E-03		4.85E-03
0.25	1.89E-02	1.76E-03		1.76E-03
0.3	1.37E-02	2.40E-04		2.40E-04
0.35	9.88E-03			
0.4	6.93E-03			
0.45	4.84E-03			
0.5	3.36E-03			
0.55	2.34E-03			
0.6	1.52E-03			
0.7	5.12E-04			

	Witan N	csuits Set 1, Case 0		
Peak Ground Acceleration (g)	Site 1	Site 2	Site 3	Site 7
0.001	7.74E-03	7.74E-03	7.74E-03	7.74E-03
0.01	7.74E-03	7.74E-03	7.74E-03	7.74E-03
0.05	7.74E-03	7.74E-03		7.74E-03
0.1	7.74E-03	7.74E-03		7.74E-03
0.15	7.74E-03	7.70E-03		7.70E-03
0.2	7.73E-03	6.77E-03		6.77E-03
0.25	7.69E-03	3.60E-03		3.60E-03
0.3	7.55E-03	4.50E-04		4.50E-04
0.35	7.21E-03			
0.4	6.65E-03			
0.45	5.89E-03			
0.5	4 98E-03			

Mean Results Set 1, Case 7						
Peak Ground Acceleration (g)	Site 1	Site 2	Site 3	Site 7		
0.001	1.16E-02	1.16E-02	1.16E-02	1.16E-02		
0.01	1.16E-02	1.16E-02	1.16E-02	1.16E-02		
0.05	1.16E-02	1.16E-02		1.16E-02		
0.1	1.16E-02	1.06E-02		1.06E-02		
0.15	1.09E-02	7.79E-03		7.79E-03		
0.2	9.67E-03	6.76E-03		6.76E-03		
0.25	8.66E-03	3.62E-03		3.62E-03		
0.3	7.96E-03					
0.35	7.39E-03					
0.4	6.71E-03					
0.45	5.87E-03					
0.5	4.95E-03					
0.55	4.00E-03					
0.6	2.91E-03					
0.7	8.50E-04					

## Mean Results Set 1, Case 6

Peak Ground	Site 1	Site 2	Site 3	Site 4	Site 5	Site 6	Site 7
Acceleration (g)							
0.001	1.59E-02						
0.01	1.59E-02	1.59E-02	1.57E-02	1.59E-02	1.59E-02	1.59E-02	1.59E-02
0.05	1.59E-02	1.59E-02	3.42E-03	1.59E-02	1.55E-02	1.59E-02	1.59E-02
0.1	1.59E-02	1.47E-02	3.19E-04	1.55E-02	1.20E-02	1.55E-02	1.47E-02
0.15	1.56E-02	1.20E-02	4.15E-05	1.41E-02	7.98E-03	1.40E-02	1.20E-02
0.2	1.48E-02	8.98E-03	7.37E-06	1.22E-02	4.99E-03	1.22E-02	8.98E-03
0.25	1.36E-02	6.41E-03	1.61E-06	1.03E-02	3.08E-03	1.02E-02	6.41E-03
0.3	1.22E-02	4.49E-03	4.03E-07	8.39E-03	1.91E-03	8.38E-03	4.49E-03
0.35	1.09E-02	3.09E-03		6.80E-03	1.21E-03	6.79E-03	3.09E-03
0.4	9.50E-03	2.14E-03		5.49E-03	7.68E-04	5.48E-03	2.14E-03
0.45	8.12E-03	1.49E-03		4.37E-03	4.99E-04	4.36E-03	1.49E-03
0.5	6.99E-03	1.04E-03		3.52E-03	3.25E-04	3.51E-03	1.04E-03
0.55	5.99E-03	7.40E-04		2.84E-03	2.19E-04	2.83E-03	7.40E-04
0.6	5.12E-03	5.24E-04		2.29E-03	1.48E-04	2.28E-03	5.24E-04
0.7	3.68E-03	2.68E-04		1.51E-03	7.01E-05	1.50E-03	2.68E-04
0.8	2.65E-03	1.44E-04		1.00E-03	3.50E-05	9.97E-04	1.44E-04
0.9	1.91E-03	7.89E-05		6.74E-04	1.81E-05	6.71E-04	7.89E-05
1	1.40E-03	4.48E-05		4.58E-04	9.72E-06	4.56E-04	4.48E-05

Mean Results Set 1, Case 8a

Mean Results Set 1, Case 8b

Peak Ground	Site 1	Site 2	Site 3	Site 4	Site 5	Site 6	Site 7
Acceleration (g)							
0.001	1.59E-02						
0.01	1.59E-02	1.59E-02	1.57E-02	1.59E-02	1.59E-02	1.59E-02	1.59E-02
0.05	1.59E-02	1.59E-02	3.14E-03	1.59E-02	1.56E-02	1.59E-02	1.59E-02
0.1	1.59E-02	1.47E-02		1.55E-02	1.20E-02	1.55E-02	1.47E-02
0.15	1.56E-02	1.19E-02		1.41E-02	7.85E-03	1.41E-02	1.19E-02
0.2	1.48E-02	8.87E-03		1.22E-02	4.78E-03	1.22E-02	8.87E-03
0.25	1.36E-02	6.17E-03		1.02E-02	2.80E-03	1.02E-02	6.17E-03
0.3	1.22E-02	4.23E-03		8.28E-03	1.59E-03	8.27E-03	4.23E-03
0.35	1.07E-02	2.81E-03		6.58E-03	8.67E-04	6.57E-03	2.81E-03
0.4	9.30E-03	1.83E-03		5.25E-03	4.55E-04	5.23E-03	1.83E-03
0.45	8.00E-03	1.15E-03		4.16E-03	2.28E-04	4.11E-03	1.15E-03
0.5	6.83E-03			3.25E-03		3.24E-03	
0.55	5.74E-03			2.53E-03		2.52E-03	
0.6	4.85E-03			1.98E-03		1.97E-03	
0.7	3.40E-03			1.18E-03		1.17E-03	
0.8	2.33E-03			7.03E-04		6.92E-04	
0.9	1.57E-03			4.08E-04		4.02E-04	
1	1.04E-03			2.28E-04		2.27E-04	

Peak Ground	Site 1	Site 2	Site 3	Site 4	Site 5	Site 6	Site 7
Acceleration							
(g)							
0.001	1.59E-02						
0.01	1.59E-02	1.59E-02	1.57E-02	1.59E-02	1.59E-02	1.59E-02	1.59E-02
0.05	1.59E-02	1.59E-02	3.40E-03	1.59E-02	1.55E-02	1.59E-02	1.59E-02
0.1	1.59E-02	1.47E-02	2.97E-04	1.55E-02	1.20E-02	1.55E-02	1.47E-02
0.15	1.56E-02	1.20E-02	1.99E-05	1.41E-02	7.97E-03	1.41E-02	1.20E-02
0.2	1.48E-02	8.97E-03		1.22E-02	4.96E-03	1.22E-02	8.97E-03
0.25	1.36E-02	6.40E-03		1.03E-02	3.05E-03	1.02E-02	6.40E-03
0.3	1.22E-02	4.47E-03		8.40E-03	1.88E-03	8.38E-03	4.47E-03
0.35	1.09E-02	3.08E-03		6.80E-03	1.17E-03	6.79E-03	3.08E-03
0.4	9.49E-03	2.12E-03		5.48E-03	7.42E-04	5.47E-03	2.12E-03
0.45	8.12E-03	1.47E-03		4.36E-03	4.70E-04	4.35E-03	1.47E-03
0.5	6.97E-03	1.02E-03		3.51E-03	2.99E-04	3.50E-03	1.02E-03
0.55	5.97E-03	7.14E-04		2.82E-03	1.93E-04	2.81E-03	7.14E-04
0.6	5.04E-03	5.01E-04		2.27E-03	1.24E-04	2.27E-03	5.01E-04
0.7	3.65E-03	2.48E-04		1.49E-03	5.08E-05	1.48E-03	2.48E-04
0.8	2.62E-03	1.23E-04		9.79E-04	1.98E-05	9.66E-04	1.23E-04
0.9	1.88E-03			6.52E-04		6.42E-04	
1	1.36E-03			4.37E-04		4.35E-04	

Mean Results Set 1, Case 8c

Mean Results Set 1, Case 9	a
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Peak Ground	Site 1	Site 2	Site 3	Site 4	Site 5	Site 6	Site 7
Acceleration							
0.001	1.69E-02						
0.01	1.69E-02	1.69E-02	1.68E-02	1.69E-02	1.69E-02	1.69E-02	1.69E-02
0.05	1.69E-02	1.68E-02	6.90E-03	1.68E-02	1.66E-02	1.68E-02	1.68E-02
0.1	1.68E-02	1.65E-02	1.14E-03	1.66E-02	1.40E-02	1.66E-02	1.58E-02
0.15	1.65E-02	1.48E-02	1.99E-04	1.56E-02	1.03E-02	1.56E-02	1.31E-02
0.2	1.58E-02	1.26E-02	2.79E-05	1.39E-02	6.99E-03	1.39E-02	1.02E-02
0.25	1.47E-02	1.02E-02		1.20E-02	4.64E-03	1.20E-02	7.50E-03
0.3	1.34E-02	7.89E-03		1.02E-02	3.07E-03	1.02E-02	5.40E-03
0.35	1.19E-02	6.02E-03		8.45E-03	2.04E-03	8.43E-03	3.85E-03
0.4	1.05E-02	4.61E-03		6.95E-03	1.36E-03	6.94E-03	2.73E-03
0.45	9.15E-03	3.50E-03		5.70E-03	9.21E-04	5.69E-03	1.94E-03
0.5	7.94E-03	2.64E-03		4.66E-03	6.22E-04	4.65E-03	1.39E-03
0.55	6.85E-03	1.98E-03		3.81E-03	4.22E-04	3.80E-03	9.92E-04
0.6	5.90E-03	1.53E-03		3.16E-03	2.91E-04	3.11E-03	7.20E-04
0.7	4.30E-03	8.78E-04		2.12E-03	1.37E-04	2.11E-03	3.74E-04
0.8	3.16E-03	5.00E-04		1.43E-03	6.41E-05	1.43E-03	1.96E-04
0.9	2.30E-03	2.97E-04		9.87E-04	2.91E-05	9.83E-04	1.01E-04
1	1.68E-03	1.73E-04		6.77E-04	1.23E-05	6.74E-04	4.99E-05

Peak Ground	Site 3	Site 4	Site 5	Site 6
Acceleration (g)				
0.001	1.69E-02	1.69E-02	1.69E-02	1.69E-02
0.01	1.69E-02	1.69E-02	1.69E-02	1.69E-02
0.05	1.69E-02	1.69E-02	1.69E-02	1.69E-02
0.1		1.69E-02	1.69E-02	1.69E-02
0.15		1.69E-02	1.69E-02	1.69E-02
0.2		1.69E-02	1.11E-02	1.69E-02
0.25		1.69E-02	5.74E-03	1.69E-02
0.3		1.67E-02	2.02E-03	1.67E-02
0.35		1.46E-02		1.45E-02
0.4		1.19E-02		1.19E-02
0.45		9.80E-03		9.77E-03
0.5		7.90E-03		7.87E-03
0.55		5.81E-03		5.72E-03
0.6		4.09E-03		4.06E-03
0.7		1.77E-03		1.72E-03
0.8		2.85E-04		2.80E-04
0.9				
1				

#### Mean Results Set 1, Case 9b

## Mean Results Set 1, Case 10

Peak Ground Acceleration (g)	Site 1	Site 2	Site 3	Site 4
0.001	3.87E-02	3.87E-02	3.87E-02	3.83E-02
0.01	2.19E-02	1.82E-02	9.32E-03	5.33E-03
0.05	2.97E-03	2.96E-03	1.39E-03	1.25E-04
0.1	9.22E-04	9.21E-04	4.41E-04	1.63E-06
0.15	3.59E-04	3.59E-04	1.76E-04	
0.2	1.31E-04	1.31E-04	6.47E-05	
0.25	4.76E-05	4.76E-05	2.27E-05	
0.3	1.72E-05	1.72E-05	8.45E-06	
0.35	5.38E-06	5.37E-06	2.66E-06	
0.4	1.18E-06	1.18E-06	5.84E-07	

Peak Ground Acceleration (g)	Site 1	Site 2	Site 3	Site 4
0.001	3.87E-02	3.87E-02	3.87E-02	3.84E-02
0.01	2.18E-02	1.81E-02	9.27E-03	5.33E-03
0.05	2.83E-03	2.83E-03	1.32E-03	1.18E-04
0.1	7.91E-04	7.90E-04	3.79E-04	1.24E-06
0.15	2.43E-04	2.44E-04	1.18E-04	
0.2	7.33E-05	7.32E-05	3.60E-05	
0.25	2.23E-05	2.21E-05	1.08E-05	
0.3	6.42E-06	6.50E-06	2.95E-06	
0.35	1.31E-06	1.30E-06	6.18E-07	
0.4	1.72E-07	1.60E-07	7.92E-08	
0.45	3.05E-09	3.09E-09	1.34E-09	

Mean Results Set 1, Case 11





A - 18







A - 20



A - 21



A - 22



A - 23



A - 24









A - 28









A - 31


















A - 40









A - 44



































A - 57



A - 58





A - 60




































































































A - 106









A - 110




























(Coordinates are in Set2\_Rev2\_Coordinates\_Results.xls)

	PEER PSHA VERIFICATION	FAULT AND SITE GEOMETRY	Figure
		FOR CASE 2	3.108















(Coordinates are in Set2\_Rev2\_Coordinates\_Results.xls)

	PEER PSHA VERIFICATION	FAULT AND SITE GEOMETRY	Figure
		FOR CASE 6	3.115







A - 134

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