## PACIFIC EARTHQUAKE ENGINEERING RESEARCH CENTER

## Verification of Probabilistic Seismic Hazard Analysis Computer Programs

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#### Abstract

Probabilistic seismic hazard analysis (PSHA) has become a fundamental tool in assessing seismic hazards and for estimating seismic design and seismic safety evaluation of ground motions. It is used both on a site-specific basis for important and critical facilities and on a national scale for building codes. This report describes a project to test and verify the numerical approaches and software used in PSHA. The project was sponsored by the Pacific Earthquake Engineering Research (PEER) Center's Lifelines Program. A Working Group was organized and members tested their own computer codes in two sets of tests. Through several iterations, codes were tested and acceptable answers were established either through analytical solutions or as the consensus answer from the test case results. The verification tests are available to any PSHA code developer/user worldwide through this publication and the PEER website. The test cases will be used as a standard verification for all PSHA codes to be used in projects for the PEER Lifelines Program sponsors, which include the California Department of Transportation (Caltrans), the Pacific Gas \& Electric Company (PG\&E), and the California Energy Commission (CEC).


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## CONTENTS

ABSTRACT ..... iii
ACKNOWLEDGMENTS ..... iv
TABLE OF CONTENTS ..... v
LIST OF FIGURES ..... vii
LIST OF TABLES ..... xi
1 INTRODUCTION ..... 1
2 APPROACH ..... 3
2.1 Verification Process ..... 7
2.2 General PSHA Theory ..... 8
3 TEST CASES AND RESULTS ..... 11
3.1 Test Case Set 1 ..... 11
3.2 Test Case Set 2 ..... 21
4 CONCLUSIONS ..... 25
REFERENCES ..... 27
APPENDIX A

## LIST OF FIGURES

Figure 3.1 Fault and Site Geometry for Test Case Set 1 ..... A-17
Figure 3.2 Test Set 1, Case 1, Site 1 ..... A-18
Figure 3.3 Test Set 1, Case 1, Site 2 ..... A-19
Figure 3.4 Test Set 1, Case 1, Site 3 ..... A-20
Figure 3.5 Test Set 1, Case 1, Site 4 ..... A-21
Figure 3.6 Test Set 1, Case 1, Site 5 ..... A-22
Figure 3.7 Test Set 1, Case 1, Site 6 ..... A-23
Figure 3.8 Test Set 1, Case 1, Site 7 ..... A-24
Figure 3.9 Test Set 1, Case 1, Site 1, Early Results ..... A-25
Figure 3.10 Test Set 1, Case 2, Site 1 ..... A-26
Figure 3.11 Test Set 1, Case 2, Site 2 ..... A-27
Figure 3.12 Test Set 1, Case 2, Site 3 ..... A-28
Figure 3.13 Test Set 1, Case 2, Site 4 ..... A-29
Figure 3.14 Test Set 1, Case 2, Site 5 ..... A-30
Figure 3.15 Test Set 1, Case 2, Site 6 ..... A-31
Figure 3.16 Test Set 1, Case 2, Site 7 ..... A-32
Figure 3.17 Test Set 1, Case 3, Site 1 ..... A-33
Figure 3.18 Test Set 1, Case 3, Site 2 ..... A-34
Figure 3.19 Test Set 1, Case 3, Site 3 ..... A-35
Figure 3.20 Test Set 1, Case 3, Site 4 ..... A-36
Figure 3.21 Test Set 1, Case 3, Site 5 ..... A-37
Figure 3.22 Test Set 1, Case 3, Site 6 ..... A-38
Figure 3.23 Test Set 1, Case 3, Site 7 ..... A-39
Figure 3.24 Test Set 1, Case 4, Site 4, Early Results ..... A-40
Figure 3.25 Test Set 1, Case 4, Site 6, Early Results ..... A-41
Figure 3.26 Test Set 1, Case 4, Site 1 ..... A-42
Figure 3.27 Test Set 1, Case 4, Site 2 ..... A-43
Figure 3.28 Test Set 1, Case 4, Site 3 ..... A-44
Figure 3.29 Test Set 1, Case 4, Site 4 ..... A-45
Figure 3.30 Test Set 1, Case 4, Site 5 ..... A-46
Figure 3.31 Test Set 1, Case 4, Site 6 ..... A-47
Figure 3.32 Test Set 1, Case 4, Site 7 ..... A-48
Figure 3.33 Test Set 1, Case 5, Site 4, Early Results ..... A-49
Figure 3.34 Test Set 1, Case 5, Site 1 ..... A-50
Figure 3.35 Test Set 1, Case 5, Site 2 ..... A-51
Figure 3.36 Test Set 1, Case 5, Site 3 ..... A-52
Figure 3.37 Test Set 1, Case 5, Site 4 ..... A-53
Figure 3.38 Test Set 1, Case 5, Site 5 ..... A-54
Figure 3.39 Test Set 1, Case 5, Site 6 ..... A-55
Figure 3.40 Test Set 1, Case 5, Site 7 ..... A-56
Figure 3.41 Test Set 1, Case 6, Site 1 ..... A-57
Figure 3.42 Test Set 1, Case 6, Site 2 ..... A-58
Figure 3.43 Test Set 1, Case 6, Site 3 ..... A-59
Figure 3.44 Test Set 1, Case 6, Site 4 ..... A-60
Figure 3.45 Test Set 1, Case 6, Site 5 ..... A-61
Figure 3.46 Test Set 1, Case 6, Site 6 ..... A-62
Figure 3.47 Test Set 1, Case 6, Site 7 ..... A-63
Figure 3.48 Test Set 1, Case 7, Site 6, Early Results ..... A-64
Figure 3.49 Test Set 1, Case 7, Site 1 ..... A-65
Figure 3.50 Test Set 1, Case 7, Site 2 ..... A-66
Figure 3.51 Test Set 1, Case 7, Site 3 ..... A-67
Figure 3.52 Test Set 1, Case 7, Site 4 ..... A-68
Figure 3.53 Test Set 1, Case 7, Site 5 ..... A-69
Figure 3.54 Test Set 1, Case 7, Site 6 ..... A-70
Figure 3.55 Test Set 1, Case 7, Site 7 ..... A-71
Figure 3.56 Test Set 1, Case 8a, Site 1 ..... A-72
Figure 3.57 Test Set 1, Case 8a, Site 2 ..... A-73
Figure 3.58 Test Set 1, Case 8a, Site 3 ..... A-74
Figure 3.59 Test Set 1, Case 8a, Site 4 ..... A-75
Figure 3.60 Test Set 1, Case 8a, Site 5 ..... A-76
Figure 3.61 Test Set 1, Case 8a, Site 6 ..... A-77
Figure 3.62 Test Set 1, Case 8a, Site 7 ..... A-78
Figure 3.63 Test Set 1, Case 8b, Site 1 ..... A-79
Figure 3.64 Test Set 1, Case 8b, Site 2 ..... A-80
Figure 3.65 Test Set 1, Case 8b, Site 3 ..... A-81
Figure 3.66 Test Set 1, Case 8b, Site 4 ..... A-82
Figure 3.67 Test Set 1, Case 8b, Site 5 ..... A-83
Figure 3.68 Test Set 1, Case 8b, Site 6 ..... A-84
Figure 3.69 Test Set 1, Case 8b, Site 7 ..... A-85
Figure 3.70 Test Set 1, Case 8c, Site 1 ..... A-86
Figure 3.71 Test Set 1, Case 8c, Site 2 ..... A-87
Figure 3.72 Test Set 1, Case 8c, Site 3 ..... A-88
Figure 3.73 Test Set 1, Case 8c, Site 4 ..... A-89
Figure 3.74 Test Set 1, Case 8c, Site 5 ..... A-90
Figure 3.75 Test Set 1, Case 8c, Site 6 ..... A-91
Figure 3.76 Test Set 1, Case 8c, Site 7 ..... A-92
Figure 3.77 Test Set 1, Case 9a, Site 1 ..... A-93
Figure 3.78 Test Set 1, Case 9a, Site 2 ..... A-94
Figure 3.79 Test Set 1, Case 9a, Site 3 ..... A-95
Figure 3.80 Test Set 1, Case 9a, Site 4 ..... A-96
Figure 3.81 Test Set 1, Case 9a, Site 5 ..... A-97
Figure 3.82 Test Set 1, Case 9a, Site 6 ..... A-98
Figure 3.83 Test Set 1, Case 9a, Site 7 ..... A-99
Figure 3.84 Test Set 1, Case 9b, Site 1 ..... A-100
Figure 3.85 Test Set 1, Case 9b, Site 2 ..... A-101
Figure 3.86 Test Set 1, Case 9b, Site 3 ..... A-102
Figure 3.87 Test Set 1, Case 9b, Site 4 ..... A-103
Figure 3.88 Test Set 1, Case 9b, Site 5 ..... A-104
Figure 3.89 Test Set 1, Case 9b, Site 6 ..... A-105
Figure 3.90 Test Set 1, Case 9b, Site 7 ..... A-106
Figure 3.91 Test Set 1, Case 9c, Site 1 ..... A-107
Figure 3.92 Test Set 1, Case 9c, Site 2 ..... A-108
Figure 3.93 Test Set 1, Case 9c, Site 3 ..... A-109
Figure 3.94 Test Set 1, Case 9c, Site 4 ..... A-110
Figure 3.95 Test Set 1, Case 9c, Site 5 ..... A-111
Figure 3.96 Test Set 1, Case 9c, Site 6 ..... A-112
Figure 3.97 Test Set 1, Case 9c, Site 7 ..... A-113
Figure 3.98 Test Set 1, Case 10, Site 1 ..... A-114
Figure 3.99 Test Set 1, Case 10, Site 2 ..... A-115
Figure 3.100 Test Set 1, Case 10, Site 3 ..... A-116
Figure 3.101 Test Set 1, Case 10, Site 4 ..... A-117
Figure 3.102 Test Set 1, Case 11, Site 1 ..... A-118
Figure 3.103 Test Set 1, Case 11, Site 2 ..... A-119
Figure 3.104 Test Set 1, Case 11, Site 3 ..... A-120
Figure 3.105 Test Set 1, Case 11, Site 4 ..... A-121
Figure 3.106 Fault and Site Geometry for Cases 1 and 5 ..... A-122
Figure 3.107 Test Set 2, Case 1, Site 1, Early Results ..... A-123
Figure 3.108 Fault and Site Coordinates for Case 2 ..... A-124
Figure 3.109 Test Set 2, Case 2, Site 1, Early Results ..... A-125
Figure 3.110 Fault and Site Geometry for Cases 3 and 4 ..... A-126
Figure 3.111 Test Set 2, Case 3, Site 1, Early Results ..... A-127
Figure 3.112 Test Set 2, Case 4, Site 1, Early Results ..... A-128
Figure 3.113 Logic Tree for Case 5 ..... A-129
Figure 3.114 Test Set 2, Case 5, Site 1, Early Results ..... A-130
Figure 3.115 Fault and Site Geometry for Case 6. ..... A-131
Figure 3.116 Test Set 2, Case 6, Site 1, Early Results ..... A-132
Figure 3.117 Intraslab Zone and Site Geometry for Case 7 ..... A-133
Figure 3.118 Test Set 2, Case 7, Site 1, Early Results ..... A-134

## LIST OF TABLES

Table 2.1 PSHA code properties ..... 4
Table 3.1 Test case set 1 ..... 13
Table 3.2 Median PGA values at sites 1-7 ..... 15

## 1 Introduction

In the past three decades, the approach to estimating earthquake ground shaking hazard, particularly to critical and important facilities, has slowly evolved from the traditional deterministic earthquake scenario analysis to probabilistic seismic hazard analysis (PSHA). A prime example is the very comprehensive PSHA that was performed to evaluate both ground shaking and fault displacement hazards at Yucca Mountain, the site of the nation's first nuclear waste repository (Stepp et al. 2001). The National Seismic Hazard Maps developed by the U.S. Geological Survey (USGS), which form the basis of building codes in the U.S. (e.g., International Building Code) are based on PSHA (Frankel et al. 1996; Petersen et al. 2008). Thus PSHA has become the primary tool in estimating seismic hazards in the U.S. and is gaining widespread use worldwide.

The results from PSHA also form the basis for (1) design ground motions specified in structural codes and standards (e.g., AASHTO for bridges); (2) site-specific design of important and critical facilities such as all U.S. Department of Energy facilities (e.g., national laboratories and Yucca Mountain); (3) site-specific design for nuclear power plants and interim nuclear waste storage sites; (4) safety analysis evaluations of important/critical facilities such as U.S. Bureau of Reclamation dams; (5) loss estimation to establish insurance rates; and many other uses. PSHA is now being used by federal and state agencies, which have traditionally used only a deterministic approach for estimating ground motions. Examples of such agencies are the U.S. Army Corps of Engineers and the California Division of Safety of Dams.

PSHA has its roots in the seminal paper by Cornell (1968). The objective in PSHA is to estimate the probability that a specified level of ground motion will be exceeded or to estimate the level of ground motions that will occur at a specified exceedance probability. PSHA integrates hazard from all significant seismic sources and incorporates the frequency of earthquakes from each seismic source. A significant aspect of PSHA is that it allows for the explicit treatment of uncertainty in the inputs. The uncertainties can be quite large in
characterizing seismic sources and ground motion attenuation. For a comprehensive discussion of PSHA, we refer the reader to the EERI monograph Seismic Hazard and Risk Analysis by McGuire (2004) or the Senior Seismic Hazard Advisory Committee (1997) report.

Despite the relatively widespread use both nationally and internationally of PSHA, only a few publicly available and proprietary PSHA computer codes have been developed. In large part, this is because PSHA calculations are still being done by a relatively small proportion of the professional community. Because of the importance of PSHA in seismic design, the Pacific Earthquake Engineering Research (PEER) Center's Lifelines Program sponsored a Working Group to verify both the numerical approaches and computer software used in PSHA. To our knowledge, this is the first ever comprehensive, organized, and structured verification of PSHA software. This project is one of several projects sponsored by the PEER Center's Lifelines Program to improve tools in seismic hazard estimation. The goal of the Lifelines Program is to increase the safety and reliability of utility and transportation systems in earthquakes through better characterization of the hazards and improved performance of system components.

The objective of the project was to develop a set of standard exercises that can be used by current and future PSHA software developers to validate their codes. The verification process will also provide the means for the PEER Lifelines Program sponsors (the California Department of Transportation, the Pacific Gas and Electric Company, and the California Energy Commission) to ensure that work done for them by others, including consultants, is done using qualified software.

The following describes the two test case sets developed for verification, the final results for Test Case Set 1, and the sample results for Test Case Set 2.

## 2 Approach

The PSHA Validation Project was managed by Ivan Wong and Patricia Thomas (co-Principal Investigators) with assistance from Norm Abrahamson. Members of the Working Group consisted of prominent code developers from government agencies and engineering and risk analysis and management services firms. The members of the Working Group and their computer programs included:

| Member | Affiliation | Program |
| :--- | :--- | :--- |
| Tianqing Cao | California Geological Survey | haz02_ |
| Ned Field | U.S. Geological Survey | OpenSHA |
| Steve Harmsen | U.S. Geological Survey | hazFX v.3f, hazgridX v 3.f, <br> fltrate.peer.f |
| Roland LaForge | U.S. Bureau of Reclamation | faultsource_20, mrs 3.1 |
| Robin McGuire | Risk Engineering | EZ-FRISK |
| Andres Mendez | Impact Forecasting | EQ-Elements |
| Badie Rowshandel | California Geological Survey | HAZDIR |
| Jean Savy | Lawrence Livermore National <br> Laboratory | ALEAS |
| Mark Stirling | New Zealand Institute of Geological <br> and Nuclear Sciences | NEWHAZ |
| Phalkun Tan | GeoPentech | GP-Haz |
| Gabriel Toro | Risk Engineering | FRISK88M Version 2.05 |
| Bob Youngs | Geomatrix Consultants | XCD52, HAZ50, TREE50 |

The Working Group tested both publicly available codes as well as proprietary codes that have been used extensively in hazard evaluation in the U.S. and worldwide. Basic attributes of the various codes are listed in Table 2.1. Three publicly available codes were tested: EZ-FRISK developed by Risk Engineering, Inc.; HAZ38 developed by Norm Abrahamson; and OpenSHA developed by the U.S. Geological Survey. The former is a widely used code both in the U.S. and internationally. HAZ38 was tested by the PIs. OpenSHA was tested by Ned Field. The basic codes used in the development of the U.S. Geological Survey's National Hazard Maps were
tested by Steve Harmsen. The project began in November 2001. A paper that described the early stages of the project was published in 2004 (Wong et al. 2004).

Table 2.1a PSHA code properties

| Code | Numerical Model | Truncation Of Ground Motion | Rupture Plane Modeling | Rupture Length \& Width Modeling |
| :---: | :---: | :---: | :---: | :---: |
| FRISK88M Version 2.0 G. Toro | Polynomial (26.2.17 of Abramowitz \& Stegun) | \# Standard <br> Deviations <br> Max. Ground Motion | Horizontal location \& hypocentral depth is uniformly distributed. Rupture confined to fault plane. | User inputs $\log \mathrm{L}=\mathrm{a}+\mathrm{bM}$ and std. dev. <br> User-specified std dev <br> Width $=$ ratio * length <br> User specified ratio <br> Length \& width not to exceed fault plane |
| EZ-FRISK <br> R. McGuire | Polynomial (26.2.17 of Abramowitz \& Stegun) | \# Standard <br> Deviations <br> Max. Ground Motion | Horizontal location \& hypocentral depth is uniformly distributed. Rupture confined to fault plane. | User inputs $\log \mathrm{L}=\mathrm{a}+\mathrm{bM}$ and std. dev. <br> User-specified std. dev. <br> Width = ratio * length. <br> User specified ratio. <br> Length \& width not to exceed fault plane. |
| XDC52, <br> HAZ50, <br> TREE50 <br> B. Youngs | Series expansion | \# Standard Deviations | Uniform distribution along length. <br> User specified hypocentral depth distribution. <br> For straight-line fault, analytical distance distribution computed. For segmented fault, numerical distribution using 1 km steps. <br> Rupture confined to fault plane | Rupture area specified by loglinear relationship with magnitude. <br> Aspect ratio defined by log linear relationship, 1:1 for M 4, user specified for M 7. Aleatory variability not modeled. |
| HazFX v3.f, hazgridX v3.f, filtrate.peer.f <br> A. Frankel <br> S. Harmsen | Call to the error function | \# Standard Deviations. For CEUS relations, can also truncate at maximum ground motion. | Rupture floats along strike. Rupture confined to fault plane. | For gridded seismicity code, use W\&C Magnitude-Length relations. <br> For fault code, rupture always extends from top to bottom ( $\mathrm{Mmin}=6.5$ ). <br> No variability in rupture length or width. |
| ALEAS J. Savy | Abramowitz polynomial approximation | \# Standard <br> Deviations <br> Max. Ground Motion | Monte-Carlo simulation with model of initiation point based on probability distributions of depth and location along the fault. User notified if rupture extends off fault plane. | Rupture area is simulated from set of weighted area-magnitude relations. Area is positioned using distributions on depth and location of initiation point. |
| EQ-Elements <br> A. Mendez | Discrete numerical integration of equation | \# Standard <br> Deviations Max. Ground Motion (Code uses both at the same time.) | Rupture centroid is uniformly distributed along length. Depth of centroid is a function of the magnitude. | $\begin{aligned} & \text { Log10(A)=m-4.2 (USGS 99- } \\ & 517 \text { ) } \\ & \text { Use Abrahamson (written } \\ & \text { communication 1992) to } \\ & \text { determine width and length. } \end{aligned}$ |

Table 2.1a-Continued

| Code | Numerical Model | Truncation Of Ground Motion | Rupture Plane Modeling | Rupture Length \& Width Modeling |
| :---: | :---: | :---: | :---: | :---: |
| GP-Haz <br> P. Tan | Series approximation | \# Standard Deviations | Rupture location is discretized uniformly on fault plane. The distance between 2 discrete points can be specified. Rupture location is truncated such that $1 / 2$ the dimension of the plane does not extend beyond the ends of the fault. | Rupture area calculated first from W\&C. <br> Next, rupture length is calculated from W\&C. Width is calculated as the ratio of area to length. No aleatory variability is included. |
| NEWHAZ <br> M. Stirling | Call to error function (For PC code, this uses polynomial expression 7.1.26 in Abramowitz \& Stegun.) | \# Standard Deviations | Rupture extends to the ends of the fault segment (characteristic model for all faults). Ruptures can overlap by calculating recurrence parameters so that they balance the slip rate. No rupture extends beyond the ends of the fault. | No aleatory variability in length or width. Epistemic uncertainty by modeling overlapping ruptures (that balance the slip rate). |
| faultsource-20 mrs 3.1 <br> R. LaForge | Discrete numerical integration directly from the equation | \# Standard Deviations | EQs are modeled as square (or any other aspect ratio) rupture areas. As many areas as possible are sequenced on plane starting in one corner. Pattern can be shifted along strike and dip as many times as necessary to achieve stable results | The normal distribution of rupture area as a function of magnitude (W\&C) can be incorporated. |
| OpenSHA <br> N. Field | Gamma Series | \# Standard <br> Deviations <br> Maximum <br> ground motion | Rupture floats along or down dip. <br> Rupture constrained to fault plane. | Uses M(A) relationships. Aleatory variability can be accommodated. |
| HAZDIR <br> B. Rowshandel | Direct numerical integration | Standard Deviations | Rupture is confined to fault surface. Rupture floats along strike and across width. Homogeneous rupture with unidirectional directivity effects. Heterogeneous rupture based on asperity and slip distribution. Single hypocenter and random hypocenter with specified distribution are handled. | Rupture area and length are calculated from magnitude. Rupture width is calculated from magnitude or using aspect ratio. Aleatory variability can be included. |

Table 2.1b PSHA code properties

| Code | Magnitude Density Functions | Area Source Modeling |
| :---: | :---: | :---: |
| FRISK88M Version 2.0 G. Toro | AREAS: Truncated exponential, modified exponential (Youngs et al. 1987). <br> FAULTS: Truncated exponential, modified exponential (Youngs et al. 1987), characteristic (user-specified width and ratio between exponential and characteristic portion; rate is specified as total recurrence rate or slip rate). Can model boxcar distribution as a special case of characteristic or exponential distributions. | Point source is default. Hypocenter depth fixed or random, with user-specified distribution; can also include effect of rupture width on depth distribution. Effect of rupture length for modeled background sources can be by randomizing rupture orientation or calculating distance to rupture or using analytical approximation. |
| EZ-FRISK <br> R. McGuire | AREAS: Truncated exponential, modified AREAS: Truncated exponential, modified exponential (Youngs et al. 1987). <br> FAULTS: Truncated exponential, modified exponential (Youngs et al. 1987), characteristic (user-specified width and ratio between exponential and characteristic portion; rate is specified as total recurrence rate or slip rate). Can model boxcar distribution as a special case of characteristic or exponential distributions. | Point source is default. Hypocenter depth fixed or random, with user-specified distribution; can also include effect of rupture width on depth distribution. Effect of rupture length for modeled background sources can be by randomizing rupture orientation or calculating distance to rupture or using analytical approximation. |
| XDC52, HAZ50, TREE50 <br> B. Youngs | Truncated exponential <br> Modified truncated exponential (Youngs et al. 1987) Characteristic with variable width (Youngs and Coppersmith) <br> Separate exponential characteristic components with user specified rates <br> Discrete frequencies for individual magnitude increments <br> Real time probabilities for specified time period | Area sources are modeled using closely spaced faults. |
| HazFX v3.f, hazgridX v3.f, filtrate.peer.f <br> A. Frankel <br> S. Harmsen | For gridded seismicity code, use truncated exponential applied to density function. For fault code, also have a maximum magnitude model. | For gridded seismicity code, above $\mathrm{M}=6.0$ use vertical faults (line sources) with random strike centered on each grid point with fixed depth. For $\mathrm{M}<6.0$ use point sources. |
| ALEAS J. Savy | Truncated exponential <br> Characteristic models: <br> Standard Youngs and Coppersmith <br> Segmented model of the types developed by <br> WG99. (Input slip rates, probabilities of segmentations, segment lengths, with uncertainty on their endings \& lengths). <br> Completely empirical occurrence curve defined at magnitude points, with uncertainty. | Area sources modeled as horizontal planes. |
| EQ-Elements <br> A. Mendez | Truncated exponential Characteristic | Area sources are modeled as faults. <br> When a-value, b, \& Mmax known over a spatial grid, faults are randomly generated over grid. When input is "complete" EQ catalog, a-value is calculated over a spatial grid through the use of an elliptical spatial weighting function applied to each event. EQ events are generated as in (a). When area is polygon, the area is filled with faults such that the seismicity follows the input distributions. "Hard" (all EQs in polygon) and "Soft" (EQs can rupture beyond polygon edge). Can enter preferred azimuth. |

## Table 2.1b-Continued

| Code | Magnitude Density Functions | Area Source Modeling |
| :--- | :--- | :--- |
| $\begin{array}{l}\text { GP-Haz } \\ \text { P. Tan }\end{array}$ | $\begin{array}{l}\text { Truncated exponential (truncation applied to } \\ \text { density function). } \\ \text { Characteristic (Youngs and Coppersmith) }\end{array}$ | $\begin{array}{l}\text { Area sources are modeled as line sources } \\ \text { (multi-linear lines on surface) and multi-planar } \\ \text { sources (planar sources defined by 3 multi- } \\ \text { linear lines). }\end{array}$ |
| $\begin{array}{l}\text { NEWHAZ } \\ \text { M. Stirling }\end{array}$ | $\begin{array}{l}\text { Truncated exponential (truncation applied to } \\ \text { density function). } \\ \text { Characteristic (assumes one EQ size that is } \\ \text { proportional to dimensions of the fault). }\end{array}$ | $\begin{array}{l}\text { Area sources are modeled as a series of point } \\ \text { sources, with the ability to use an adaptation of } \\ \text { the Frankel Gaussian smoothing function. }\end{array}$ |
| $\begin{array}{l}\text { faultsource-20 } \\ \text { mrs 3.1 } \\ \text { R. LaForge }\end{array}$ | $\begin{array}{l}\text { Exponential } \\ \text { Characteristic } \\ \text { Maximum Moment }\end{array}$ | $\begin{array}{l}\text { Area sources are modeled as point sources with } \\ \text { fixed grid spacing. Depths are modeled as a } \\ \text { triangular distribution with peak and maximum } \\ \text { depth specified, with a near-surface } \\ \text { modification. }\end{array}$ |
| N. Field | $\begin{array}{l}\text { Dirac delta. } \\ \text { Gaussian with optional truncation. } \\ \text { Truncated exponential (truncation on density } \\ \text { function). }\end{array}$ | $\begin{array}{l}\text { Area sources are modeled as grid points on a } \\ \text { horizontal plane. }\end{array}$ |
| $\begin{array}{l}\text { HAZDIR } \\ \text { B. Rowshandel }\end{array}$ | $\begin{array}{l}\text { Truncated exponential, Gaussian, characteristic } \\ \text { (single magnitude), Characteristic (Youngs and } \\ \text { Coppersmith), Characteristic with aleatory } \\ \text { uncertainty on M M }\end{array}$ |  |
| probability density function. |  |  |\(\left.\quad \begin{array}{l}Area sources are modeled as point sources with <br>

fixed grid spacing distributed over any shape <br>
area. Horizontal source with uniform depth and <br>
dipping source with variable depth. Capable of <br>
Gaussian smoothing, as used in the USGS\end{array}\right\}\)

### 2.1 VERIFICATION PROCESS

The focus of the project was the numerical verification of the codes, and analysis and comparison of their various features. The verification exercises consisted of two sets of cases that tested fundamental aspects of the codes including how they modeled (1) faults, areal sources, and complex fault geometries, (2) recurrence models and rates, and (3) attenuation relationships and their uncertainties. The test cases ranged from the simplest to more sophisticated. The simplest cases have analytical solutions, but the more complex cases do not. "Acceptable" answers to the test cases were defined either through comparisons with the analytical solutions or the means over all results.

The test case sets were developed by the PIs and were distributed to each member of the Working Group. Each member initially ran the test cases and sent their results back to the PIs. The results were compiled for the whole Working Group and sent back to each participant without identifying the names of the codes except for their own code. This initial feedback allowed for each code developer to identify numerical errors, errors in interpretations, or
limitations in their codes and the opportunity to correct them. In some cases, this resulted in modifications of the codes. For each test case set, the above steps were followed and a workshop was held to discuss the group results, to identify discrepancies and the reasons for them, particularly if differences were due to differences in assumptions, numerical solutions, and hence features of the codes. Recommendations of minimum standards for meeting the benchmark results (e.g., $10 \%$ in probability level) were also defined to qualify the hazard codes.

A total of five workshops were held by the Working Group to discuss and evaluate the results of the two test case sets. Several iterations of running the test cases were required by the Working Group members. In some cases, test cases required re-running because of misinterpretations of the tests as well as software errors. Because of the extended duration of the project, schedule conflicts and change in affiliations prevented some of the Working Group members (Cao, Harmsen, Savy, and Stirling) from completing the test cases.

The major differences between the individual results, however, were due to differences in numerical approaches in the codes. For example, possibly the most significant difference among the Working Group members was the approach in modeling rupture areas for events smaller than the total fault area. In particular, the way the rupture area is moved along the length and width of a fault led to significant differences in the PSHA results. Some developers allowed the rupture area to extend beyond the fault. Some pushed the rupture area back onto the fault, while others tapered the slip at the edges. Some of the large differences were found to be an initial lack of clearly defined test cases (i.e., artificially set sigma to zero, not truncate sigma at zero). Other issues encountered in the test cases were the implementation of hanging wall/footwall factor in the Abrahamson and Silva (1997) attenuation relationship, the modeling of nonplanar faults with depth, and the lower limit of integration of the hazard (e.g., Mmin or negative infinity). The magnitude step size used in the test cases also led to differences in the test cases.

### 2.2 GENERAL PSHA THEORY

The standard PSHA approach is based on the model developed principally by Cornell (1968). The occurrence of earthquakes on a fault is assumed to be a Poisson process. The Poisson model is widely used and is a reasonable assumption in regions where data are sufficient to provide only an estimate of average recurrence rate (Cornell 1968). When there are sufficient data to permit a real-time estimate of the occurrence of earthquakes, the probability of exceeding a given
value can be modeled as an equivalent Poisson process in which a variable average recurrence rate is assumed. The occurrence of ground motions at the site in excess of a specified level is also a Poisson process if (1) the occurrence of earthquakes is a Poisson process and (2) the probability that any one event will result in ground motions at the site in excess of a specified level is independent of the occurrence of other events.

The probability that a ground motion parameter " $Z$ " exceeds a specified value " $z$ " in a time period " t " is given by:

$$
\begin{equation*}
\mathrm{p}(Z>z)=1-\mathrm{e}^{-v(z) \bullet t} \tag{2.1}
\end{equation*}
$$

where $v(z)$ is the annual mean number (or rate) of events in which $Z$ exceeds $z$. It should be noted that the assumption of a Poisson process for the number of events is not critical. This is because the mean number of events in time $t, v(z) \bullet t$, can be shown to be a close upper bound on the probability $\mathrm{p}(Z>z)$ for small probabilities (less than 0.10 ) that generally are of interest for engineering applications. The annual mean number of events is obtained by summing the contributions from all sources, that is:

$$
\begin{equation*}
\mathrm{v}(z)=\sum_{\mathrm{n}} v_{\mathrm{n}}(z) \tag{2.2}
\end{equation*}
$$

where $v_{\mathrm{n}}(z)$ is the annual mean number (or rate) of events on source n for which $Z$ exceeds $z$ at the site. The parameter $\nu_{\mathrm{n}}(z)$ is given by the expression:

$$
\begin{equation*}
v_{\mathrm{n}}(z)=\sum_{\mathrm{i}} \sum_{\mathrm{j}} \beta_{\mathrm{n}}\left(\mathrm{~m}_{\mathrm{i}}\right) \bullet \mathrm{p}\left(\mathrm{R}=\mathrm{r}_{\mathrm{j}} \mid \mathrm{m}_{\mathrm{i}}\right) \bullet \mathrm{p}\left(\mathrm{Z}>z \mid \mathrm{m}_{\mathrm{i}}, \mathrm{r}_{\mathrm{j}}\right) \tag{2.3}
\end{equation*}
$$

where:

$$
\begin{array}{ll}
\beta_{\mathrm{n}}\left(\mathrm{~m}_{\mathrm{i}}\right) \quad=\quad \begin{array}{l}
\text { annual mean rate of recurrence of earthquakes of magnitude } \\
\text { increment } \mathrm{m}_{\mathrm{i}} \text { on source } \mathrm{n} ;
\end{array} \\
\mathrm{p}\left(\mathrm{R}=\mathrm{r}_{\mathrm{j}} \mid \mathrm{m}_{\mathrm{i}}\right) \quad=\quad \begin{array}{l}
\text { probability that given the occurrence of an earthquake of magnitude } \\
\\
\mathrm{m}_{\mathrm{i}} \text { on source } \mathrm{n}, \mathrm{r}_{\mathrm{j}} \text { is the closest distance increment from the rupture }
\end{array} \\
\mathrm{p}\left(Z>z \mid \mathrm{m}_{\mathrm{i}}, \mathrm{r}_{\mathrm{j}}\right)=\quad \begin{array}{l}
\text { surface to the site; }
\end{array} \\
\begin{array}{l}
\text { probability that given an earthquake of magnitude } \mathrm{m}_{\mathrm{i}} \text { at a distance } \\
\text { of } \mathrm{r}_{\mathrm{j}}, \text { the ground motion exceeds the specified level } z .
\end{array}
\end{array}
$$

## 3 Test Cases and Results

Two sets of test cases were developed to evaluate elements of the PSHA codes. The objective of Test Case Set 1 was to test some basic elements of the codes, including how rupture areas were modeled on a fault plane, how recurrence models were used, how area sources were modeled, and how the standard deviations (sigma) in attenuation relationships were incorporated into the hazard calculations.

The purpose of Test Case Set 2 was to test more sophisticated elements of the codes such as the modeling of non-planar faults, listric faults, and the intraslab regions of subduction zones (Wadati-Benioff zones), multiple seismic sources, recurrence intervals as implemented with recurrence models, use of logic trees, computation of fractiles, and deaggregation.

The solutions to Test Case Set 1 are shown in the Appendix. The solutions to test Case Set 2 are not provided because consensus results were not reached due to schedule constraints (Section 3.2).

### 3.1 TEST CASE SET 1

Test Case 1 underwent three revisions due to not readily explainable differences in results in the first two versions. This third version was chosen to focus on the simple test cases of Set 1. The solutions have been calculated by hand and with Microsoft Excel for some of the test cases. To aid in the process, magnitude probability functions and distance probability functions have been provided for many of the cases and sites. Figure 3.1 illustrates the fault and site geometry. Site and source coordinates are provided in Appendix A.

The following were the instructions to the Working Group Members:
Please provide mean hazard results (probability of exceedance) for peak horizontal acceleration (PGA) defined at $0.001,0.01,0.05,0.1,0.15,0.2,0.25,0.3,0.35,0.4,0.45,0.5,0.55,0.6,0.7$,
$0.8,0.9$, and 1.0 g . Assume a Poisson model when converting rates to annual probabilities of exceedance. Hand-calculated solutions are provided in Appendix A for the following test cases: $1,2,4,5,6,7$, and 9 b . For tests cases and sites without hand-calculated solutions, mean results from the group of participants is provided in Appendix A.

- Use 16.05 (not 16.1 ) in the equation $\operatorname{logM}_{0}=16.05+1.5 \mathbf{M}$
- Use $3 \times 10^{11}$ dyne/cm ${ }^{2}$
- Use a magnitude integration step size small enough to define the specified magnitude density function. The bin size for magnitude integration should be defined such that the $\mathrm{M}_{\text {min }}$ is at the lower edge of a bin, not in the center (i.e., If your magnitude step size is 0.01 , one magnitude bin should be from $\mathbf{M} 5.0$ to 5.01 )
- When integrating over the magnitude density function, integrate from zero (not $\mathrm{M}_{\min }$ )
- Use uniform slip with tapered edges. Downdip and along-strike integration step size should be small enough to produce uniform rupture location. Do not allow rupture off the ends of fault.
- Maintain the aspect ratio defined until maximum width is reached, then increase length (conservation of area at the expense of aspect ratio)
- $\operatorname{Sigma}=0$ for the attenuation relationship implies that the sigma in the relationship is artificially set to zero, not that the sigma is truncated.
- Note that equation for $\ln (\mathrm{y})$ in Table 3.1 of Sadigh et al. (1997) has a typo in the third term. It should read $\mathrm{C} 3 *(8.5-\mathrm{M})^{\wedge} 2.5$ to match equation 2.2.
- Rupture dimension relationships:
$\log (\mathrm{A})=\mathbf{M}-4 \quad \sigma_{\mathrm{A}}=0.25$
$\log (W)=0.5 * \mathbf{M}-2.15 \quad \sigma_{W}=0.15$
$\log (\mathrm{L})=0.5 * \mathbf{M}-1.85 \quad \sigma_{\mathrm{L}}=0.20$
Aspect Ratio $=2$
Note: Sigma for all rupture dimension relationships should be set to zero for all cases except $3 \mathrm{a}-\mathrm{g}$.
- For all faults, the slip rate is $2 \mathrm{~mm} /$ year, b -value $=0.9$
- For the area source, number of events per year of $M_{\min }$ and greater $(\mathbf{M} \geq 5)$ is 0.0395 for the whole area, $b$-value $=0.9$, and $\mathrm{M}_{\max }=61 / 2$.

The following test cases are also summarized in Table 3.1.

Table 3.1 Test cases set 1

| Name | Description | Source | MagnitudeDensity Function ${ }^{1,2}$ | Attenuation Relation | Rupture Dimension Relationships ${ }^{\text {3,4,5,6 }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Set 1 <br> Case 1 | Single rupture of entire fault plane. Tests distance, rate, and attenuation calculations. | Fault 1 (vertical SS) <br> b-value $=0.9$ <br> slip rate $=2 \mathrm{~mm} / \mathrm{yr}$ | Delta <br> Function at M $6.5$ | $\begin{aligned} & \text { Sadigh et } \\ & \text { al.(1997), rock } \\ & \sigma=0 \end{aligned}$ | $\begin{aligned} & \log (\mathrm{A})=\mathrm{M}-4 ; \sigma_{\mathrm{A}}=0 \\ & \log (\mathrm{~W})=0.5 * \mathrm{M}-2.15 ; \\ & \sigma_{\mathrm{W}}=0 \\ & \log (\mathrm{~L})=0.5 * \mathrm{M}-1.85 ; \sigma_{\mathrm{L}} \\ & =0 \end{aligned}$ |
| Set 1 Case 2 | Single rupture smaller than fault plane. <br> Tests uniform slip and edge effects. | Fault 1(vertical SS) <br> b-value $=0.9$ <br> slip rate $=2 \mathrm{~mm} / \mathrm{yr}$ | $\begin{aligned} & \hline \text { Delta } \\ & \text { Function at M } \\ & 6.0 \end{aligned}$ | $\begin{aligned} & \text { Sadigh et } \\ & \text { al.(1997), rock } \\ & \sigma=0 \end{aligned}$ | $\begin{aligned} & \log (\mathrm{A})=\mathrm{M}-4 ; \sigma_{\mathrm{A}}=0 \\ & \log (\mathrm{~W})=0.5 * \mathrm{M}-2.15 ; \\ & \sigma_{\mathrm{W}}=0 \\ & \log (\mathrm{~L})=0.5 * \mathrm{M}-1.85 ; \sigma_{\mathrm{L}} \\ & =0 \end{aligned}$ |
| Set 1 Case 3 | Single rupture smaller than fault plane, including variation of rupture plane dimensions. Tests uniform slip and edge effects, variability of rupture areas. | Fault 1(vertical SS) <br> b-value $=0.9$ <br> slip rate $=2 \mathrm{~mm} / \mathrm{yr}$ | Delta <br> Function at M $6.0$ | $\begin{aligned} & \text { Sadigh et } \\ & \text { al.(1997), rock } \\ & \sigma=0 \end{aligned}$ | $\begin{aligned} & \log (\mathrm{A})=\mathrm{M}-4 ; \sigma_{\mathrm{A}}=0.25 \\ & \log (\mathrm{~W})=0.5 * \mathrm{M}-2.15 ; \\ & \sigma_{\mathrm{W}}=0.15 \\ & \log (\mathrm{~L})=0.5 * \mathrm{M}-1.85 ; \sigma_{\mathrm{L}} \\ & =0.20 \end{aligned}$ |
| Set 1 <br> Case 4 | Single rupture smaller than fault plane on dipping fault. | Fault 2(reverse $60^{\circ}$ ) b-value $=0.9$ slip rate $=2 \mathrm{~mm} / \mathrm{yr}$ | Delta Function at M 6.0 | $\begin{aligned} & \text { Sadigh et } \\ & \text { al.(1997), rock } \\ & \sigma=0 \end{aligned}$ | $\begin{aligned} & \log (\mathrm{A})=\mathrm{M}-4 ; \sigma_{\mathrm{A}}=0 \\ & \log (\mathrm{~W})=0.5 * \mathrm{M}-2.15 ; \\ & \sigma_{\mathrm{W}}=0 \\ & \log (\mathrm{~L})=0.5 * \mathrm{M}-1.85 ; \sigma_{\mathrm{L}} \\ & =0 \end{aligned}$ |
| Set 1 Case 5 | Truncated exponential model. | Fault 1(vertical SS) <br> b-value $=0.9$ <br> slip rate $=2 \mathrm{~mm} / \mathrm{yr}$ | $\begin{aligned} & \begin{array}{l} \text { Truncated } \\ \text { exponential } \\ \text { model, } \mathrm{M}_{\max } \end{array}= \\ & 6.5 \\ & \mathrm{M}_{\min }=5 \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { Sadigh et } \\ & \text { al.(1997), rock } \\ & \sigma=0 \end{aligned}$ | $\begin{aligned} & \log (\mathrm{A})=\mathrm{M}-4 ; \sigma_{\mathrm{A}}=0 \\ & \log (\mathrm{~W})=0.5 * \mathrm{M}-2.15 ; \\ & \sigma_{\mathrm{W}}=0 \\ & \log (\mathrm{~L})=0.5 * \mathrm{M}-1.85 ; \sigma_{\mathrm{L}} \\ & =0 \end{aligned}$ |
| Set 1 <br> Case 6 | Truncated normal model. | Fault 1(vertical SS) <br> b-value $=0.9$ <br> slip rate $=2 \mathrm{~mm} / \mathrm{yr}$ | Truncated normal model, $\mathrm{M}_{\mathrm{char}}=6.2$ <br> $M_{\text {max }}=6.5$, <br> sigma $=.25$ <br> $\mathrm{M}_{\text {min }}=5$ | $\begin{aligned} & \text { Sadigh et } \\ & \text { al.(1997), rock } \\ & \sigma=0 \end{aligned}$ | $\begin{aligned} & \log (\mathrm{A})=\mathrm{M}-4 ; \sigma_{\mathrm{A}}=0 \\ & \log (\mathrm{~W})=0.5 * \mathrm{M}-2.15 ; \\ & \sigma_{\mathrm{W}}=0 \\ & \log (\mathrm{~L})=0.5 * \mathrm{M}-1.85 ; \sigma_{\mathrm{L}} \\ & =0 \end{aligned}$ |
| Set 1 Case 7 | Characteristic model (Youngs \& Coppersmith 1985) | Fault 1(vertical SS) <br> b-value $=0.9$ <br> slip rate $=2 \mathrm{~mm} / \mathrm{yr}$ | $\begin{aligned} & \text { Characteristic } \\ & \text { model, } \mathrm{M}_{\text {char }}= \\ & 6.2, \mathrm{M}_{\max }= \\ & 6.45 \\ & \mathrm{M}_{\min }=5 \end{aligned}$ | $\begin{aligned} & \text { Sadigh et } \\ & \text { al.(1997), rock } \\ & \sigma=0 \end{aligned}$ | $\begin{aligned} & \log (\mathrm{A})=\mathrm{M}-4 ; \sigma_{\mathrm{A}}=0 \\ & \log (\mathrm{~W})=0.5 * \mathrm{M}-2.15 ; \\ & \sigma_{\mathrm{W}}=0 \\ & \log (\mathrm{~L})=0.5 * \mathrm{M}-1.85 ; \sigma_{\mathrm{L}} \\ & =0 \end{aligned}$ |
| Set 1 <br> Case 8a | Single rupture smaller than fault plane. <br> (Repeat of case 2 with gm variability untruncated). | Fault 1(vertical SS) <br> b-value $=0.9$ <br> slip rate $=2 \mathrm{~mm} / \mathrm{yr}$ | Delta Function at M 6.0 | Sadigh et al.(1997), rock Do not truncate sigma | $\begin{aligned} & \log (\mathrm{A})=\mathrm{M}-4 ; \sigma_{\mathrm{A}}=0 \\ & \log (\mathrm{~W})=0.5 * \mathrm{M}-2.15 ; \\ & \sigma_{\mathrm{W}}=0 \\ & \log (\mathrm{~L})=0.5 * \mathrm{M}-1.85 ; \sigma_{\mathrm{L}} \\ & =0 \end{aligned}$ |

Table 3.1—Continued

| Name | Description | Source | $\begin{gathered} \hline \text { Magnitude- } \\ \text { Density } \\ \text { Function }{ }^{1,2} \\ \hline \end{gathered}$ | Attenuation Relation | Rupture Dimension Relationships ${ }^{3,4,5,6}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Set 1 <br> Case 8b | Single rupture smaller than fault plane. <br> (Repeat of case 2 with gm variability truncated at 2 std. dev.). | Fault 1(vertical SS) <br> b-value $=0.9$ slip rate $=2 \mathrm{~mm} / \mathrm{yr}$ | Delta <br> Function at M $6.0$ | Sadigh et al.(1997), rock <br> Truncate sigma at 2 std.dev. | $\begin{aligned} & \log (\mathrm{A})=\mathrm{M}-4 ; \sigma_{\mathrm{A}}=0 \\ & \log (\mathrm{~W})=0.5 * \mathrm{M}-2.15 ; \\ & \sigma_{\mathrm{W}}=0 \\ & \log (\mathrm{~L})=0.5 * \mathrm{M}-1.85 ; \sigma_{\mathrm{L}} \\ & =0 \end{aligned}$ |
| Set 1 <br> Case 8c | Single rupture smaller than fault plane. <br> (Repeat of case 2 with gm variability truncated at 3 std.dev.) | Fault 1(vertical SS) <br> b-value $=0.9$ <br> slip rate $=2 \mathrm{~mm} / \mathrm{yr}$ | $\begin{aligned} & \hline \text { Delta } \\ & \text { Function at M } \\ & 6.0 \end{aligned}$ | Sadigh et al. (1997), rock Truncate sigma at 3 std.dev. | $\begin{aligned} & \log (\mathrm{A})=\mathrm{M}-4 ; \sigma_{\mathrm{A}}=0 \\ & \log (\mathrm{~W})=0.5 * \mathrm{M}-2.15 ; \\ & \sigma_{\mathrm{W}}=0 \\ & \log (\mathrm{~L})=0.5 * \mathrm{M}-1.85 ; \sigma_{\mathrm{L}} \\ & =0 \end{aligned}$ |
| $\begin{aligned} & \hline \text { Set } 1 \\ & \text { Case 9a } \end{aligned}$ | Single rupture smaller than fault plane on dipping fault with gm truncated at 3 std. dev. | $\begin{aligned} & \text { Fault 2(reverse } \\ & \left.60^{\circ}\right) \\ & \text { b-value }=0.9 \\ & \text { slip rate }=2 \mathrm{~mm} / \mathrm{yr} \end{aligned}$ | Delta Function at M 6.0 | Sadigh et al.(1997), rock Truncate sigma at 3 std.dev. | $\begin{aligned} & \log (\mathrm{A})=\mathrm{M}-4 ; \sigma_{\mathrm{A}}=0 \\ & \log (\mathrm{~W})=0.5 * \mathrm{M}-2.15 ; \\ & \sigma_{\mathrm{W}}=0 \\ & \log (\mathrm{~L})=0.5 * \mathrm{M}-1.85 ; \sigma_{\mathrm{L}} \\ & =0 \end{aligned}$ |
| Set 1 <br> Case 9b | Single rupture smaller than fault plane on dipping fault using AS 97 gm, no gm variability. | Fault 2(reverse $60^{\circ}$ ) <br> b-value $=0.9$ <br> slip rate $=2 \mathrm{~mm} / \mathrm{yr}$ | $\begin{aligned} & \text { Delta } \\ & \text { Function at M } \\ & 6.0 \end{aligned}$ | Abrahamson \& Silva (1997), rock $\sigma=0$ | $\begin{aligned} & \log (\mathrm{A})=\mathrm{M}-4 ; \sigma_{\mathrm{A}}=0 \\ & \log (\mathrm{~W})=0.5 * \mathrm{M}-2.15 ; \\ & \sigma_{\mathrm{W}}=0 \\ & \log (\mathrm{~L})=0.5 * \mathrm{M}-1.85 ; \sigma_{\mathrm{L}} \\ & =0 \end{aligned}$ |
| Set 1 <br> Case 9c | Single rupture smaller than fault plane on dipping fault using Campbell 1997 and gm truncated at 3 std. dev. | $\begin{aligned} & \text { Fault 2(reverse } \\ & \left.60^{\circ}\right) \\ & \text { b-value }=0.9 \\ & \text { slip rate }=2 \mathrm{~mm} / \mathrm{yr} \end{aligned}$ | $\begin{aligned} & \hline \text { Delta } \\ & \text { Function at M } \\ & 6.0 \end{aligned}$ | Campbell (1997), <br> soft rock, depth to basement rock $=$ <br> 2 km , depth to <br> seismogenic <br> zone $=3 \mathrm{~km}$ <br> Truncate sigma at <br> 3 std.dev., use <br> amplitude <br> dependent sigma | $\begin{aligned} & \log (\mathrm{A})=\mathrm{M}-4 ; \sigma_{\mathrm{A}}=0 \\ & \log (\mathrm{~W})=0.5 * \mathrm{M}-2.15 ; \\ & \sigma_{\mathrm{W}}=0 \\ & \log (\mathrm{~L})=0.5 * \mathrm{M}-1.85 ; \sigma_{\mathrm{L}} \\ & =0 \end{aligned}$ |
| Set 1 <br> Case 10 | Area Source with fixed depth of 5 km . | $\begin{aligned} & \text { Area 1 } \\ & \mathrm{M}_{\mathrm{w}} \geq=0.0395 \\ & \mathrm{~b} \text {-value }=0.9 \end{aligned}$ | Truncated Exponential $\begin{aligned} & M_{\max }=6.5 \\ & M_{\min }=5 \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { Sadigh et al. } \\ & (1997) \text {, rock } \\ & \sigma=0 \end{aligned}$ | Use 1 km grid spacing of point sources or small faults to simulate uniform distribution. |
| Set 1 <br> Case 11 | Volume Source with depth of 5 km to 10 km. | $\begin{aligned} & \text { Area 1 } \\ & \mathrm{M}_{\mathrm{w}} \geq=0.0395 \\ & \mathrm{~b} \text {-value }=0.9 \end{aligned}$ | Truncated Exponential, $M_{\max }=6.5$ $\mathrm{M}_{\min }=5$ | $\begin{aligned} & \text { Sadigh et } \\ & \text { al.(1997), rock } \\ & \sigma=0 \end{aligned}$ | Use 1 km grid spacing of point sources or small faults to simulate uniform distribution. |
| Set 1 <br> Case 12 | Single rupture of entire fault plane. Adding ground motion variability to Case 1. | Fault 1 (vertical SS) <br> b-value $=0.9$ <br> slip rate $=2 \mathrm{~mm} / \mathrm{yr}$ | Delta <br> Function at M 6.5 | Sadigh et al.(1997), rock <br> Truncate sigma at 3 std.dev | $\begin{aligned} & \log (\mathrm{A})=\mathrm{M}-4 ; \sigma_{\mathrm{A}}=0 \\ & \log (\mathrm{~W})=0.5 * \mathrm{M}-2.15 ; \\ & \sigma_{\mathrm{W}}=0 \\ & \log (\mathrm{~L})=0.5 * \mathrm{M}-1.85 ; \sigma_{\mathrm{L}} \\ & =0 \end{aligned}$ |

[^0]
## Case 1

Purpose: A single rupture of the entire fault plane will test the code calculation of distance, fault activity rate, and attenuation relation without variability.

Single-magnitude event (M6.5) on Fault 1 that ruptures entire fault plane. Use Sadigh et al. $(1997)$, rock, sigma $=0$. Calculate the hazard for the seven sites shown in Figure 3.1.

## Results

Test Case 1 is designed to test the code computation of fault distance, fault activity rate, and median ground motion predicted by the Sadigh et al. (1997), rock, for a given magnitude and distance. With a single-magnitude event (delta function of $\mathbf{M} 6.5$ ) that ruptures the entire fault, the fault activity rate of $2.853 \mathrm{E}-3$ is easily computed using the slip rate ( $2 \mathrm{~mm} / \mathrm{year}$ ) and fault area $\left(300 \mathrm{~km}^{2}\right)$. Due to the lack of variability in the ground motion and in the distance to the rupture plane for each site, the resulting hazard curve is a horizontal line at the fault activity rate extending to the ground motion value predicted for the magnitude and distance. Table 3.2 provides the median ground motion for each site. The results from all codes tested matched the analytical solution (Figs. 3.2-3.8).

Table 3.2 Median PGA values at sites 1-7

| Site | Distance <br> $(\mathbf{k m})$ | PGA for M 6.5 <br> $(\mathbf{g})$ |
| :---: | :---: | :---: |
| 1 | 0 | 0.7717 |
| 2 | 10 | 0.3123 |
| 3 | 50 | 0.0497 |
| 4 | 0 | 0.7717 |
| 5 | 10 | 0.3123 |
| 6 | 0 | 0.7717 |
| 7 | 10 | 0.3123 |

## Case 2

Purpose: A single rupture smaller than the fault plane tests uniform slip and edge effects.
Single-magnitude event (M 6.0) on Fault 1 with one size rupture plane (smaller than total fault plane area) as defined using the rupture area (RA), rupture width (RW), rupture length (RL) and/or aspect ratio relationships given below ( $\sigma_{R A}=\sigma_{R L}=\sigma_{R W}=0$ ). Use Sadigh et al. (1997), rock, sigma $=0$. Calculate the hazard for the seven sites shown in Figure 3.1.

## Results

Test Case 2 is designed to test a code's computation of rupture area, distribution of slip, and distance to rupture. Variability of RA dimensions and ground motion was set to zero to simplify the test case. The initial results from the codes tested showed significant differences. Figure 3.9 shows an early set of results for Site 1 , which is located on the trace of the fault at the midpoint along the strike. Some codes initially provided different results for Sites 4 and 6, which are located at the ends of the fault. An examination of the results and discussion among participants determined that modeling of the rupture on the fault plane, especially near the fault edges, differed among code developers. These differences in approach led to significant differences in hazard for this simple test case. The Working Group decided to adopt a recommended approach for the rupture model: uniform slip which tapers at the fault edges. This can be achieved by uniformly distributing the rupture plane from one edge of the fault to the other end both along the strike and the down-dip width. No ruptures are allowed to extend beyond the edges of the fault. Hazard near the ends is sensitive to the step-size used to move the rupture. With the recommended approach, the codes tested were able to approximate the analytical solution closely. Figures 3.10 to 3.16 show the results for the seven sites.

## Case 3

Purpose: A single rupture smaller than the fault plane with variability in the rupture dimension relationships included tests of the uniform slip and edge effects with variability of the rupture area, the width and the length.

Single-magnitude event (M6.0) on Fault 1 with rupture planes as defined using the RA, RW, RL and/or aspect ratio relationships given below (include sigma in these relationships). Maintain the aspect ratio defined until maximum width is reached, then increase length (conservation of area at the expense of aspect ratio.) Use Sadigh et al. (1997), rock, sigma $=0$. Calculate the hazard for the seven sites shown in Figure 3.1.

## Results

Test Case 3 builds directly on Case 2 . The only change is the inclusion of variability in the rupture dimension relations. The rupture dimension equations were chosen such that the median rupture length and width would not be sensitive to the computation approach. Some of the codes compute RA based on magnitude then maintain a constant aspect ratio. Other codes compute RA and width based on magnitude and back out the rupture length. However, the different approaches to incorporating the variability and computing the rupture dimensions will provide
different hazard results. The variation of hazard results provides an example of the sensitivity to this parameter. Note that the variability in the rupture dimension equations is not always incorporated in standard PSHAs. The results for all sites are shown in Figures 3.17-3.23.

## Case 4

Purpose: This case is a repeat of Case 2 using a dipping fault (Fault 2). It tests the calculation of distance to a dipping fault.

Single-magnitude event (M6.0) on Fault 2 with one size rupture plane (smaller than total fault plane area) as defined using the RA, RW, RL and/or aspect ratio relationships given above $\left(\sigma_{R A}=\sigma_{R L}=\sigma_{R W}=0\right)$. Use Sadigh et al. (1997), rock, sigma $=0$. Calculate the hazard for the seven sites shown in Figure 3.1.

## Results

Test Case 4 is intended to further test the geometric modeling of faults. It is a slight variation of Test Case 2. In this case, a single size rupture smaller than the full fault plane occurs on a buried dipping fault. With variability in ground motion and rupture dimensions set to zero, the hazard is a function only of the fault activity rate (calculated from the magnitude, slip rate and fault area) and distance to the rupture. The solutions computed by hand and Microsoft Excel are compared to the results for Sites 1, 2, and 7. As with Test Case 2, initial results showed large variation due to variation in approaches for distribution of rupture plane on the fault plane, especially near the edges. Figures 3.24 and 3.25 are the initial results for sites on the ends of the fault (Sites 4 and 6, respectively.) After modifications to model slip that tapers at the edges, all results compare well with the hand solutions, with the exception of one code for Site 7, which is on the footwall (Figs. 3.26-3.32). In addition, results from these codes are all tightly grouped. These results indicate that the geometric modeling of dipping faults and movement of ruptures on the fault plane are consistent among the codes.

## Case 5

Purpose: Tests calculation of the truncated exponential model.
Calculate the hazard for all seven sites due to rupture of Fault 1 using the truncated exponential model $\left(\mathrm{M}_{\max } 6.5\right.$ and $\left.\mathrm{M}_{\text {min }} 5.0\right)$ and Sadigh et al. (1997), rock, sigma $=0$. Use the RA, RW, and RL relationships (with $\sigma_{R A}=\sigma_{R L}=\sigma_{R W}=0$ ) to define the dimensions of the rupture planes.

## Results

Test Case 5 is intended to test one magnitude-frequency distribution, specifically the truncated exponential model. This model is used extensively in realistic hazard analyses. The initial results pointed toward a difference in approach for calculating the fault activity rate using the truncated exponential magnitude distribution model. As seen in Figure 3.33, the initial hazard results could be grouped into two sets. The difference is due to whether the integration over magnitude is done from the minimum magnitude or zero. Participants were then asked to modify their codes to integrate from zero. The results for all sites are shown in Figures 3.34-3.40. The solutions were computed by hand with the assistance of Microsoft Excel for Sites 4, 5, and 6, for which the geometries provide simple distance to rupture distributions. Hazard results from all codes compare well with the hand solutions, and are tightly grouped for the sites without hand solutions.

## Case 6

Purpose: Tests the truncated normal model.
Calculate the hazard for all 7 sites due to the rupture of Fault 1 using the truncated normal model ( $\mathrm{M}_{\text {char }} 6.2, \mathrm{M}_{\max } 6.5$, sigma 0.25 and $\mathrm{M}_{\min } 5.0$ ) and Sadigh et al. (1997), rock, sigma 0 . Use the RA, RW, and RL relationships (with $\sigma_{R A}=\sigma_{R L}=\sigma_{R W}=0$ ) to define the dimensions of the rupture planes.

## Results

Test Case 6 is intended to test the truncated normal magnitude distribution model. Figures 3.41 to 3.47 show the results for all sites. As with Test Case 5, the results from all codes compare well with the hand solutions, and are tightly grouped for the sites without hand solutions.

## Case 7

Purpose: Tests the characteristic model.
Calculate the hazard for all 7 sites due to the rupture of Fault 1 using the characteristic model (Youngs and Coppersmith [1985] $\mathrm{M}_{\text {char }} 6.2, \mathrm{M}_{\max } 6.45$, and $\mathrm{M}_{\min } 5.0$ ) and Sadigh et al. (1997), rock, sigma 0 . Use the RA, RW, and RL relationships (with $\sigma_{R A}=\sigma_{R L}=\sigma_{R W}=0$ ) to define the dimensions of rupture planes.

## Results

Test Case 7 is intended to test the characteristic magnitude frequency distribution, which is used extensively in modern PSHAs. Similar to Test Case 5, which tests the exponential model, early results showed differences in calculating the fault activity rate. The initial results for Site 6 are shown in Figure 3.48. Note the spread in hazard at very low ground motions. The final results show consistency between all codes (Figs. 3.49-3.55).

## Case 8

Purpose: This is a repeat of Case 2 with ground motion variability included as defined by the attenuation relationship. The case is run with ground motion variability untruncated, truncated at 2 standard deviations, and truncated at 3 standard deviations.

Calculate the hazard for all seven sites due to a single-magnitude event (M6.0) on Fault 1 using Sadigh et al. (1997), rock, sigma untruncated, and truncated at two and three standard deviations. Use the RA, RW, and RL relationships (with $\sigma_{R A}=\sigma_{R L}=\sigma_{R W}=0$ ) to define the dimensions of the rupture planes.

## Results

Test Case 8 is an extension of Case 2 in order to test the addition of aleatory variability in the ground motion prediction equation. The case was analyzed using untruncated variability and variability truncated at two and three standard deviations. The hazard results from all codes are tightly grouped. Figures 3.56 to 3.62 show the results for untruncated ground motion variability. The hazard results for cases with ground motion variability truncated at two and three standard deviations are shown in Figures 3.63-3.69 and Figures 3.70-3.76, respectively.

## Case 9

Purpose: A single rupture smaller than the fault plane on a dipping fault testing three common attenuation relationships.

Calculate the hazard for all seven sites due to a single-magnitude event (M6.0) on Fault 2 using the following three attenuation relationships
(9a) Sadigh et al. (1997), rock, sigma truncated at 3 standard deviations
(9b) Abrahamson and Silva (1997), rock, sigma $=0$
(9c) Campbell (1997), soft rock, depth to basement rock $=2 \mathrm{~km}$, depth to seismogenic zone $=3 \mathrm{~km}$, sigma truncated at 3 standard deviations

Compute the results for the attenuation relationships individually. Use the RA, RW, and RL relationships (with $\sigma_{R A}=\sigma_{R L}=\sigma_{R W}=0$ ) to define the dimensions of the rupture planes.

Note for Abrahamson and Silva (1997), include the style of faulting factor ( $\mathrm{F}=1 \mathrm{for}$ reverse fault) and the hanging wall factor. As defined, the hanging wall factor applies to only Site 2. HW = 1 for Sites 1, 2, 3, 4, and 6. However, fHW (Rrup) $=0$ for Sites 1, 4, and 6 (Rrup $<$ 4) as well as Site 3 (Rrup $>25$ ). HW $=0$ for Site 5 (off edge) and Site 7 (on footwall).

Also note that the Abrahamson and Silva (1997) formula for f3(M), Eq. 6, p. 106 contains an error. For $\mathbf{M}$ between 5.8 and c 1 , the fraction $\left[\left(\mathrm{a}_{6}-\mathrm{a}_{5}\right) /\left(\mathrm{c}_{1}-5.8\right)\right]$ should be multiplied by (M5.8).

## Results

Test Case 9a is an extension of Test Case 4. The variability in the ground motion attenuation relation is included and truncated at three sigma. The hazard results are shown in Figures 3.773.83. Hand solutions were not computed; however, there is consistency in the results from all codes.

Test Case 9b uses an attenuation relation that includes hanging wall effects. The variability in the ground motion is not included so as to allow for easier hand solution. The solutions are provided for Sites 1, 2, and 7. The hazard results for all sites are shown in Figures 3.84-3.90. For sites on the ends of the surface projection of the fault, Sites 4 and 6, there is one outlier (Figs. 3.87 and 3.89). The results from Site 1 also show some variation among codes, the source of which has not been determined.

Test Case 9c tests the implementation of the Campbell (1997) attenuation relation for soft rock. The results are presented in Figures 3.91-3.97. The hazard results are clustered into two groups. This is due to the use of different estimates of variability in the ground motion attenuation relation. Campbell (1997) provides two estimates of variability, one as a function of magnitude and one as a function of amplitude, or PGA. To confirm, Haz38 was run for Sites 2, 3 , and 5 using both relations (Figs. 3.92, 3.93, and 3.95, respectively).

## Case 10

Purpose: Area source with fixed depth of 5 km
Calculate the hazard at four sites for the area source defined in Figure 3.1. Use the truncated exponential model with $\mathrm{M}_{\max }=6.5$ and $\mathrm{M}_{\min }=5.0$. Source should be uniformly
distributed point sources (or approximations to point source) across the area ( 1 km grid spacing) at a fixed depth of 5 km . The attenuation relationship is Sadigh et al. (1997), rock, sigma $=0$.

## Results

Test Case 10 tests the computation of hazard from an area source. The case was defined as having uniformly distributed point sources throughout the area at a fixed depth. However, some of the codes tested do not implement point sources. These codes used an area source defined with uniformly distributed small faults that were set to be 1 square km in size. Even with these differences, results from all codes are consistent, as shown in Figures 3.98-3.101.

## Case 11

Purpose: Volume source with fixed depth of 5-10 km
Calculate the hazard at four sites for area source defined in Figure 3.1. Use the truncated exponential model with $\mathrm{M}_{\max }=6.5$ and $\mathrm{M}_{\min }=5.0$. The source should be uniformly distributed point sources (or approximation to point sources) throughout the volume ( 1 km grid spacing) defined by the area and a depth range of 5-10 km. The attenuation relationship is Sadigh et al. (1997), rock, sigma $=0$.

## Results

Test Case 11 extends the area source to a volume with point sources distributed over a depth range. The hazard results are shown in Figures 3.102-3.105. As with Test Case 10, the results from all codes are consistent with each other.

### 3.2 TEST CASE SET 2

The following describes the second set of test cases. Mean hazard results (probability of exceedance) for PGA defined at $0.001,0.01,0.05,0.1,0.2,0.3,0.4,0.5,0.75,1.0,1.25$, and 1.5 g were calculated. A Poisson model was assumed when converting rates to probabilities.

The second set of test cases is designed to test more complicated source geometry, multiple sources, and the implementation of logic trees. The participants provided the hazard results. However, due to schedule constraints, the results were not revised after all code issues related to Test Case 1 were resolved. The consensus results are not provided for Test Case 2.

## For All Cases:

Use $\mathrm{M}_{\text {min }}=5.0$ with an integration step size small enough to adequately model the

- Magnitude density function
- Fault rupture dimension relationships:

$$
\begin{array}{ll}
\log (\mathrm{A})=\mathrm{M}-4 & \sigma_{\mathrm{A}}=0 \\
\log (\mathrm{~W})=0.5 * \mathrm{M}-2.15 & \sigma_{\mathrm{W}}=0 \\
\log (\mathrm{~L})=0.5 * \mathrm{M}-1.85 & \sigma_{\mathrm{L}}=0 \\
\text { Aspect Ratio }=2 &
\end{array}
$$

## Case 1a-f (Non-Planar Fault)

Calculate the hazard at the three sites shown in Figure 3.106 due to the rupture of Fault A (unsegmented rupture only) using the truncated exponential model $\left(\mathrm{M}_{\max }=7.0\right)$, slip rate $=2$ $\mathrm{mm} / \mathrm{yr}$, b-value $=0.9$, and the Sadigh et al. (1997) attenuation relationship, rock, sigma $=0$. Use the RA, RW, and RL relationships given below (with $\sigma_{R A}=\sigma_{R L}=\sigma_{R W}=0$ ) to define the dimensions of the rupture planes. For cases $1 \mathrm{a}, 1 \mathrm{~b}$, and 1 c use a dip of 60 degrees to the east. For cases $1 \mathrm{~d}, 1 \mathrm{e}$, and 1 f use a dip of 60 degrees to the west.

The initial results for Site 1 are provided in Figure 3.107. This test case is designed to test how the geometry of non-straight-line faults are handled across available codes. Most codes to date model faults with planes. For a fault that bends along strike and dips other than 90 degrees, this creates gaps or overlaps of the planes at the bend along strike. Modeling approaches to address these gaps or overlaps range from ignoring the gap and combining planes at the intersection, to using the average strike to project the fault bottom points and connect (which changes the dip), to using conical surfaces to fill the gaps. This issue becomes more important when hanging wall factors are considered. Determination of whether a site is on the hanging wall or not may be sensitive to gaps. In addition, the Rx parameter in the Next Generation of Attenuation (NGA) ground motion relations can be sensitive to the correct geometric modeling of the fault.

## Cases 2a-c (Multiple Sources, Deaggregation)

Calculate the hazard at the three sites shown in Figure 3.108 due to the area source, Fault B, and Fault C. For the area source, use the truncated exponential model $\left(\mathrm{M}_{\max }=6.5\right)$ and the cumulative number of events with $\mathbf{M} \geq 5.0=0.0395$. For Fault $B$ ( $\mathrm{L}=75 \mathrm{~km}$ ), use the characteristic model
(Youngs and Coppersmith [1985], $\mathrm{M}_{\text {char }}=7.0, \mathrm{M}_{\max }=7.25$ ), and slip rate $=2 \mathrm{~mm} / \mathrm{yr}$. For Fault $\mathrm{C}(\mathrm{L}=25 \mathrm{~km})$, use the characteristic model (Youngs and Coppersmith [1985], $\mathrm{M}_{\mathrm{char}}=6.5, \mathrm{M}_{\max }=$ 6.75), and slip rate $=1 \mathrm{~mm} / \mathrm{yr}$. For all sources, use the Sadigh et al. (1997) attenuation relationship, rock, sigma truncated at 3 standard deviations, $b$-value $=0.9, \mathrm{a}_{\min }=5.0$. For the faults, use the RA, RW, and RL relationships given below (with $\sigma_{R A}=\sigma_{R L}=\sigma_{R W}=0$ ) to define the dimensions of the rupture planes.

Provide the following deaggregation results for peak ground acceleration at Sites 1 and 3 corresponding to the annual exceedance probabilities of 0.01 and 0.0001 :

$$
\begin{aligned}
& \text { Modal values } \mathrm{M}^{*}, \mathrm{D}^{*}, \varepsilon^{*} \\
& \text { Mean values } \mathrm{M} \text {-bar, } \mathrm{D} \text {-bar, } \varepsilon \text {-bar }
\end{aligned}
$$

Test Case 2 was designed to look at multiple sources and deaggregation. An example of early hazard results is shown in Figure 3.109. With perhaps two outliers, the results are fairly closely grouped.

## Cases 3a-c (Recurrence Interval, Characteristic Model)

Calculate the hazard for all three sites due to the rupture of Fault D (Fig. 3.110) using the characteristic model (Youngs and Coppersmith [1985], $\mathrm{M}_{\text {char }}=6.2, \mathrm{M}_{\max }=6.45$ ), recurrence interval $=1000$ years, and the Sadigh et al. (1997) attenuation relationship, rock, sigma $=0$. Use the RA, RW, and RL relationships (with $\sigma_{R A}=\sigma_{R L}=\sigma_{R W}=0$ ) to define the dimensions of the rupture planes.

Test Case 3 is an extension of Test Case 7 from Set 1. It is intended to test the use of the recurrence interval using the characteristic model of earthquake magnitude distribution. Early results are shown in Figure 3.111 for Site 1.

## Cases 4a-c (Recurrence Interval, Truncated Normal Model)

Calculate the hazard for all three sites due to the rupture of Fault D (Fig. 3.110) using the truncated normal model $\left(\mathrm{M}_{\text {char }}=6.2, \mathrm{M}_{\max }=6.5\right.$, sigma $\left.=0.25\right)$, recurrence interval $=1000$ years, and the Sadigh et al. (1997) attenuation relationship, rock, sigma $=0$. Use the RA, RW, and RL relationships (with $\sigma_{R A}=\sigma_{R L}=\sigma_{R W}=0$ ) to define the dimensions of the rupture planes.

Test Case 4 is intended to test the use of the recurrence interval with the truncated normal distribution of earthquake magnitude. Early results are shown in Figure 3.112 for Site 1.

## Cases 5a-c (Logic Tree, Fractiles)

Calculate the hazard for all three sites due to the rupture of Fault A (Fig. 3.106) as shown in the logic tree in Figure 3.113. Provide the mean hazard along with the $5^{\text {th }}$ and $95^{\text {th }}$ percentile fractiles. Use the Sadigh et al. (1997) attenuation relationship, rock, truncate sigma at three standard deviations. Use the RA, RW, and RL relationships (with $\sigma_{R A}=\sigma_{R L}=\sigma_{R W}=0$ ) to define dimensions of rupture planes.

The initial results for Test Case 5 for Site 1 is shown in Figure 3.114. Due to a lack of discussion and revision, it is unknown if the wide range of results is a result of different interpretation of the logic tree or input errors.

## Cases 6a-c (Listric Fault)

Calculate the hazard for all three sites due to the rupture of Fault E (Fig. 3.115) using the truncated exponential model $\left(\mathrm{M}_{\max }=6.5\right)$ and the Sadigh et al. (1997) attenuation relationship, rock, sigma $=0$. Assume that the fault is strike-slip for the attenuation relationship. Slip-rate $=2$ $\mathrm{mm} / \mathrm{yr}$. Use the RA, RW, and RL relationships (with $\sigma_{R A}=\sigma_{R L}=\sigma_{R W}=0$ ) to define the dimensions of the rupture planes.

Test Case 6 is intended to examine the various modeling approaches for a listric fault and its effect on hazard. The initial results are shown in Figure 3.116. Differences in rate could be a result of different fault areas due to the different fault geometries, but also could be due to the integration issues discovered in Test Case 1.

## Cases 7a-c (Intraslab Zone)

Calculate the hazard for all three sites due to rupture of the intraslab zone with uniform thickness of 10 km (Fig. 3.117) using the truncated exponential model $\left(\mathrm{M}_{\max }=7.5\right)$ and the Youngs et al. (1997) attenuation relationship, with sigma truncated at three standard deviations. The $b$-value is 0.9 . The rate for events greater and equal to 5 is 0.005644 .

Test Case 7 is intended to test the modeling of an intraslab zone. The slab was defined as a dipping volume. The modeling approaches for this varied among codes. Most used a series of horizontal volumes that stairstep down from the shallow end to the deeper end of the slab. Figure 3.118 shows the initial results for Site 1 .

## 4 Conclusions

This report describes a project to test and verify the numerical approaches and software used in PSHA. A Working Group was organized and each member tested their own computer code in two sets of tests. Through several iterations, codes were tested and acceptable answers were established either through analytical solutions or as the consensus answer from the test case results. Given the significant experience of the Working Group members, it was somewhat surprising to find major differences in the initial code verification results. However, more often than not, the differences were due to the differences in the numerical approaches used to solve a particular mathematical problem. Once an agreed-upon solution was adopted and the source characterization clearly defined, the results generally converged.

The verification tests are available to any PSHA code developer/user worldwide through this publication and the PEER website. The test cases will be used as a standard verification for all PSHA codes to be used in projects for the PEER Lifelines Program sponsors, which include the California Department of Transportation (Caltrans), the Pacific Gas \& Electric Company (PG\&E), and the California Energy Commission (CEC).

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Appendix A

## SITE AND SOURCE COORDINATES

| Sites for Test Set 1, Cases 1 through 9 |  |  |  |
| :--- | :---: | :---: | :--- |
| Site | Latitude | Longitude | Comment |
| 1 | 38.113 | -122.000 | On Fault Midpoint along Strike |
| 2 | 38.113 | -122.114 | 10 km West of fault, at midpoint |
| 3 | 38.111 | -122.570 | 50 km West of fault, at midpoint |
| 4 | 38.000 | -122.000 | South end of fault |
| 5 | 37.910 | -122.000 | 10 km south of fault along strike |
| 6 | 38.225 | -122.000 | North end of fault |
| 7 | 38.113 | -121.886 | 10 km East of fault, at midpoint |

Coordinates for 25 km fault for Test Set 1, Cases 1 through 9

| Latitude | Longitude | Comment |
| :---: | :---: | :--- |
| 38.00000 | -122.000 | South end of fault |
| 38.22480 | -122.000 | North end of fault |

Sites for Test Set 1, Cases 10 and 11

| Site | Latitude | Longitude | Comment |
| :--- | :---: | :---: | :--- |
| 1 | 38.000 | -122.000 | Center of Area 1 |
| 2 | 37.550 | -122.000 | 50 km N of Site 1 |
| 3 | 37.099 | -122.000 | On Area Boundary |
| 4 | 36.874 | -122.000 | 25 km N of Area Boundary |

Coordinates for Area Source for Test Set 1, Cases 10 and 11

| Latitude | Longitude |
| :---: | :---: |
| 38.901 | -122.000 |
| 38.899 | -121.920 |
| 38.892 | -121.840 |
| 38.881 | -121.760 |
| 38.866 | -121.682 |
| 38.846 | -121.606 |
| 38.822 | -121.532 |
| 38.794 | -121.460 |
| 38.762 | -121.390 |
| 38.727 | -121.324 |
| 38.688 | -121.261 |
| 38.645 | -121.202 |
| 38.600 | -121.147 |
| 38.551 | -121.096 |
| 38.500 | -121.050 |
| 38.446 | -121.008 |
| 38.390 | -120.971 |
| 38.333 | -120.940 |
| 38.273 | -120.913 |
| 38.213 | -120.892 |
| 38.151 | -120.876 |
| 38.089 | -120.866 |
| 38.026 | -120.862 |
| 37.963 | -120.863 |
| 37.900 | -120.869 |
| 37.838 | -120.881 |
| 37.777 | -120.899 |
| 37.717 | -120.921 |
| 37.658 | -120.949 |
|  |  |

A-3

| Latitude | Longitude |
| :---: | :---: |
| 37.601 | -120.982 |
| 37.545 | -121.020 |
| 37.492 | -121.063 |
| 37.442 | -121.110 |
| 37.394 | -121.161 |
| 37.349 | -121.216 |
| 37.308 | -121.275 |
| 37.269 | -121.337 |
| 37.234 | -121.403 |
| 37.203 | -121.471 |
| 37.176 | -121.542 |
| 37.153 | -121.615 |
| 37.133 | -121.690 |
| 37.118 | -121.766 |
| 37.108 | -121.843 |
| 37.101 | -121.922 |
| 37.099 | -122.000 |
| 37.101 | -122.078 |
| 37.108 | -122.157 |
| 37.118 | -122.234 |
| 37.133 | -122.310 |
| 37.153 | -122.385 |
| 37.176 | -122.458 |
| 37.203 | -122.529 |
| 37.234 | -122.597 |
| 37.269 | -122.663 |
| 37.308 | -122.725 |
| 37.349 | -122.784 |
| 37.394 | -122.839 |
| 37.442 | -122.890 |
| 37.492 | -122.937 |
| 37.545 | -122.980 |
| 37.601 | -123.018 |
| 37.658 | -123.051 |
| 37.717 | -123.079 |
| 37.777 | -123.101 |
| 37.838 | -123.119 |
| 37.900 | -123.131 |
| 37.963 | -123.137 |
| 38.026 | -123.138 |
| 38.089 | -123.134 |
| 38.151 | -123.124 |
| 38.213 | -123.108 |
| 38.273 | -123.087 |
| 38.333 | -123.060 |
| 38.390 | -123.029 |
| 38.446 | -122.992 |
| 38.500 | -122.950 |
| 38.551 | -122.904 |
| 38.600 | -122.853 |
| 38.645 | -122.798 |
| 38.688 | -122.739 |
| 38.727 | -122.676 |
| 38.762 | -122.610 |

A-4

| Latitude | Longitude |
| :---: | :---: |
| 38.794 | -122.540 |
| 38.822 | -122.468 |
| 38.846 | -122.394 |
| 38.866 | -122.318 |
| 38.881 | -122.240 |
| 38.892 | -122.160 |
| 38.899 | -122.080 |

Sites for Test Set 2

| Test Case | Site | Latitude | Longitude |
| :---: | :---: | :---: | :---: |
| 1 | $\mathbf{1}$ | 38.1126 | -121.886 |
| 1 | $\mathbf{2}$ | 38.1800 | -121.886 |
| 1 | $\mathbf{3}$ | 38.2696 | -122.114 |
| 2 | $\mathbf{1}$ | 37.5495 | -122.000 |
| 2 | $\mathbf{2}$ | 37.0990 | -122.000 |
| 2 | $\mathbf{3}$ | 36.8737 | -122.000 |
| $3-7$ | $\mathbf{1}$ | 38.1126 | -121.886 |
| $3-7$ | $\mathbf{2}$ | 38.2252 | -122.000 |
| $3-7$ | $\mathbf{3}$ | 38.0000 | -122.000 |

Fault Coordinates for Test Set 2

| Test Case | Fault | Latitude | Longitude |
| :--- | :--- | :---: | :---: |
| 1,5 | Fault A - Unsegmented | 38.6147 | -121.7130 |
| 1,5 | Fault A - Unsegmented | 38.4200 | -121.8569 |
| 1,5 | Fault A - Unsegmented | 38.2248 | -122.0000 |
| 1,5 | Fault A - Unsegmented | 38.0000 | -122.0000 |
| 1,5 | Fault A - Unsegmented | 37.8049 | -121.8581 |
| 1,5 | Fault A - Unsegmented | 37.6095 | -121.7169 |
| 1,5 | Fault A - Segment A | 38.6147 | -121.7130 |
| 1,5 | Fault A - Segment A | 38.4200 | -121.8569 |
| 1,5 | Fault A - Segment B | 38.4200 | -121.8569 |
| 1,5 | Fault A - Segment B | 38.2248 | -122.0000 |
| 1,5 | Fault A - Segment C | 38.2248 | -122.0000 |
| 1,5 | Fault A - Segment C | 38.0000 | -122.0000 |
| 1,5 | Fault A - Segment D | 38.0000 | -122.0000 |
| 1,5 | Fault A - Segment D | 37.8049 | -121.8581 |
| 1,5 | Fault A - Segment E | 37.8049 | -121.8581 |
| 1,5 | Fault A - Segment E | 37.6095 | -121.7169 |
| 2 | Fault B | 38.6749 | -121.5691 |
| 2 | Fault B | 38.6749 | -122.4309 |
| 2 | Fault C | 37.3242 | -121.8590 |
| 2 | Fault C | 37.3242 | -122.1410 |
| 3,4 | Fault D | 38.2248 | -122.0000 |
| 3,4 | Fault D | 38.0000 | -122.0000 |
| 6 | Fault E | 38.2248 | -122.0000 |
| 6 | Fault E | 38.0000 | -122.0000 |
| 7 | Intraslab | 38.4496 | -122.0000 |
| 7 | Intraslab | 37.7752 | -122.0000 |

Area Source Coordinates for Test Set 2, Case 2

| Latitude | Longitude |
| :---: | :---: |
| 38.901 | -122.000 |
| 38.899 | -121.920 |
| 38.892 | -121.840 |
| 38.881 | -121.760 |
| 38.866 | -121.682 |
| 38.846 | -121.606 |
| 38.822 | -121.532 |
| 38.794 | -121.460 |
| 38.762 | -121.390 |
| 38.727 | -121.324 |
| 38.688 | -121.261 |
| 38.645 | -121.202 |
| 38.600 | -121.147 |
| 38.551 | -121.096 |
| 38.500 | -121.050 |
| 38.446 | -121.008 |
| 38.390 | -120.971 |
| 38.333 | -120.940 |
| 38.273 | -120.913 |
| 38.213 | -120.892 |
| 38.151 | -120.876 |
| 38.089 | -120.866 |
| 38.026 | -120.862 |
| 37.963 | -120.863 |
| 37.900 | -120.869 |
| 37.838 | -120.881 |
| 37.777 | -120.899 |
| 37.717 | -120.921 |
| 37.658 | -120.949 |
| 37.601 | -120.982 |
| 37.545 | -121.020 |
| 37.492 | -121.063 |
| 37.442 | -121.110 |
| 37.394 | -121.161 |
| 37.349 | -121.216 |
| 37.308 | -121.275 |
| 37.269 | -121.337 |
| 37.234 | -121.403 |
| 37.203 | -121.471 |
| 37.176 | -121.542 |
| 37.153 | -121.615 |
| 37.133 | -121.690 |
| 37.118 | -121.766 |
| 37.108 | -121.843 |
| 37.101 | -121.922 |
| 37.099 | -122.000 |
| 37.101 | -122.078 |
| 37.108 | -122.157 |
| 37.118 | -122.234 |
| 37.133 | -122.310 |
| 37.153 | -122.385 |
| 37.176 | -122.458 |
| 37.203 | -122.529 |


| Latitude | Longitude |
| :---: | :---: |
| 37.234 | -122.597 |
| 37.269 | -122.663 |
| 37.308 | -122.725 |
| 37.349 | -122.784 |
| 37.394 | -122.839 |
| 37.442 | -122.890 |
| 37.492 | -122.937 |
| 37.545 | -122.980 |
| 37.601 | -123.018 |
| 37.658 | -123.051 |
| 37.717 | -123.079 |
| 37.777 | -123.101 |
| 37.838 | -123.119 |
| 37.900 | -123.131 |
| 37.963 | -123.137 |
| 38.026 | -123.138 |
| 38.089 | -123.134 |
| 38.151 | -123.124 |
| 38.213 | -123.108 |
| 38.273 | -123.087 |
| 38.333 | -123.060 |
| 38.390 | -123.029 |
| 38.446 | -122.992 |
| 38.500 | -122.950 |
| 38.551 | -122.904 |
| 38.600 | -122.853 |
| 38.645 | -122.798 |
| 38.688 | -122.739 |
| 38.727 | -122.676 |
| 38.762 | -122.610 |
| 38.794 | -122.540 |
| 38.822 | -122.468 |
| 38.846 | -122.394 |
| 38.866 | -122.318 |
| 38.881 | -122.240 |
| 38.892 | -122.160 |

A-7

## SOLUTIONS TO SET 1, TEST CASES 2, 4, 5, 6, 7 AND 9b

Hand Solutions for Set 1, Test Case 2

| Peak Ground <br> Acceleration <br> $\mathbf{( g )}$ | Annual Exceedance Probability |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Site 1 | Site 2 | Site 3 | Site 4 | Site 5 | Site 6 | Site 7 |  |
| 0.001 | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ |  |
| 0.01 | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ |  |
| 0.05 | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ | $0.00 \mathrm{E}+00$ | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ |  |
| 0.1 | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ | $0.00 \mathrm{E}+00$ | $1.59 \mathrm{E}-02$ | $1.56 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ |  |
| 0.15 | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ | $0.00 \mathrm{E}+00$ | $1.59 \mathrm{E}-02$ | $7.69 \mathrm{E}-03$ | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ |  |
| 0.2 | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ | $0.00 \mathrm{E}+00$ | $1.58 \mathrm{E}-02$ | $1.60 \mathrm{E}-03$ | $1.58 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ |  |
| 0.25 | $1.59 \mathrm{E}-02$ | $0.00 \mathrm{E}+00$ | $0.00 \mathrm{E}+00$ | $1.20 \mathrm{E}-02$ | $0.00 \mathrm{E}+00$ | $1.20 \mathrm{E}-02$ | $0.00 \mathrm{E}+00$ |  |
| 0.3 | $1.59 \mathrm{E}-02$ | $0.00 \mathrm{E}+00$ | $0.00 \mathrm{E}+00$ | $8.64 \mathrm{E}-03$ | $0.00 \mathrm{E}+00$ | $8.64 \mathrm{E}-03$ | $0.00 \mathrm{E}+00$ |  |
| 0.35063 | $1.59 \mathrm{E}-02$ | $0.00 \mathrm{E}+00$ | $0.00 \mathrm{E}+00$ | $5.68 \mathrm{E}-03$ | $0.00 \mathrm{E}+00$ | $5.68 \mathrm{E}-03$ | $0.00 \mathrm{E}+00$ |  |
| 0.4 | $1.18 \mathrm{E}-02$ | $0.00 \mathrm{E}+00$ | $0.00 \mathrm{E}+00$ | $3.09 \mathrm{E}-03$ | $0.00 \mathrm{E}+00$ | $3.09 \mathrm{E}-03$ | $0.00 \mathrm{E}+00$ |  |
| 0.45 | $8.23 \mathrm{E}-03$ | $0.00 \mathrm{E}+00$ | $0.00 \mathrm{E}+00$ | $1.51 \mathrm{E}-03$ | $0.00 \mathrm{E}+00$ | $1.51 \mathrm{E}-03$ | $0.00 \mathrm{E}+00$ |  |
| 0.5 | $5.23 \mathrm{E}-03$ | $0.00 \mathrm{E}+00$ | $0.00 \mathrm{E}+00$ | $6.08 \mathrm{E}-04$ | $0.00 \mathrm{E}+00$ | $6.08 \mathrm{E}-04$ | $0.00 \mathrm{E}+00$ |  |
| 0.55 | $2.64 \mathrm{E}-03$ | $0.00 \mathrm{E}+00$ | $0.00 \mathrm{E}+00$ | $1.54 \mathrm{E}-04$ | $0.00 \mathrm{E}+00$ | $1.54 \mathrm{E}-04$ | $0.00 \mathrm{E}+00$ |  |
| 0.6 | $3.63 \mathrm{E}-04$ | $0.00 \mathrm{E}+00$ | $0.00 \mathrm{E}+00$ | $2.92 \mathrm{E}-06$ | $0.00 \mathrm{E}+00$ | $2.92 \mathrm{E}-06$ | $0.00 \mathrm{E}+00$ |  |
| 0.65 | $0.00 \mathrm{E}+00$ | $0.00 \mathrm{E}+00$ | $0.00 \mathrm{E}+00$ | $0.00 \mathrm{E}+00$ | $0.00 \mathrm{E}+00$ | $0.00 \mathrm{E}+00$ | $0.00 \mathrm{E}+00$ |  |

Hand Solutions for Set 1, Test Case 4

| Peak Ground <br> Acceleration (g) | Site 1 | Site 2 | Site 7 |
| :---: | :---: | :---: | :---: |
| 0.001 | $1.68 \mathrm{E}-02$ | $1.68 \mathrm{E}-02$ | $1.68 \mathrm{E}-02$ |
| 0.01 | $1.68 \mathrm{E}-02$ | $1.68 \mathrm{E}-02$ | $1.68 \mathrm{E}-02$ |
| 0.05 | $1.68 \mathrm{E}-02$ | $1.68 \mathrm{E}-02$ | $1.68 \mathrm{E}-02$ |
| 0.10 | $1.68 \mathrm{E}-02$ | $1.68 \mathrm{E}-02$ | $1.68 \mathrm{E}-02$ |
| 0.15 | $1.68 \mathrm{E}-02$ | $1.68 \mathrm{E}-02$ | $1.68 \mathrm{E}-02$ |
| 0.20 | $1.68 \mathrm{E}-02$ | $1.68 \mathrm{E}-02$ | $1.64 \mathrm{E}-02$ |
| 0.25 | $1.68 \mathrm{E}-02$ | $1.68 \mathrm{E}-02$ | $4.17 \mathrm{E}-03$ |
| 0.30 | $1.68 \mathrm{E}-02$ | $0.00 \mathrm{E}+00$ | $0.00 \mathrm{E}+00$ |
| 0.35 | $1.68 \mathrm{E}-02$ | $0.00 \mathrm{E}+00$ | $0.00 \mathrm{E}+00$ |
| 0.40 | $1.37 \mathrm{E}-02$ | $0.00 \mathrm{E}+00$ | $0.00 \mathrm{E}+00$ |
| 0.45 | $1.01 \mathrm{E}-02$ | $0.00 \mathrm{E}+00$ | $0.00 \mathrm{E}+00$ |
| 0.50 | $7.03 \mathrm{E}-03$ | $0.00 \mathrm{E}+00$ | $0.00 \mathrm{E}+00$ |
| 0.55 | $4.37 \mathrm{E}-03$ | $0.00 \mathrm{E}+00$ | $0.00 \mathrm{E}+00$ |
| 0.60 | $2.00 \mathrm{E}-03$ | $0.00 \mathrm{E}+00$ | $0.00 \mathrm{E}+00$ |
| 0.65 | $0.00 \mathrm{E}+00$ | $0.00 \mathrm{E}+00$ | $0.00 \mathrm{E}+00$ |

Hand Solutions for Set 1, Test Case 5

| Peak Ground <br> Acceleration (g) | Site 4 | Site 5 | Site 6 |
| :---: | :---: | :---: | :---: |
| 0.001 | $3.99 \mathrm{E}-02$ | $3.99 \mathrm{E}-02$ | $3.99 \mathrm{E}-02$ |
| 0.01 | $3.99 \mathrm{E}-02$ | $3.99 \mathrm{E}-02$ | $3.99 \mathrm{E}-02$ |
| 0.05 | $3.98 \mathrm{E}-02$ | $3.14 \mathrm{E}-02$ | $3.98 \mathrm{E}-02$ |
| 0.1 | $2.99 \mathrm{E}-02$ | $1.21 \mathrm{E}-02$ | $2.99 \mathrm{E}-02$ |
| 0.15 | $2.00 \mathrm{E}-02$ | $4.41 \mathrm{E}-03$ | $2.00 \mathrm{E}-02$ |
| 0.2 | $1.30 \mathrm{E}-02$ | $1.89 \mathrm{E}-03$ | $1.30 \mathrm{E}-02$ |
| 0.25 | $8.58 \mathrm{E}-03$ | $7.53 \mathrm{E}-04$ | $8.58 \mathrm{E}-03$ |
| 0.3 | $5.72 \mathrm{E}-03$ | $1.25 \mathrm{E}-04$ | $5.72 \mathrm{E}-03$ |
| 0.35 | $3.88 \mathrm{E}-03$ | $0.00 \mathrm{E}+00$ | $3.88 \mathrm{E}-03$ |
| 0.4 | $2.69 \mathrm{E}-03$ | $0.00 \mathrm{E}+00$ | $2.69 \mathrm{E}-03$ |
| 0.45 | $1.91 \mathrm{E}-03$ | $0.00 \mathrm{E}+00$ | $1.91 \mathrm{E}-03$ |
| 0.5 | $1.37 \mathrm{E}-03$ | $0.00 \mathrm{E}+00$ | $1.37 \mathrm{E}-03$ |
| 0.55 | $9.74 \mathrm{E}-04$ | $0.00 \mathrm{E}+00$ | $9.74 \mathrm{E}-04$ |
| 0.6 | $6.75 \mathrm{E}-04$ | $0.00 \mathrm{E}+00$ | $6.75 \mathrm{E}-04$ |
| 0.7 | $2.52 \mathrm{E}-04$ | $0.00 \mathrm{E}+00$ | $2.52 \mathrm{E}-04$ |
| 0.8 | $0.00 \mathrm{E}+00$ | $0.00 \mathrm{E}+00$ | $0.00 \mathrm{E}+00$ |

Hand Solutions for Set 1, Test Case 6

| Peak Ground <br> Acceleration (g) | Site 4 | Site 5 | Site 6 |
| :---: | :---: | :---: | :---: |
| 0.001 | $7.75 \mathrm{E}-03$ | $7.75 \mathrm{E}-03$ | $7.75 \mathrm{E}-03$ |
| 0.01 | $7.75 \mathrm{E}-03$ | $7.75 \mathrm{E}-03$ | $7.75 \mathrm{E}-03$ |
| 0.05 | $7.75 \mathrm{E}-03$ | $7.75 \mathrm{E}-03$ | $7.75 \mathrm{E}-03$ |
| 0.075 | $7.75 \mathrm{E}-03$ | $7.75 \mathrm{E}-03$ | $7.75 \mathrm{E}-03$ |
| 0.10 | $7.74 \mathrm{E}-03$ | $7.37 \mathrm{E}-03$ | $7.74 \mathrm{E}-03$ |
| 0.15 | $7.64 \mathrm{E}-03$ | $5.81 \mathrm{E}-03$ | $7.64 \mathrm{E}-03$ |
| 0.20 | $7.31 \mathrm{E}-03$ | $3.57 \mathrm{E}-03$ | $7.31 \mathrm{E}-03$ |
| 0.25 | $6.73 \mathrm{E}-03$ | $1.52 \mathrm{E}-03$ | $6.73 \mathrm{E}-03$ |
| 0.30 | $5.99 \mathrm{E}-03$ | $2.26 \mathrm{E}-04$ | $5.99 \mathrm{E}-03$ |
| 0.40 | $4.27 \mathrm{E}-03$ | $0.00 \mathrm{E}+00$ | $4.27 \mathrm{E}-03$ |
| 0.50 | $2.64 \mathrm{E}-03$ | $0.00 \mathrm{E}+00$ | $2.64 \mathrm{E}-03$ |
| 0.60 | $1.35 \mathrm{E}-03$ | $0.00 \mathrm{E}+00$ | $1.35 \mathrm{E}-03$ |
| 0.65 | $8.63 \mathrm{E}-04$ | $0.00 \mathrm{E}+00$ | $8.63 \mathrm{E}-04$ |
| 0.70 | $4.74 \mathrm{E}-04$ | $0.00 \mathrm{E}+00$ | $4.74 \mathrm{E}-04$ |
| 0.80 | $0.00 \mathrm{E}+00$ | $0.00 \mathrm{E}+00$ | $0.00 \mathrm{E}+00$ |

Hand Solutions for Set 1, Test Case 7

| Peak Ground <br> Acceleration (g) | Site 4 | Site 5 | Site 6 |
| :---: | :---: | :---: | :---: |
| 0.001 | $1.14 \mathrm{E}-02$ | $1.14 \mathrm{E}-02$ | $1.14 \mathrm{E}-02$ |
| 0.01 | $1.14 \mathrm{E}-02$ | $1.14 \mathrm{E}-02$ | $1.14 \mathrm{E}-02$ |
| 0.05 | $1.14 \mathrm{E}-02$ | $1.03 \mathrm{E}-02$ | $1.14 \mathrm{E}-02$ |
| 0.1 | $1.01 \mathrm{E}-02$ | $7.65 \mathrm{E}-03$ | $1.01 \mathrm{E}-02$ |
| 0.15 | $8.72 \mathrm{E}-03$ | $5.66 \mathrm{E}-03$ | $8.72 \mathrm{E}-03$ |
| 0.2 | $7.75 \mathrm{E}-03$ | $3.50 \mathrm{E}-03$ | $7.75 \mathrm{E}-03$ |
| 0.25 | $6.84 \mathrm{E}-03$ | $1.40 \mathrm{E}-03$ | $6.84 \mathrm{E}-03$ |
| 0.3 | $5.95 \mathrm{E}-03$ | $4.89 \mathrm{E}-06$ | $5.95 \mathrm{E}-03$ |
| 0.35 | $5.06 \mathrm{E}-03$ | $0.00 \mathrm{E}+00$ | $5.06 \mathrm{E}-03$ |
| 0.4 | $4.18 \mathrm{E}-03$ | $0.00 \mathrm{E}+00$ | $4.18 \mathrm{E}-03$ |
| 0.45 | $3.34 \mathrm{E}-03$ | $0.00 \mathrm{E}+00$ | $3.34 \mathrm{E}-03$ |
| 0.5 | $2.56 \mathrm{E}-03$ | $0.00 \mathrm{E}+00$ | $2.56 \mathrm{E}-03$ |
| 0.55 | $1.85 \mathrm{E}-03$ | $0.00 \mathrm{E}+00$ | $1.85 \mathrm{E}-03$ |
| 0.6 | $1.20 \mathrm{E}-03$ | $0.00 \mathrm{E}+00$ | $1.20 \mathrm{E}-03$ |
| 0.7 | $1.87 \mathrm{E}-04$ | $0.00 \mathrm{E}+00$ | $1.87 \mathrm{E}-04$ |
| 0.80 | $0.00 \mathrm{E}+00$ | $0.00 \mathrm{E}+00$ | $0.00 \mathrm{E}+00$ |

Hand Solutions for Set 1, Test Case 9b

| Peak Ground Acceleration <br> $(\mathbf{g})$ | Site 1 | Site 2 | Site 7 |
| :---: | :---: | :---: | :---: |
| 0.001 | $1.68 \mathrm{E}-02$ | $1.68 \mathrm{E}-02$ | $1.68 \mathrm{E}-02$ |
| 0.01 | $1.68 \mathrm{E}-02$ | $1.68 \mathrm{E}-02$ | $1.68 \mathrm{E}-02$ |
| 0.05 | $1.68 \mathrm{E}-02$ | $1.68 \mathrm{E}-02$ | $1.68 \mathrm{E}-02$ |
| 0.1 | $1.68 \mathrm{E}-02$ | $1.68 \mathrm{E}-02$ | $1.68 \mathrm{E}-02$ |
| 0.15 | $1.68 \mathrm{E}-02$ | $1.68 \mathrm{E}-02$ | $1.68 \mathrm{E}-02$ |
| 0.2 | $1.68 \mathrm{E}-02$ | $1.68 \mathrm{E}-02$ | $1.68 \mathrm{E}-02$ |
| 0.25 | $1.68 \mathrm{E}-02$ | $1.68 \mathrm{E}-02$ | $1.68 \mathrm{E}-02$ |
| 0.3 | $1.68 \mathrm{E}-02$ | $1.68 \mathrm{E}-02$ | $8.76 \mathrm{E}-03$ |
| 0.35 | $1.68 \mathrm{E}-02$ | $1.68 \mathrm{E}-02$ | $8.46 \mathrm{E}-04$ |
| 0.4 | $1.68 \mathrm{E}-02$ | $1.68 \mathrm{E}-02$ | $0.00 \mathrm{E}+00$ |
| 0.45 | $1.68 \mathrm{E}-02$ | $1.68 \mathrm{E}-02$ | $0.00 \mathrm{E}+00$ |
| 0.5 | $1.68 \mathrm{E}-02$ | $0.00 \mathrm{E}+00$ | $0.00 \mathrm{E}+00$ |
| 0.55 | $1.46 \mathrm{E}-02$ | $0.00 \mathrm{E}+00$ | $0.00 \mathrm{E}+00$ |
| 0.6 | $1.22 \mathrm{E}-02$ | $0.00 \mathrm{E}+00$ | $0.00 \mathrm{E}+00$ |
| 0.7 | $7.66 \mathrm{E}-03$ | $0.00 \mathrm{E}+00$ | $0.00 \mathrm{E}+00$ |
| 0.8 | $2.70 \mathrm{E}-03$ | $0.00 \mathrm{E}+00$ | $0.00 \mathrm{E}+00$ |

## MEAN RESULTS FOR TEST CASES WITHOUT HAND SOLUTIONS

| Peak Ground <br> Acceleration (g) | Site 3 | Site 4 | Site 5 | Site 6 |
| :---: | :---: | :---: | :---: | :---: |
| 0.001 | $1.68 \mathrm{E}-02$ | $1.68 \mathrm{E}-02$ | $1.68 \mathrm{E}-02$ | $1.68 \mathrm{E}-02$ |
| 0.01 | $1.68 \mathrm{E}-02$ | $1.68 \mathrm{E}-02$ | $1.68 \mathrm{E}-02$ | $1.68 \mathrm{E}-02$ |
| 0.05 |  | $1.68 \mathrm{E}-02$ | $1.68 \mathrm{E}-02$ | $1.68 \mathrm{E}-02$ |
| 0.1 |  | $1.68 \mathrm{E}-02$ | $1.68 \mathrm{E}-02$ | $1.68 \mathrm{E}-02$ |
| 0.15 |  | $1.68 \mathrm{E}-02$ | $1.23 \mathrm{E}-02$ | $1.68 \mathrm{E}-02$ |
| 0.2 |  | $1.68 \mathrm{E}-02$ | $5.22 \mathrm{E}-03$ | $1.68 \mathrm{E}-02$ |
| 0.25 |  | $1.57 \mathrm{E}-02$ | $4.75 \mathrm{E}-04$ | $1.57 \mathrm{E}-02$ |
| 0.3 |  | $1.18 \mathrm{E}-02$ |  | $1.18 \mathrm{E}-02$ |
| 0.35 |  | $5.42 \mathrm{E}-03$ |  | $8.40 \mathrm{E}-03$ |
| 0.4 |  | $2.88 \mathrm{E}-03$ |  | $5.09 \mathrm{E}-03$ |
| 0.45 |  | $1.50 \mathrm{E}-03$ |  | $2.86 \mathrm{E}-03$ |
| 0.5 |  | $6.44 \mathrm{E}-04$ |  |  |
| 0.55 |  | $1.75 \mathrm{E}-04$ |  |  |
| 0.6 |  |  |  |  |

Mean Results Set 1, Case 5

| Peak Ground <br> Acceleration (g) | Site 1 | Site 2 | Site 3 | Site 7 |
| :---: | :---: | :---: | :---: | :---: |
| 0.001 | $4.00 \mathrm{E}-02$ | $4.00 \mathrm{E}-02$ | $4.00 \mathrm{E}-02$ | $4.00 \mathrm{E}-02$ |
| 0.01 | $4.00 \mathrm{E}-02$ | $4.00 \mathrm{E}-02$ | $4.00 \mathrm{E}-02$ | $4.00 \mathrm{E}-02$ |
| 0.05 | $4.00 \mathrm{E}-02$ | $4.00 \mathrm{E}-02$ |  | $4.00 \mathrm{E}-02$ |
| 0.1 | $3.99 \mathrm{E}-02$ | $3.31 \mathrm{E}-02$ |  | $3.31 \mathrm{E}-02$ |
| 0.15 | $3.46 \mathrm{E}-02$ | $1.22 \mathrm{E}-02$ |  | $1.22 \mathrm{E}-02$ |
| 0.2 | $2.57 \mathrm{E}-02$ | $4.85 \mathrm{E}-03$ |  | $4.85 \mathrm{E}-03$ |
| 0.25 | $1.89 \mathrm{E}-02$ | $1.76 \mathrm{E}-03$ |  | $1.76 \mathrm{E}-03$ |
| 0.3 | $1.37 \mathrm{E}-02$ | $2.40 \mathrm{E}-04$ |  | $2.40 \mathrm{E}-04$ |
| 0.35 | $9.88 \mathrm{E}-03$ |  |  |  |
| 0.4 | $6.93 \mathrm{E}-03$ |  |  |  |
| 0.45 | $4.84 \mathrm{E}-03$ |  |  |  |
| 0.5 | $3.36 \mathrm{E}-03$ |  |  |  |
| 0.55 | $2.34 \mathrm{E}-03$ |  |  |  |
| 0.6 | $1.52 \mathrm{E}-03$ |  |  |  |
| 0.7 | $5.12 \mathrm{E}-04$ |  |  |  |

Mean Results Set 1, Case 6

| Peak Ground <br> Acceleration (g) | Site 1 | Site 2 | Site 3 | Site 7 |
| :---: | :---: | :---: | :---: | :---: |
| 0.001 | $7.74 \mathrm{E}-03$ | $7.74 \mathrm{E}-03$ | $7.74 \mathrm{E}-03$ | $7.74 \mathrm{E}-03$ |
| 0.01 | $7.74 \mathrm{E}-03$ | $7.74 \mathrm{E}-03$ | $7.74 \mathrm{E}-03$ | $7.74 \mathrm{E}-03$ |
| 0.05 | $7.74 \mathrm{E}-03$ | $7.74 \mathrm{E}-03$ |  | $7.74 \mathrm{E}-03$ |
| 0.1 | $7.74 \mathrm{E}-03$ | $7.74 \mathrm{E}-03$ |  | $7.74 \mathrm{E}-03$ |
| 0.15 | $7.74 \mathrm{E}-03$ | $7.70 \mathrm{E}-03$ |  | $7.70 \mathrm{E}-03$ |
| 0.2 | $7.73 \mathrm{E}-03$ | $6.77 \mathrm{E}-03$ |  | $6.77 \mathrm{E}-03$ |
| 0.25 | $7.69 \mathrm{E}-03$ | $3.60 \mathrm{E}-03$ |  | $3.60 \mathrm{E}-03$ |
| 0.3 | $7.55 \mathrm{E}-03$ | $4.50 \mathrm{E}-04$ |  | $4.50 \mathrm{E}-04$ |
| 0.35 | $7.21 \mathrm{E}-03$ |  |  |  |
| 0.4 | $6.65 \mathrm{E}-03$ |  |  |  |
| 0.45 | $5.89 \mathrm{E}-03$ |  |  |  |
| 0.5 | $4.98 \mathrm{E}-03$ |  |  |  |

Mean Results Set 1, Case 7

| Peak Ground <br> Acceleration (g) | Site 1 | Site 2 | Site 3 | Site 7 |
| :---: | :---: | :---: | :---: | :---: |
| 0.001 | $1.16 \mathrm{E}-02$ | $1.16 \mathrm{E}-02$ | $1.16 \mathrm{E}-02$ | $1.16 \mathrm{E}-02$ |
| 0.01 | $1.16 \mathrm{E}-02$ | $1.16 \mathrm{E}-02$ | $1.16 \mathrm{E}-02$ | $1.16 \mathrm{E}-02$ |
| 0.05 | $1.16 \mathrm{E}-02$ | $1.16 \mathrm{E}-02$ |  | $1.16 \mathrm{E}-02$ |
| 0.1 | $1.16 \mathrm{E}-02$ | $1.06 \mathrm{E}-02$ |  | $1.06 \mathrm{E}-02$ |
| 0.15 | $1.09 \mathrm{E}-02$ | $7.79 \mathrm{E}-03$ |  | $7.79 \mathrm{E}-03$ |
| 0.2 | $9.67 \mathrm{E}-03$ | $6.76 \mathrm{E}-03$ |  | $6.76 \mathrm{E}-03$ |
| 0.25 | $8.66 \mathrm{E}-03$ | $3.62 \mathrm{E}-03$ |  | $3.62 \mathrm{E}-03$ |
| 0.3 | $7.96 \mathrm{E}-03$ |  |  |  |
| 0.35 | $7.39 \mathrm{E}-03$ |  |  |  |
| 0.4 | $6.71 \mathrm{E}-03$ |  |  |  |
| 0.45 | $5.87 \mathrm{E}-03$ |  |  |  |
| 0.5 | $4.95 \mathrm{E}-03$ |  |  |  |
| 0.55 | $4.00 \mathrm{E}-03$ |  |  |  |
| 0.6 | $2.91 \mathrm{E}-03$ |  |  |  |
| 0.7 | $8.50 \mathrm{E}-04$ |  |  |  |

Mean Results Set 1, Case 8a

| Peak Ground <br> Acceleration (g) | Site 1 | Site 2 | Site 3 | Site 4 | Site 5 | Site 6 | Site 7 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.001 | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ |
| 0.01 | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ | $1.57 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ |
| 0.05 | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ | $3.42 \mathrm{E}-03$ | $1.59 \mathrm{E}-02$ | $1.55 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ |
| 0.1 | $1.59 \mathrm{E}-02$ | $1.47 \mathrm{E}-02$ | $3.19 \mathrm{E}-04$ | $1.55 \mathrm{E}-02$ | $1.20 \mathrm{E}-02$ | $1.55 \mathrm{E}-02$ | $1.47 \mathrm{E}-02$ |
| 0.15 | $1.56 \mathrm{E}-02$ | $1.20 \mathrm{E}-02$ | $4.15 \mathrm{E}-05$ | $1.41 \mathrm{E}-02$ | $7.98 \mathrm{E}-03$ | $1.40 \mathrm{E}-02$ | $1.20 \mathrm{E}-02$ |
| 0.2 | $1.48 \mathrm{E}-02$ | $8.98 \mathrm{E}-03$ | $7.37 \mathrm{E}-06$ | $1.22 \mathrm{E}-02$ | $4.99 \mathrm{E}-03$ | $1.22 \mathrm{E}-02$ | $8.98 \mathrm{E}-03$ |
| 0.25 | $1.36 \mathrm{E}-02$ | $6.41 \mathrm{E}-03$ | $1.61 \mathrm{E}-06$ | $1.03 \mathrm{E}-02$ | $3.08 \mathrm{E}-03$ | $1.02 \mathrm{E}-02$ | $6.41 \mathrm{E}-03$ |
| 0.3 | $1.22 \mathrm{E}-02$ | $4.49 \mathrm{E}-03$ | $4.03 \mathrm{E}-07$ | $8.39 \mathrm{E}-03$ | $1.91 \mathrm{E}-03$ | $8.38 \mathrm{E}-03$ | $4.49 \mathrm{E}-03$ |
| 0.35 | $1.09 \mathrm{E}-02$ | $3.09 \mathrm{E}-03$ |  | $6.80 \mathrm{E}-03$ | $1.21 \mathrm{E}-03$ | $6.79 \mathrm{E}-03$ | $3.09 \mathrm{E}-03$ |
| 0.4 | $9.50 \mathrm{E}-03$ | $2.14 \mathrm{E}-03$ |  | $5.49 \mathrm{E}-03$ | $7.68 \mathrm{E}-04$ | $5.48 \mathrm{E}-03$ | $2.14 \mathrm{E}-03$ |
| 0.45 | $8.12 \mathrm{E}-03$ | $1.49 \mathrm{E}-03$ |  | $4.37 \mathrm{E}-03$ | $4.99 \mathrm{E}-04$ | $4.36 \mathrm{E}-03$ | $1.49 \mathrm{E}-03$ |
| 0.5 | $6.99 \mathrm{E}-03$ | $1.04 \mathrm{E}-03$ |  | $3.52 \mathrm{E}-03$ | $3.25 \mathrm{E}-04$ | $3.51 \mathrm{E}-03$ | $1.04 \mathrm{E}-03$ |
| 0.55 | $5.99 \mathrm{E}-03$ | $7.40 \mathrm{E}-04$ |  | $2.84 \mathrm{E}-03$ | $2.19 \mathrm{E}-04$ | $2.83 \mathrm{E}-03$ | $7.40 \mathrm{E}-04$ |
| 0.6 | $5.12 \mathrm{E}-03$ | $5.24 \mathrm{E}-04$ |  | $2.29 \mathrm{E}-03$ | $1.48 \mathrm{E}-04$ | $2.28 \mathrm{E}-03$ | $5.24 \mathrm{E}-04$ |
| 0.7 | $3.68 \mathrm{E}-03$ | $2.68 \mathrm{E}-04$ |  | $1.51 \mathrm{E}-03$ | $7.01 \mathrm{E}-05$ | $1.50 \mathrm{E}-03$ | $2.68 \mathrm{E}-04$ |
| 0.8 | $2.65 \mathrm{E}-03$ | $1.44 \mathrm{E}-04$ |  | $1.00 \mathrm{E}-03$ | $3.50 \mathrm{E}-05$ | $9.97 \mathrm{E}-04$ | $1.44 \mathrm{E}-04$ |
| 0.9 | $1.91 \mathrm{E}-03$ | $7.89 \mathrm{E}-05$ |  | $6.74 \mathrm{E}-04$ | $1.81 \mathrm{E}-05$ | $6.71 \mathrm{E}-04$ | $7.89 \mathrm{E}-05$ |
| 1 | $1.40 \mathrm{E}-03$ | $4.48 \mathrm{E}-05$ |  | $4.58 \mathrm{E}-04$ | $9.72 \mathrm{E}-06$ | $4.56 \mathrm{E}-04$ | $4.48 \mathrm{E}-05$ |

Mean Results Set 1, Case 8b

| Peak Ground <br> Acceleration <br> $\mathbf{( g )}$ | Site 1 | Site 2 | Site 3 | Site 4 | Site 5 | Site 6 | Site 7 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.001 | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ |
| 0.01 | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ | $1.57 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ |
| 0.05 | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ | $3.14 \mathrm{E}-03$ | $1.59 \mathrm{E}-02$ | $1.56 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ |
| 0.1 | $1.59 \mathrm{E}-02$ | $1.47 \mathrm{E}-02$ |  | $1.55 \mathrm{E}-02$ | $1.20 \mathrm{E}-02$ | $1.55 \mathrm{E}-02$ | $1.47 \mathrm{E}-02$ |
| 0.15 | $1.56 \mathrm{E}-02$ | $1.19 \mathrm{E}-02$ |  | $1.41 \mathrm{E}-02$ | $7.85 \mathrm{E}-03$ | $1.41 \mathrm{E}-02$ | $1.19 \mathrm{E}-02$ |
| 0.2 | $1.48 \mathrm{E}-02$ | $8.87 \mathrm{E}-03$ |  | $1.22 \mathrm{E}-02$ | $4.78 \mathrm{E}-03$ | $1.22 \mathrm{E}-02$ | $8.87 \mathrm{E}-03$ |
| 0.25 | $1.36 \mathrm{E}-02$ | $6.17 \mathrm{E}-03$ |  | $1.02 \mathrm{E}-02$ | $2.80 \mathrm{E}-03$ | $1.02 \mathrm{E}-02$ | $6.17 \mathrm{E}-03$ |
| 0.3 | $1.22 \mathrm{E}-02$ | $4.23 \mathrm{E}-03$ |  | $8.28 \mathrm{E}-03$ | $1.59 \mathrm{E}-03$ | $8.27 \mathrm{E}-03$ | $4.23 \mathrm{E}-03$ |
| 0.35 | $1.07 \mathrm{E}-02$ | $2.81 \mathrm{E}-03$ |  | $6.58 \mathrm{E}-03$ | $8.67 \mathrm{E}-04$ | $6.57 \mathrm{E}-03$ | $2.81 \mathrm{E}-03$ |
| 0.4 | $9.30 \mathrm{E}-03$ | $1.83 \mathrm{E}-03$ |  | $5.25 \mathrm{E}-03$ | $4.55 \mathrm{E}-04$ | $5.23 \mathrm{E}-03$ | $1.83 \mathrm{E}-03$ |
| 0.45 | $8.00 \mathrm{E}-03$ | $1.15 \mathrm{E}-03$ |  | $4.16 \mathrm{E}-03$ | $2.28 \mathrm{E}-04$ | $4.11 \mathrm{E}-03$ | $1.15 \mathrm{E}-03$ |
| 0.5 | $6.83 \mathrm{E}-03$ |  |  | $3.25 \mathrm{E}-03$ |  | $3.24 \mathrm{E}-03$ |  |
| 0.55 | $5.74 \mathrm{E}-03$ |  |  | $2.53 \mathrm{E}-03$ |  | $2.52 \mathrm{E}-03$ |  |
| 0.6 | $4.85 \mathrm{E}-03$ |  |  | $1.98 \mathrm{E}-03$ |  | $1.97 \mathrm{E}-03$ |  |
| 0.7 | $3.40 \mathrm{E}-03$ |  |  | $1.18 \mathrm{E}-03$ |  | $1.17 \mathrm{E}-03$ |  |
| 0.8 | $2.33 \mathrm{E}-03$ |  |  | $7.03 \mathrm{E}-04$ |  | $6.92 \mathrm{E}-04$ |  |
| 0.9 | $1.57 \mathrm{E}-03$ |  |  | $4.08 \mathrm{E}-04$ |  | $4.02 \mathrm{E}-04$ |  |
| 1 | $1.04 \mathrm{E}-03$ |  |  | $2.28 \mathrm{E}-04$ |  | $2.27 \mathrm{E}-04$ |  |

Mean Results Set 1, Case 8c

| Peak Ground <br> Acceleration <br> $\mathbf{( g )}$ | Site 1 | Site 2 | Site 3 | Site 4 | Site 5 | Site 6 | Site 7 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.001 | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ |
| 0.01 | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ | $1.57 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ |
| 0.05 | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ | $3.40 \mathrm{E}-03$ | $1.59 \mathrm{E}-02$ | $1.55 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ | $1.59 \mathrm{E}-02$ |
| 0.1 | $1.59 \mathrm{E}-02$ | $1.47 \mathrm{E}-02$ | $2.97 \mathrm{E}-04$ | $1.55 \mathrm{E}-02$ | $1.20 \mathrm{E}-02$ | $1.55 \mathrm{E}-02$ | $1.47 \mathrm{E}-02$ |
| 0.15 | $1.56 \mathrm{E}-02$ | $1.20 \mathrm{E}-02$ | $1.99 \mathrm{E}-05$ | $1.41 \mathrm{E}-02$ | $7.97 \mathrm{E}-03$ | $1.41 \mathrm{E}-02$ | $1.20 \mathrm{E}-02$ |
| 0.2 | $1.48 \mathrm{E}-02$ | $8.97 \mathrm{E}-03$ |  | $1.22 \mathrm{E}-02$ | $4.96 \mathrm{E}-03$ | $1.22 \mathrm{E}-02$ | $8.97 \mathrm{E}-03$ |
| 0.25 | $1.36 \mathrm{E}-02$ | $6.40 \mathrm{E}-03$ |  | $1.03 \mathrm{E}-02$ | $3.05 \mathrm{E}-03$ | $1.02 \mathrm{E}-02$ | $6.40 \mathrm{E}-03$ |
| 0.3 | $1.22 \mathrm{E}-02$ | $4.47 \mathrm{E}-03$ |  | $8.40 \mathrm{E}-03$ | $1.88 \mathrm{E}-03$ | $8.38 \mathrm{E}-03$ | $4.47 \mathrm{E}-03$ |
| 0.35 | $1.09 \mathrm{E}-02$ | $3.08 \mathrm{E}-03$ |  | $6.80 \mathrm{E}-03$ | $1.17 \mathrm{E}-03$ | $6.79 \mathrm{E}-03$ | $3.08 \mathrm{E}-03$ |
| 0.4 | $9.49 \mathrm{E}-03$ | $2.12 \mathrm{E}-03$ |  | $5.48 \mathrm{E}-03$ | $7.42 \mathrm{E}-04$ | $5.47 \mathrm{E}-03$ | $2.12 \mathrm{E}-03$ |
| 0.45 | $8.12 \mathrm{E}-03$ | $1.47 \mathrm{E}-03$ |  | $4.36 \mathrm{E}-03$ | $4.70 \mathrm{E}-04$ | $4.35 \mathrm{E}-03$ | $1.47 \mathrm{E}-03$ |
| 0.5 | $6.97 \mathrm{E}-03$ | $1.02 \mathrm{E}-03$ |  | $3.51 \mathrm{E}-03$ | $2.99 \mathrm{E}-04$ | $3.50 \mathrm{E}-03$ | $1.02 \mathrm{E}-03$ |
| 0.55 | $5.97 \mathrm{E}-03$ | $7.14 \mathrm{E}-04$ |  | $2.82 \mathrm{E}-03$ | $1.93 \mathrm{E}-04$ | $2.81 \mathrm{E}-03$ | $7.14 \mathrm{E}-04$ |
| 0.6 | $5.04 \mathrm{E}-03$ | $5.01 \mathrm{E}-04$ |  | $2.27 \mathrm{E}-03$ | $1.24 \mathrm{E}-04$ | $2.27 \mathrm{E}-03$ | $5.01 \mathrm{E}-04$ |
| 0.7 | $3.65 \mathrm{E}-03$ | $2.48 \mathrm{E}-04$ |  | $1.49 \mathrm{E}-03$ | $5.08 \mathrm{E}-05$ | $1.48 \mathrm{E}-03$ | $2.48 \mathrm{E}-04$ |
| 0.8 | $2.62 \mathrm{E}-03$ | $1.23 \mathrm{E}-04$ |  | $9.79 \mathrm{E}-04$ | $1.98 \mathrm{E}-05$ | $9.66 \mathrm{E}-04$ | $1.23 \mathrm{E}-04$ |
| 0.9 | $1.88 \mathrm{E}-03$ |  |  | $6.52 \mathrm{E}-04$ |  | $6.42 \mathrm{E}-04$ |  |
| 1 | $1.36 \mathrm{E}-03$ |  |  | $4.37 \mathrm{E}-04$ |  | $4.35 \mathrm{E}-04$ |  |

Mean Results Set 1, Case 9a

| Peak Ground <br> Acceleration <br> $\mathbf{( g )}$ | Site 1 | Site 2 | Site 3 | Site 4 | Site 5 | Site 6 | Site 7 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.001 | $1.69 \mathrm{E}-02$ | $1.69 \mathrm{E}-02$ | $1.69 \mathrm{E}-02$ | $1.69 \mathrm{E}-02$ | $1.69 \mathrm{E}-02$ | $1.69 \mathrm{E}-02$ | $1.69 \mathrm{E}-02$ |
| 0.01 | $1.69 \mathrm{E}-02$ | $1.69 \mathrm{E}-02$ | $1.68 \mathrm{E}-02$ | $1.69 \mathrm{E}-02$ | $1.69 \mathrm{E}-02$ | $1.69 \mathrm{E}-02$ | $1.69 \mathrm{E}-02$ |
| 0.05 | $1.69 \mathrm{E}-02$ | $1.68 \mathrm{E}-02$ | $6.90 \mathrm{E}-03$ | $1.68 \mathrm{E}-02$ | $1.66 \mathrm{E}-02$ | $1.68 \mathrm{E}-02$ | $1.68 \mathrm{E}-02$ |
| 0.1 | $1.68 \mathrm{E}-02$ | $1.65 \mathrm{E}-02$ | $1.14 \mathrm{E}-03$ | $1.66 \mathrm{E}-02$ | $1.40 \mathrm{E}-02$ | $1.66 \mathrm{E}-02$ | $1.58 \mathrm{E}-02$ |
| 0.15 | $1.65 \mathrm{E}-02$ | $1.48 \mathrm{E}-02$ | $1.99 \mathrm{E}-04$ | $1.56 \mathrm{E}-02$ | $1.03 \mathrm{E}-02$ | $1.56 \mathrm{E}-02$ | $1.31 \mathrm{E}-02$ |
| 0.2 | $1.58 \mathrm{E}-02$ | $1.26 \mathrm{E}-02$ | $2.79 \mathrm{E}-05$ | $1.39 \mathrm{E}-02$ | $6.99 \mathrm{E}-03$ | $1.39 \mathrm{E}-02$ | $1.02 \mathrm{E}-02$ |
| 0.25 | $1.47 \mathrm{E}-02$ | $1.02 \mathrm{E}-02$ |  | $1.20 \mathrm{E}-02$ | $4.64 \mathrm{E}-03$ | $1.20 \mathrm{E}-02$ | $7.50 \mathrm{E}-03$ |
| 0.3 | $1.34 \mathrm{E}-02$ | $7.89 \mathrm{E}-03$ |  | $1.02 \mathrm{E}-02$ | $3.07 \mathrm{E}-03$ | $1.02 \mathrm{E}-02$ | $5.40 \mathrm{E}-03$ |
| 0.35 | $1.19 \mathrm{E}-02$ | $6.02 \mathrm{E}-03$ |  | $8.45 \mathrm{E}-03$ | $2.04 \mathrm{E}-03$ | $8.43 \mathrm{E}-03$ | $3.85 \mathrm{E}-03$ |
| 0.4 | $1.05 \mathrm{E}-02$ | $4.61 \mathrm{E}-03$ |  | $6.95 \mathrm{E}-03$ | $1.36 \mathrm{E}-03$ | $6.94 \mathrm{E}-03$ | $2.73 \mathrm{E}-03$ |
| 0.45 | $9.15 \mathrm{E}-03$ | $3.50 \mathrm{E}-03$ |  | $5.70 \mathrm{E}-03$ | $9.21 \mathrm{E}-04$ | $5.69 \mathrm{E}-03$ | $1.94 \mathrm{E}-03$ |
| 0.5 | $7.94 \mathrm{E}-03$ | $2.64 \mathrm{E}-03$ |  | $4.66 \mathrm{E}-03$ | $6.22 \mathrm{E}-04$ | $4.65 \mathrm{E}-03$ | $1.39 \mathrm{E}-03$ |
| 0.55 | $6.85 \mathrm{E}-03$ | $1.98 \mathrm{E}-03$ |  | $3.81 \mathrm{E}-03$ | $4.22 \mathrm{E}-04$ | $3.80 \mathrm{E}-03$ | $9.92 \mathrm{E}-04$ |
| 0.6 | $5.90 \mathrm{E}-03$ | $1.53 \mathrm{E}-03$ |  | $3.16 \mathrm{E}-03$ | $2.91 \mathrm{E}-04$ | $3.11 \mathrm{E}-03$ | $7.20 \mathrm{E}-04$ |
| 0.7 | $4.30 \mathrm{E}-03$ | $8.78 \mathrm{E}-04$ |  | $2.12 \mathrm{E}-03$ | $1.37 \mathrm{E}-04$ | $2.11 \mathrm{E}-03$ | $3.74 \mathrm{E}-04$ |
| 0.8 | $3.16 \mathrm{E}-03$ | $5.00 \mathrm{E}-04$ |  | $1.43 \mathrm{E}-03$ | $6.41 \mathrm{E}-05$ | $1.43 \mathrm{E}-03$ | $1.96 \mathrm{E}-04$ |
| 0.9 | $2.30 \mathrm{E}-03$ | $2.97 \mathrm{E}-04$ |  | $9.87 \mathrm{E}-04$ | $2.91 \mathrm{E}-05$ | $9.83 \mathrm{E}-04$ | $1.01 \mathrm{E}-04$ |
| 1 | $1.68 \mathrm{E}-03$ | $1.73 \mathrm{E}-04$ |  | $6.77 \mathrm{E}-04$ | $1.23 \mathrm{E}-05$ | $6.74 \mathrm{E}-04$ | $4.99 \mathrm{E}-05$ |

Mean Results Set 1, Case 9b

| Peak Ground <br> Acceleration (g) | Site 3 | Site 4 | Site 5 | Site 6 |
| :---: | :---: | :---: | :---: | :---: |
| 0.001 | $1.69 \mathrm{E}-02$ | $1.69 \mathrm{E}-02$ | $1.69 \mathrm{E}-02$ | $1.69 \mathrm{E}-02$ |
| 0.01 | $1.69 \mathrm{E}-02$ | $1.69 \mathrm{E}-02$ | $1.69 \mathrm{E}-02$ | $1.69 \mathrm{E}-02$ |
| 0.05 | $1.69 \mathrm{E}-02$ | $1.69 \mathrm{E}-02$ | $1.69 \mathrm{E}-02$ | $1.69 \mathrm{E}-02$ |
| 0.1 |  | $1.69 \mathrm{E}-02$ | $1.69 \mathrm{E}-02$ | $1.69 \mathrm{E}-02$ |
| 0.15 |  | $1.69 \mathrm{E}-02$ | $1.69 \mathrm{E}-02$ | $1.69 \mathrm{E}-02$ |
| 0.2 |  | $1.69 \mathrm{E}-02$ | $1.11 \mathrm{E}-02$ | $1.69 \mathrm{E}-02$ |
| 0.25 |  | $1.69 \mathrm{E}-02$ | $5.74 \mathrm{E}-03$ | $1.69 \mathrm{E}-02$ |
| 0.3 |  | $1.46 \mathrm{E}-02$ | $2.02 \mathrm{E}-03$ | $1.67 \mathrm{E}-02$ |
| 0.35 |  | $1.19 \mathrm{E}-02$ |  | $1.45 \mathrm{E}-02$ |
| 0.4 | $9.80 \mathrm{E}-03$ |  | $1.19 \mathrm{E}-02$ |  |
| 0.45 |  | $7.90 \mathrm{E}-03$ |  | $9.77 \mathrm{E}-03$ |
| 0.5 |  | $5.81 \mathrm{E}-03$ |  | $7.87 \mathrm{E}-03$ |
| 0.55 |  | $4.09 \mathrm{E}-03$ |  | $5.72 \mathrm{E}-03$ |
| 0.6 |  | $1.77 \mathrm{E}-03$ |  | $4.06 \mathrm{E}-03$ |
| 0.7 |  | $2.85 \mathrm{E}-04$ |  | $1.72 \mathrm{E}-03$ |
| 0.8 |  |  |  | $2.80 \mathrm{E}-04$ |
| 0.9 |  |  |  |  |
| 1 |  |  |  |  |

Mean Results Set 1, Case 10

| Peak Ground <br> Acceleration (g) |  |  |  |  |  | Site 1 | Site 2 | Site 3 | Site 4 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.001 | $3.87 \mathrm{E}-02$ | $3.87 \mathrm{E}-02$ | $3.87 \mathrm{E}-02$ | $3.83 \mathrm{E}-02$ |  |  |  |  |  |
| 0.01 | $2.19 \mathrm{E}-02$ | $1.82 \mathrm{E}-02$ | $9.32 \mathrm{E}-03$ | $5.33 \mathrm{E}-03$ |  |  |  |  |  |
| 0.05 | $2.97 \mathrm{E}-03$ | $2.96 \mathrm{E}-03$ | $1.39 \mathrm{E}-03$ | $1.25 \mathrm{E}-04$ |  |  |  |  |  |
| 0.1 | $9.22 \mathrm{E}-04$ | $9.21 \mathrm{E}-04$ | $4.41 \mathrm{E}-04$ | $1.63 \mathrm{E}-06$ |  |  |  |  |  |
| 0.15 | $3.59 \mathrm{E}-04$ | $3.59 \mathrm{E}-04$ | $1.76 \mathrm{E}-04$ |  |  |  |  |  |  |
| 0.2 | $1.31 \mathrm{E}-04$ | $1.31 \mathrm{E}-04$ | $6.47 \mathrm{E}-05$ |  |  |  |  |  |  |
| 0.25 | $4.76 \mathrm{E}-05$ | $4.76 \mathrm{E}-05$ | $2.27 \mathrm{E}-05$ |  |  |  |  |  |  |
| 0.3 | $1.72 \mathrm{E}-05$ | $1.72 \mathrm{E}-05$ | $8.45 \mathrm{E}-06$ |  |  |  |  |  |  |
| 0.35 | $5.38 \mathrm{E}-06$ | $5.37 \mathrm{E}-06$ | $2.66 \mathrm{E}-06$ |  |  |  |  |  |  |
| 0.4 | $1.18 \mathrm{E}-06$ | $1.18 \mathrm{E}-06$ | $5.84 \mathrm{E}-07$ |  |  |  |  |  |  |

Mean Results Set 1, Case 11

| Peak Ground <br> Acceleration (g) | Site 1 | Site 2 | Site 3 | Site 4 |
| :---: | :---: | :---: | :---: | :---: |
| 0.001 | $3.87 \mathrm{E}-02$ | $3.87 \mathrm{E}-02$ | $3.87 \mathrm{E}-02$ | $3.84 \mathrm{E}-02$ |
| 0.01 | $2.18 \mathrm{E}-02$ | $1.81 \mathrm{E}-02$ | $9.27 \mathrm{E}-03$ | $5.33 \mathrm{E}-03$ |
| 0.05 | $2.83 \mathrm{E}-03$ | $2.83 \mathrm{E}-03$ | $1.32 \mathrm{E}-03$ | $1.18 \mathrm{E}-04$ |
| 0.1 | $7.91 \mathrm{E}-04$ | $7.90 \mathrm{E}-04$ | $3.79 \mathrm{E}-04$ | $1.24 \mathrm{E}-06$ |
| 0.15 | $2.43 \mathrm{E}-04$ | $2.44 \mathrm{E}-04$ | $1.18 \mathrm{E}-04$ |  |
| 0.2 | $7.33 \mathrm{E}-05$ | $7.32 \mathrm{E}-05$ | $3.60 \mathrm{E}-05$ |  |
| 0.25 | $2.23 \mathrm{E}-05$ | $2.21 \mathrm{E}-05$ | $1.08 \mathrm{E}-05$ |  |
| 0.3 | $6.42 \mathrm{E}-06$ | $6.50 \mathrm{E}-06$ | $2.95 \mathrm{E}-06$ |  |
| 0.35 | $1.31 \mathrm{E}-06$ | $1.30 \mathrm{E}-06$ | $6.18 \mathrm{E}-07$ |  |
| 0.4 | $1.72 \mathrm{E}-07$ | $1.60 \mathrm{E}-07$ | $7.92 \mathrm{E}-08$ |  |
| 0.45 | $3.05 \mathrm{E}-09$ | $3.09 \mathrm{E}-09$ | $1.34 \mathrm{E}-09$ |  |

FAULT 1


Fault Type: Strike Slip Dip: 90 degrees Fault Plane Depths: 0-12 km

FAULT 2


Cross-sectional view of Fault 2


Fault Type: Reverse
Dip: 60 degrees west
Fault Plane Depths: 1-12 km

SITES FOR FAULTS 1 \& 2


Site 1: On fault, at midpoint along strike
Site 2: 10 km west of fault, at midpoint along strike
Site 3: 50 km west of fault, at midpoint along strike
Site 4: On fault, at southern end
Site 5: 10 km south of fault along strike
Site 6: On fault, northern end
Site 7: 10 km east of fault, at midpoint along strike

AREA 1 WITH SITES


Site 1: At center of area
Site 2: 50 km from center (radially)
Site 3: On area boundary
Site 4: 25 km from boundary
$\uparrow N$

|  | PEER PSHA VERIFICATION | FAULT AND SITE GEOMETRY | Figure |
| :---: | :---: | :---: | :---: |
|  |  | FOR TEST CASE SET\#1 | 3.1 |



A-18


A-19



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A - 25


A - 26


A-27



A-29


A-30


A-31


A-32


A-33


A-34


A-35


A - 36



A-38



A - 40


A-41


A - 42



A-44







A - 50


A - 51


A-52


A - 53


A-54



A-56



A-58



A-60


A-61


A-62


A-63


A-64








A-71


A-72






























A-101


A-102





A-106
















(Coordinates are in Set2_Rev2_Coordinates_Results.xls)

|  | PEER PSHA VERIFICATION | FAULT AND SITE GEOMETRY | Figure |
| :---: | :---: | :---: | :---: |
|  |  | FOR CASES 1 AND 5 | 3.106 |




|  | PEER PSHA VERIFICATION | FAULT AND SITE GEOMETRY | Figure <br> 3.108 |
| :---: | :---: | :---: | :---: |



(Coordinates are in Set2_Rev2_Coordinates_Results.xls)

|  | PEER PSHA VERIFICATION | FAULT AND SITE GEOMETRY | Figure |
| :---: | :---: | :---: | :---: |
|  |  | FOR CASES 3 AND 4 | 3.110 |



A-127



|  | PEER PSHA VERIFICATION | LOGIC TREE FOR CASE 5 | Figure <br> 3.113 |
| :--- | :--- | :--- | :--- |



(Coordinates are in Set2_Rev2_Coordinates_Results.xls)

|  | PEER PSHA VERIFICATION | FAULT AND SITE GEOMETRY | Figure |
| :---: | :---: | :---: | :---: |
|  |  | FOR CASE 6 | 3.115 |



(Coordinates are in Set2_Rev2_Coordinates_Results.xls)

|  | PEER PSHA VERIFICATION | FAULT AND SITE GEOMETRY | Figure |
| :---: | :---: | :---: | :---: |
|  |  | FOR CASE 7 | 3.117 |



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[^0]:    Integration over magnitude zero.
    Use magnitude integration step size as small as necessary to model magnitude density function.
    3 For all cases, uniform slip with tapered slip at edges (see Fig. 3.2).
    $4 \quad$ No ruptures are to extend beyond the edge of the fault plane.
    5 Aspect Ratio to be maintained until maximum width is reached, then increase length (conserve area at the expense of aspect ratio).
    ${ }^{6}$ Downdip and along strike integration step size should be as small as necessary for uniform rupture location.

